

TRIGONOMETRY

SHEET 06

**Questions which can be solved by using
options & assuming values**

$$\theta = 45^\circ$$

$$= \frac{2+1+1}{2} = \textcircled{2}$$

1. $\frac{2 + \tan^2 \theta + \cot^2 \theta}{\sec \theta \cdot \operatorname{cosec} \theta}$ is equal to :

SSC CGL 4 June 2019 (Morning)

(a) $\cot \theta$ $\textcircled{1}$

(b) $\cos \theta \cdot \sin \theta$ $\textcircled{\frac{1}{2}}$

☒ (c) $\sec \theta \cdot \operatorname{cosec} \theta$ $\textcircled{2}$

(d) $\tan \theta$ $\textcircled{1}$

**2. The value of θ when $\sqrt{3}\cos\theta + \sin\theta = 1$
($0^\circ \leq \theta \leq 90^\circ$), is**

SSC CGL 4 June 2019 (Evening)

☒ (a) 90°
(c) 30°

(b) 60°
(d) 0°

$$\theta = 45^\circ$$

$$\sqrt{2+2} \times \sqrt{1-\frac{1}{2}}$$

$$= \sqrt{2} \cancel{2} \times \frac{1}{\sqrt{2}}$$

$$= \textcircled{\sqrt{2}} \checkmark$$

3. The value of $\sqrt{\sec^2 \theta + \operatorname{cosec}^2 \theta} \times$

$\sqrt{\tan^2 \theta - \sin^2 \theta}$ is equal to :

SSC CGL 6 June 2019 (Morning)

$$2\sqrt{2} \leftarrow \text{(a) } \operatorname{cosec} \theta \cdot \sec^2 \theta$$

$$\frac{1}{2\sqrt{2}} \leftarrow \text{(c) } \sin \theta \cdot \cos^2 \theta$$

$$\frac{1}{\sqrt{2}} \cdot \frac{1}{2}$$

$$\checkmark \text{(b) } \sin \theta \cdot \sec^2 \theta \quad \frac{1}{\sqrt{2}} \cdot 2 \cdot \sqrt{2}$$

$$\text{(d) } \operatorname{cosec} \theta \cdot \cos^2 \theta$$

$$\cancel{\sqrt{2}} \cdot \frac{1}{2} = \frac{1}{\sqrt{2}}$$

$$\theta = 45^\circ$$

$$* \sin \theta = \cos \theta = \frac{1}{\sqrt{2}}$$

$$* \sec \theta = \csc \theta = \sqrt{2}$$

$$* \tan \theta = \cot \theta = \underline{1}$$

$$\theta = 45^\circ$$

$$2 \times \left(\sqrt{2} - \frac{1}{\sqrt{2}} \right)^2 - (1-1)^2$$

$$= 2 \times \left(\frac{2-1}{\sqrt{2}} \right)^2$$

$$= 2 \times \left(\frac{1}{\sqrt{2}} \right)^2$$

$$= 2 \times \frac{1}{2}$$

4. $(\operatorname{cosec} A - \sin A)^2 + (\sec A - \cos A)^2 - (\cot A - \tan A)^2$ is equal to :

SSC CPO 2018, 16 March 2019 (Evening)

(a) 2

(b) 0

☒ (c) 1

(d) -1

Note:- जब भी options Number के Form में दिए हों तो आप उस सवाल को 100% Value Putting से बनाईजें।

$$3 \sin \theta = 2 \cos^2 \theta$$

✓ (a) $\theta = 30^\circ$

$3 \times \frac{1}{2}$	$2 \times \frac{3}{4}$
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$$\frac{1}{3} + \frac{4}{3} - 4$$

$$= \frac{5}{3} - 4$$

$$= \frac{5-12}{3} = -\frac{7}{3}$$

5. If $3 \sin \theta = 2 \cos^2 \theta$, $0^\circ < \theta < 90^\circ$, then the value of $(\tan^2 \theta + \sec^2 \theta - \operatorname{cosec}^2 \theta)$ is :

SSC CGL 10 June 2019 (Morning)

(a) -2

✓ (b) $-\frac{7}{3}$

(c) $\frac{7}{3}$

(d) 2

$$\frac{\cancel{\frac{1}{2}} \cdot \cancel{\frac{4}{3}}^2}{\frac{1}{3} + \frac{3}{4}} = \frac{13}{12}$$

6. If $\sin\theta \cdot \sec^2\theta = \frac{2}{3}$, ~~0°~~ $< \theta < \del{90^\circ}, then the value of $(\tan^2\theta + \cos^2\theta)$ is :$

SSC CHSL 3 July 2019 (Morning)

(a) $\frac{7}{6}$

(b) $\frac{11}{12}$

☒ (c) $\frac{13}{12}$

(d) $\frac{5}{4}$

$$\frac{2 \sin x}{1 + \sin x + \cos x} = \frac{c}{1 + \sin x}$$

$$\boxed{x = 45^\circ}$$

$$\Rightarrow \frac{\sqrt{2} \times \frac{1}{\sqrt{2}}}{1 + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}} = \frac{c}{1 + \frac{1}{\sqrt{2}}}$$

$$\Rightarrow \frac{\sqrt{2}}{1 + \sqrt{2}} = \frac{c \times \sqrt{2}}{\sqrt{2} + 1}$$

$$\boxed{c = 1}$$

7.

Let $a = \frac{2 \sin x}{1 + \sin x + \cos x}$ and $b = \frac{c}{1 + \sin x}$.

If $a = b$ then $c = ?$

SSC CGL 6 June 2019 (Afternoon)

- $\frac{1}{2}$ ~~(a)~~ $1 - \sin x \cdot \cos x$ ~~(b)~~ $1 + \sin x - \cos x$
 $\frac{3}{2}$ ~~(c)~~ $1 + \sin x \cdot \cos x$ ~~(d)~~ $1 + \cos x \cdot \sin x$

$$\frac{2 \sin x}{1 + \sin x + \cos x} = \frac{c}{1 + \sin x} \quad 7.$$

$$\boxed{x = 90^\circ} \begin{cases} c = 0 \\ s = 1 \end{cases}$$

$$\frac{2}{1+1+0} = \frac{c}{1+1}$$

$$\boxed{c = 2}$$

$$\text{Let } a = \frac{2 \sin x}{1 + \sin x + \cos x} \text{ and } b = \frac{c}{1 + \sin x}.$$

If $a = b$ then $c = ?$

SSC CGL 6 June 2019 (Afternoon)

- (a) $\textcircled{1} - \overset{0}{\sin x} \cdot \overset{0}{\cos x}$ (b) $\checkmark \textcircled{1} + \overset{1}{\sin x} - \overset{0}{\cos x}$
(c) $\textcircled{1} + \sin x \cdot \cos x$ (d) $\textcircled{1} + \cos x \cdot \sin x$

$$\alpha = 0^\circ \quad \beta = 45^\circ$$

8.

$$\sqrt{2} + \frac{1/\sqrt{2}}{1/\sqrt{2} - 1} = \frac{x}{0 - \frac{1}{\sqrt{2}}} + \frac{1/\sqrt{2}}{1/\sqrt{2} + 1}$$

$$\Rightarrow \sqrt{2} + \frac{1}{1 - \sqrt{2}} = -\sqrt{2}x + \frac{1}{1 + \sqrt{2}}$$

$$\Rightarrow \cancel{\sqrt{2}} - \cancel{\sqrt{2}} - 1 = -\sqrt{2}x + \sqrt{2} - 1$$

$$\Rightarrow \cancel{\sqrt{2}}x = \sqrt{2} \quad \Rightarrow x = 1$$

If $\frac{\cos \alpha}{\sin \alpha + \cos \beta} + \frac{\cos \beta}{\sin \beta - \cos \alpha} = \frac{x}{\sin \alpha - \cos \beta}$

+ $\frac{\cos \beta}{\sin \beta + \cos \alpha}$, then x is equal to :

SSC CHSL 8 July 2019 (Morning)

- (a) $\cos \beta$
(c) $\sin \beta$

- (b) $\cos \alpha$
(d) $\sin \alpha$

$$\left(2 \times \left(\frac{1}{\sqrt{2}}\right)^6 - 1\right) (2 \times 1 + 2)$$

$$= \left(2 \times \frac{1}{8} - 1\right) \times 4$$

$$= \left(\frac{1}{4} - 1\right) \times 4$$

$$= -\frac{3}{4} \times 4$$

9. The value of the expression
 $(\cos^6\theta + \sin^6\theta - 1)(\tan^2\theta + \cot^2\theta + 2)$ is :
SSC CGL Tier-II (11 September, 2019)

(a) 0

(b) -1

✓ (c) -3

(d) 1

$A=0^\circ$

10. $\frac{(2\sin A)(1 + \sin A)}{1 + \sin A + \cos A}$ is equal to :

SSC CGL Tier-II (11 September, 2019)

- (a) $1 + \sin A - \cos A$ (b) $1 - \sin A \cdot \cos A$
 (c) $1 + \cos A - \sin A$ (d) $1 + \sin A \cdot \cos A$

Note $\sin 0, \cos 0$

$\theta = 45^\circ \times$ / $\theta = 0^\circ \checkmark$
 $90^\circ \checkmark$

$$\phi = 45^\circ$$

- 11.** The value of $\tan^2\phi + \cot^2\phi - \sec^2\phi \cdot \operatorname{cosec}^2\phi$ is equal to :

SSC CGL Tier-II (12 September, 2019)

- ☒ (a) -2 (b) 1
(c) 0 (d) -1

$$1+1-2 \times 2$$

$$\begin{aligned} & (1+1-\sqrt{2}) \left(1 + \frac{1}{\sqrt{2}} \times \sqrt{2}\right) \sqrt{2} \\ &= (2-\sqrt{2}) (1+\sqrt{2}) \times \sqrt{2} \\ &= (2-\sqrt{2}) (2+\sqrt{2}) \\ &= 4-2 = \textcircled{2} \end{aligned}$$

12. The value of $(1 + \cot\theta - \operatorname{cosec}\theta)(1 + \cos\theta + \sin\theta) \sec\theta = ?$

SSC CGL Tier-II (13 September, 2019)

(a) -2

☒ (b) 2

(c) $\sec\theta \cdot \operatorname{cosec}\theta$

(d) $\sin\theta \cdot \cos\theta$

$$\left(1 + \frac{4}{3} - \frac{5}{3}\right) \left(1 + \frac{4}{5} + \frac{3}{5}\right) \frac{5}{4} \quad \mathbf{12.}$$

The value of $(1 + \underline{\cot\theta} - \operatorname{cosec}\theta)(1 + \cos\theta + \sin\theta) \sec\theta = ?$

SSC CGL Tier-II (13 September, 2019)

(a) -2

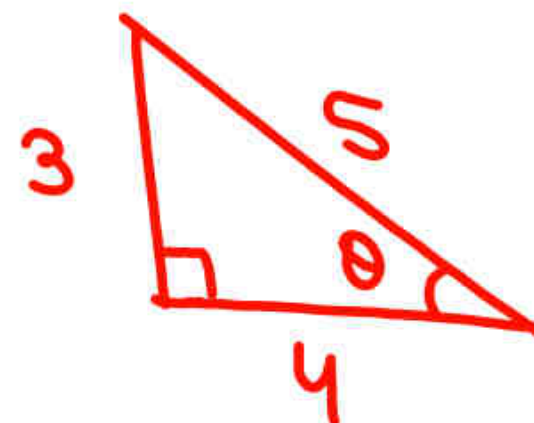
☒ (b) 2

(c) $\sec\theta \cdot \operatorname{cosec}\theta$

(d) $\sin\theta \cdot \cos\theta$

$$\frac{5}{4} \times \frac{5}{3} = \frac{25}{12}$$

$$\frac{3}{5} \times \frac{4}{5} = \frac{12}{25}$$



$$= \left(1 - \frac{1}{3}\right) \left(1 + \frac{7}{5}\right) \times \frac{5}{4}$$

$$= \frac{2}{3} \times \frac{12}{5} \times \frac{5}{4}$$

$$= \textcircled{2}$$

$$\theta = 0^\circ$$

$$S = 0 \quad C = 1$$

$$\frac{2(0+1) - 3(0+1)}{1 - 0 - 2}$$

$$= \frac{2 - 3}{-1} = \cancel{\frac{1}{1}}$$

13. The value of

$$\frac{2(\sin^6 \theta + \cos^6 \theta) - 3(\sin^4 \theta + \cos^4 \theta)}{\cos^4 \theta - \sin^4 \theta - 2\cos^2 \theta} \text{ is :}$$

SSC CGL Tier-II (13 September, 2019)

(a) - 1

(b) - 2

(c) 2

☒ (d) 1

$$\theta = 45^\circ$$

$$\begin{aligned} &= \frac{1 - \frac{1}{2} \times \frac{1}{2}}{\frac{1}{4} + \frac{1}{4}} - 1 \\ &= \frac{1 - \frac{1}{4}}{\frac{2}{4}} - 1 \\ &= \frac{\frac{3}{4}}{\frac{1}{2}} - 1 \\ &= \frac{3}{2} - 1 \\ &= \frac{3-2}{2} \\ &= \frac{1}{2} \end{aligned}$$

14. The value of $\frac{1 - \sin^2 \theta \cos^2 \theta}{\sin^4 \theta + \cos^4 \theta} - 1$ is :

SSC CGL 7 March 2020 (Morning)

- (a) $2\sin^2 \theta \cos^2 \theta$ (b) -1
(c) 0 (d) 1

$$2 \times \frac{1}{2} \times \frac{1}{2}$$

16. If $x = \operatorname{cosec} A + \cos A$ and $y = \operatorname{cosec} A - \cos A$, then find the value of

$$\left(\frac{2}{2 \operatorname{cosec} A} \right)^2 + \left(\frac{2 \cos A}{2} \right)^2 - 1$$

$$= (\sin A)^2 + (\cos A)^2 - 1$$
$$= 1 - 1 = 0$$

$$\left(\frac{2}{x+y} \right)^2 + \left(\frac{x-y}{2} \right)^2 - 1.$$

SSC CHSL 19/10/2020 (Morning)

(a) 3

(c) 2

☒ (b) 0

(d) 1

$$x = \operatorname{cosec} A + \cos A$$
$$y = \operatorname{cosec} A - \cos A$$

$$A = 45^\circ$$

17. The value of $(\tan^2 A + \cot^2 A - 2) - \sec^2 A \operatorname{cosec}^2 A$ is :

CGL 2019 Tier-II (16/10/2020) →

- ✓ (a) - 4
(c) 1

- (b) - 1
(d) 4

$$(1+1-2)-(2 \times 2)$$
$$0-4$$

$$3(0-1)^4 + 6(0+1)^2 + 4(0+1)$$

20.

$$= 3 + 6 + 4$$

The value of $3(\sin x - \cos x)^4 + 6(\sin x + \cos x)^2 + 4(\sin^6 x + \cos^6 x)$ is :

(a) 14

(b) 11

(c) 12

(d) 13

$$, x=0 \quad s=0 \quad c=1$$

$$3(0+1) + 2(0+1) + 12 \times 0 \times 1$$
$$= 3 + 2 + 0$$

21.

The value of the following is : $3(\sin^4\theta + \cos^4\theta) + 2(\sin^6\theta + \cos^6\theta) + 12\sin^2\theta.\cos^2\theta$

(a) 0

(b) 3

(c) 2

(d) 5

$$\theta = 0 \quad S = 0 \quad C = 1$$

$$\frac{x}{a} = \sin\theta + \cos\theta$$

$$\Rightarrow \boxed{\frac{x}{a} = 1}$$

$$\frac{y}{b} = \sin\theta - \cos\theta$$

$$\boxed{\frac{y}{b} = -1}$$

$$1^2 + (-1)^2 = 2$$

$$\theta = 0 \quad \sin = 0 \quad \cos = 1$$

22. If $x = a(\sin\theta + \cos\theta)$, $y = b(\sin\theta - \cos\theta)$,

then the value of $\frac{x^2}{a^2} + \frac{y^2}{b^2}$ is :

(a) 0

(b) 1

☒ (c) 2

(d) -2

$$(1 + \sin \alpha)(1 + \sin \beta)(1 + \sin \gamma) = k$$

$$(1 - \sin \alpha)(1 - \sin \beta)(1 - \sin \gamma) = k$$

$$(1 - \sin^2 \alpha)(1 - \sin^2 \beta)(1 - \sin^2 \gamma) = k^2$$

$$\Rightarrow \cos^2 \alpha \cdot \cos^2 \beta \cdot \cos^2 \gamma = k^2$$

$$\Rightarrow \pm \cos \alpha \cos \beta \cos \gamma = k$$

$$\alpha = \beta = \gamma = 0$$

24. If $(1 + \sin\alpha)(1 + \sin\beta)(1 + \sin\gamma) = (1 - \sin\alpha)(1 - \sin\beta)(1 - \sin\gamma)$, then each side is equal to :

- ☒ (a) $\pm \cos\alpha. \cos\beta. \cos\gamma$
- ☐ (b) $\pm \sin\alpha. \sin\beta. \sin\gamma$
- ☐ (c) $\pm \sin\alpha. \cos\beta. \cos\gamma.$
- ☐ (d) $\pm \sin\alpha. \sin\beta. \cos\gamma$

$$\theta = 0^\circ$$

$$x = 0 + 0 = 0$$

$$y = 1 + 1 = 2$$

$$\begin{aligned} & (x^2 + y^2)(x^2 + y^2 - 3) \\ &= (0 + 4)(0 + 4 - 3) \\ &= 4 \times 1 = \textcircled{4} \end{aligned}$$

26. If $\sin\theta + \sin 2\theta = x$ and $\cos\theta + \cos 2\theta = y$, then $(x^2 + y^2)(x^2 + y^2 - 3) = ?$

☒ (a) $2y = 4$

(b) $3y = 6$

(c) $-2y = -4$

(d) $4y = 8$

30. If $\overset{0}{P} + \overset{60^\circ}{Q} + \overset{0}{R} = 60^\circ$, then what is the value of $\cos Q \cdot \cos R (\cos P - \sin P) + \sin Q \cdot \sin R (\sin P - \cos P)$

(a) $\frac{1}{2}$

(b) $\frac{\sqrt{3}}{2}$

(c) $\frac{1}{\sqrt{2}}$

(d) $\sqrt{2}$

$$= \frac{1}{2} \times 1 (1 - 0) + \frac{\sqrt{3}}{2} \times 0 \times \underline{\hspace{1cm}}$$

$$= \left(\frac{1}{2}\right) + 0$$

$$\phi = 45^\circ$$

34. The value of $\tan^2\phi + \cot^2\phi - \sec^2\phi \cdot \operatorname{cosec}^2\phi$ is equal to : $1 + 1 - 2 \times 2 = -2$

SSC CGL Tier-II (12 September 2019)

☒ (a) - 2

(b) 1

(c) 0

(d) - 1

$A = 45^\circ$

41. The value of $(\tan^2 A + \cot^2 A - 2) - \sec^2 A \operatorname{cosec}^2 A$ is :

SSC CGL 2019, Tier-II (16/10/2020)

☒ (a) -4

(b) -1

(c) 1

(d) 4

$(1+1-2) - 2 \times 2$

$0 - 4$

