

TRIGONOMETRY

SHEET 06

**Questions which can be solved by using
options & assuming values**

$$\theta = 45^\circ$$

$$= \frac{2+1+1}{2} = 2$$

1. $\frac{2 + \tan^2 \theta + \cot^2 \theta}{\sec \theta \cdot \cosec \theta}$ is equal to :

SSC CGL 4 June 2019 (Morning)

- (a) $\cot \theta$ ①
- (b) $\cos \theta \cdot \sin \theta$ $\frac{1}{2}$ ②
- ~~(c) $\sec \theta \cdot \cosec \theta$~~ ③
- (d) $\tan \theta$ ④

2. The value of θ when $\sqrt{3}\cos\theta + \sin\theta = 1$ ($0^\circ \leq \theta \leq 90^\circ$), is

SSC CGL 4 June 2019 (Evening)

- (a) ~~90°~~
- (b) 60°
- (c) 30°
- (d) 0°

$$\theta = 45^\circ$$

$$\sqrt{2+2} \times \sqrt{1-\frac{1}{2}}$$

$$= \sqrt{2} \cancel{\times} \frac{1}{\sqrt{2}}$$

$$= \sqrt{2}$$

3. The value of $\sqrt{\sec^2 \theta + \cosec^2 \theta} \times \sqrt{\tan^2 \theta - \sin^2 \theta}$ is equal to :

SSC CGL 6 June 2019 (Morning)

- $2\sqrt{2}$ (a) $\cosec \theta \cdot \sec^2 \theta$ (b) $\sin \theta \cdot \sec^2 \theta$ $\frac{1}{\sqrt{2}} \cdot 2\sqrt{2}$
 $\frac{1}{2\sqrt{2}}$ (c) $\sin \theta \cdot \cos^2 \theta$ (d) $\cosec \theta \cdot \cos^2 \theta$

$$\frac{1}{\sqrt{2}} \cdot \frac{1}{2}$$

$$\cancel{\sqrt{2}} \cdot \frac{1}{2} = \frac{1}{2}$$

$$\theta = 45^\circ$$

$$* \sin \theta = \cos \theta = \frac{1}{\sqrt{2}}$$

$$* \sec \theta = \csc \theta = \sqrt{2}$$

$$* \tan \theta = \cot \theta = \underline{1}$$

$$\theta = 45^\circ$$

$$\begin{aligned}
 & 2 \times \left(\sqrt{2} - \frac{1}{\sqrt{2}} \right)^2 - (1-1)^2 \\
 &= 2 \times \left(\frac{2-1}{\sqrt{2}} \right)^2 \\
 &= 2 \times \left(\frac{1}{\sqrt{2}} \right)^2 \\
 &= \cancel{2} \times \frac{1}{2}
 \end{aligned}$$

4. $(\cosec A - \sin A)^2 + (\sec A - \cos A)^2 - (\cot A - \tan A)^2$ is equal to :

SSC CPO 2018, 16 March 2019 (Evening)

- (a) 2
- (c) 1
- (b) 0
- (d) -1

Note:- यहाँ में options Number $\frac{1}{4}$ form
में हैं इन्हीं पर आप उस सवाल
को 100% Value Putting से जवाबें।

$$3\sin\theta = 2\cos^2\theta$$

(a) $\theta = 30^\circ$

$$\textcircled{3} \times \frac{1}{2}$$

$$\textcircled{2} \times \frac{3}{4}$$

$$\frac{1}{3} + \frac{4}{3} - 4$$

$$= \frac{5}{3} - 4$$

$$= \frac{5-12}{3} = -\frac{7}{3}$$

5. If $3\sin\theta = 2\cos^2\theta$, $0^\circ < \theta < 90^\circ$, then the value of $(\tan^2\theta + \sec^2\theta - \operatorname{cosec}^2\theta)$ is :

SSC CGL 10 June 2019 (Morning)

(a) - 2

(c) $\frac{7}{3}$

(b) $-\frac{7}{3}$

(d) 2

$$\frac{\frac{1}{2} \cdot \frac{4}{3}^2}{\frac{1}{3} + \frac{3}{4}} = \frac{13}{12}$$

6. If $\sin\theta \cdot \sec^2\theta = \frac{2}{3}$, $0^\circ < \theta < 90^\circ$, then the value of $(\tan^2\theta + \cos^2\theta)$ is :

SSC CHSL 3 July 2019 (Morning)

(a) $\frac{7}{6}$

(b) $\frac{11}{12}$

(c) $\frac{13}{12}$

(d) $\frac{5}{4}$

$$\frac{2\sin x}{1+\sin x + \cos x} = \frac{C}{1+\sin x}$$

$$x = 45^\circ$$

$$\Rightarrow \frac{\sqrt{2} \cancel{\sin 1}}{1 + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}} = \frac{C}{1 + \frac{1}{\sqrt{2}}}$$

$$\Rightarrow \frac{\sqrt{2}}{1 + \sqrt{2}} = \frac{C \times \sqrt{2}}{\sqrt{2} + 1}$$

$$(C=1)$$

7. Let $a = \frac{2\sin x}{1 + \sin x + \cos x}$ and $b = \frac{c}{1 + \sin x}$.
 If $a = b$ then $c = ?$

SSC CGL 6 June 2019 (Afternoon)

- | | | |
|---------------|--|--|
| $\frac{1}{2}$ | (A) $1 - \sin x \cdot \cos x$ | (B) $1 + \sin x - \cos x$ |
| $\frac{3}{2}$ | (C) $1 + \sin x \cdot \cos x$ | (D) $1 + \cos x \cdot \sin x$ |

$$\frac{2\sin x}{1+\sin x + \cos x} = \frac{c}{1+\sin x}$$

$x = 90^\circ$ $\Rightarrow c=0$
 $s=1$

$$\frac{2}{1+1+0} = \frac{c}{1+1}$$

$c=2$

7.

Let $a = \frac{2\sin x}{1 + \sin x + \cos x}$ and $b = \frac{c}{1 + \sin x}$.

If $a = b$ then $c = ?$

SSC CGL 6 June 2019 (Afternoon)

- (a) $1 - \cancel{\sin x \cdot \cos x}$
- (b) $1 + \cancel{\sin x} - \cancel{\cos x}$
- (c) $1 + \cancel{\sin x \cdot \cos x}$
- (d) $1 + \cancel{\cos x \cdot \sin x}$

$$\frac{\alpha = 0^\circ}{\beta = 45^\circ}$$

$$\frac{\sqrt{2} + \frac{1}{\sqrt{2}}}{\sqrt{2}-1} = \frac{x}{0-1} + \frac{1}{\sqrt{2}+1}$$

$$\Rightarrow \sqrt{2} + \frac{1}{1-\sqrt{2}} = -\sqrt{2}x + \frac{1}{1+\sqrt{2}}$$

$$\Rightarrow \cancel{\sqrt{2}} - \cancel{\sqrt{2}} - 1 = -\sqrt{2}x + \sqrt{2} - 1$$

$$\Rightarrow \cancel{\sqrt{2}}x = \cancel{\sqrt{2}} \quad \text{∴ } x = 1$$

8.

If $\frac{\cos\alpha}{\sin\alpha + \cos\beta} + \frac{\cos\beta}{\sin\beta - \cos\alpha} = \frac{x}{\sin\alpha - \cos\beta}$
 $+ \frac{\cos\beta}{\sin\beta + \cos\alpha}$, then x is equal to :

SSC CHSL 8 July 2019 (Morning)

(a) $\cos\beta \frac{1}{\sqrt{2}}$
 (c) $\sin\beta \frac{1}{\sqrt{2}}$

(b) $\cos\alpha \frac{1}{0}$
 (d) $\sin\alpha \frac{1}{0}$

$$\left(2 \times \left(\frac{1}{\sqrt{2}} - 1\right)\right) (2 \times 1 + 2)$$

$$= \left(2 \times \frac{1}{8} - 1\right) \times 4$$

$$= \left(\frac{1}{4} - 1\right) \times 4$$

$$= -\frac{3}{4} \times 4$$

9.

The value of the expression **$(\cos^6\theta + \sin^6\theta - 1)(\tan^2\theta + \cot^2\theta + 2)$ is :****SSC CGL Tier-II (11 September, 2019)**

(a) 0

(c) - 3

(b) - 1

(d) 1

$A=0^\circ$ o ~~w~~ 10.

$\frac{(2\sin A)(1 + \sin A)}{1 + \sin A + \cos A}$ is equal to :

SSC CGL Tier-II (11 September, 2019)

- o (a) $1 + \cancel{\sin A} - \cos A$ (b) $1 - \cancel{\sin A \cdot \cos A}$
 2 (c) $1 + \cos A - \cancel{\sin A}$ (d) $1 + \cancel{\sin A \cdot \cos A}$

Note $\sin \theta, \cos \theta$

$0 = 45^\circ \times$ | $0 = 0^\circ \checkmark$
 $90^\circ \checkmark$

$$\phi = 45^\circ$$

11. The value of $\tan^2\phi + \cot^2\phi - \sec^2\phi \cdot \cosec^2\phi$ is equal to :

SSC CGL Tier-II (12 September, 2019)

- (a) - 2
- (b) 1
- (c) 0
- (d) - 1

$$1+1-2\times2$$

$$\begin{aligned}
 & (1+1-\sqrt{2}) \left(1 + \frac{1}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} \right) \sqrt{2} \\
 &= (2-\sqrt{2}) (1+\sqrt{2}) \times \sqrt{2} \\
 &= (2-\sqrt{2})(2+\sqrt{2}) \\
 &= 4-2 = \textcircled{2}
 \end{aligned}$$

12. The value of $\frac{(1 + \cot\theta - \operatorname{cosec}\theta)(1 + \cos\theta + \sin\theta)}{\sec\theta} = ?$

SSC CGL Tier-II (13 September, 2019)

- (a) - 2
- (b) 2
- (c) $\sec\theta \cdot \operatorname{cosec}\theta$
- (d) $\sin\theta \cdot \cos\theta$

$$\left(1 + \frac{4}{3} - \frac{5}{3}\right) \left(1 + \frac{4}{5} + \frac{3}{5}\right) \times \frac{5}{4}$$

12.

The value of $(1 + \underline{\cot\theta} - \cosec\theta)(1 + \cos\theta + \sin\theta) \sec\theta = ?$

$$= \left(1 - \frac{1}{3}\right) \left(1 + \frac{7}{5}\right) \times \frac{5}{4}$$

$$= \frac{2}{3} \times \frac{12}{5} \times \frac{5}{4}$$

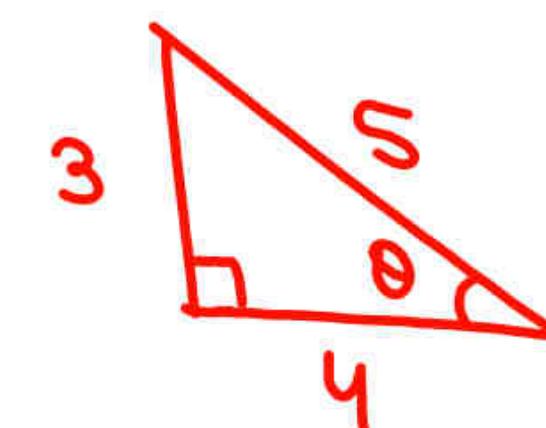
$$= \textcircled{2}$$

- (a) - 2
- (c) $\sec\theta \cdot \cosec\theta$

$$\frac{5}{4} \times \frac{5}{3} = \frac{25}{12}$$

- (b) ~~2~~
- (d) $\sin\theta \cdot \cos\theta$

SSC CGL Tier-II (13 September, 2019)



$$\frac{3}{5} \times \frac{4}{5} = \frac{12}{25}$$

$$\theta = 0^\circ$$

$$S=0 \quad C=1$$

$$\frac{2(0+1) - 3(0+1)}{1-0-2}$$

$$= \frac{2-3}{-1} = \cancel{\frac{-1}{1}}$$

13.

The value of

$$\frac{2(\sin^6\theta + \cos^6\theta) - 3(\sin^4\theta + \cos^4\theta)}{\cos^4\theta - \sin^4\theta - 2\cos^2\theta} \text{ is :}$$

SSC CGL Tier-II (13 September, 2019)

- (a) - 1
 (c) 2

- (b) - 2
 (d) 1

$$\theta = 45^\circ$$

$$= \frac{1 - \frac{1}{2} \times \frac{1}{2}}{\frac{1}{4} + \frac{1}{4}} - 1$$

$$= \frac{\frac{3}{4}}{\frac{2}{4}} - 1$$

$$= \frac{3}{2} - 1$$

$$= \frac{1}{2}$$

14. The value of $\frac{1 - \sin^2\theta \cos^2\theta}{\sin^4\theta + \cos^4\theta} - 1$ is :

SSC CGL 7 March 2020 (Morning)

- (a) $2\sin^2\theta \cos^2\theta$
- (b) -1
- (c) 0
- (d) 1

$$2 \times \frac{1}{2} \times \frac{1}{2}$$

$$\frac{1+\frac{1}{2}-\frac{\sqrt{3}}{2}}{1+\frac{1}{2}+\frac{\sqrt{3}}{2}} + \frac{1+\frac{1}{2}+\frac{\sqrt{3}}{2}}{1+\frac{1}{2}-\frac{\sqrt{3}}{2}}$$

$$= \frac{\frac{3}{2}-\frac{\sqrt{3}}{2}}{\frac{3}{2}+\frac{\sqrt{3}}{2}} + \frac{\frac{3}{2}+\frac{\sqrt{3}}{2}}{\frac{3}{2}-\frac{\sqrt{3}}{2}}$$

$$= \frac{\cancel{\sqrt{3}}(\sqrt{3}-1)}{\cancel{\sqrt{3}}(\sqrt{3}+1)} + \frac{\cancel{\sqrt{3}}(\sqrt{3}+1)}{\cancel{\sqrt{3}}(\sqrt{3}-1)}$$

$$= \frac{(\sqrt{3}-1)^2 + (\sqrt{3}+1)^2}{3-1} = \frac{3+1-2\cancel{\sqrt{3}} + 3+1+2\cancel{\sqrt{3}}}{2} = 4$$

15. If $\frac{(1+\sin\theta - \cos\theta)}{(1+\sin\theta + \cos\theta)} + \frac{(1+\sin\theta + \cos\theta)}{(1+\sin\theta - \cos\theta)} = 4$, then which of the following values will be suitable for θ ?

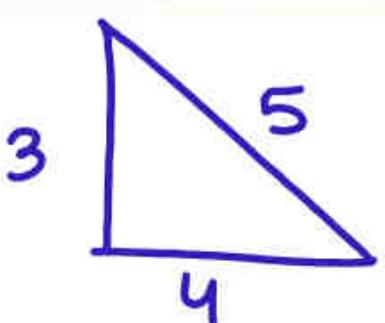
SSC CHSL 13/10/2020 (Afternoon)

- (a) 90° (b) 60°
 (c) 45° (d) 30°

$$x = \frac{5}{3} + \frac{4}{5}$$

$$= \left(\frac{37}{15} \right)$$

$$y = \frac{5}{3} - \frac{4}{5} = \left(\frac{13}{15} \right)$$



16.

If $x = \operatorname{cosec} A + \cos A$ and $y = \operatorname{cosec} A - \cos A$, then find the value of

$$\left(\frac{2}{x+y} \right)^2 + \left(\frac{x-y}{2} \right)^2 - 1.$$

SSC CHSL 19/10/2020 (Morning)

- (a) 3
(c) 2

- ~~(b) 0~~
(d) 1

$$\begin{aligned} & \left(\frac{2}{\frac{50}{15}} \right)^2 + \left(\frac{\frac{24}{15}}{2} \right)^2 - 1 \\ &= \left(\frac{3}{\frac{50}{25}} \right)^2 + \left(\frac{\frac{4}{12}}{\frac{15}{5}} \right)^2 - 1 \\ &= \frac{9}{25} + \frac{16}{25} - 1 \\ &= \frac{1}{25} = 0 \end{aligned}$$

16. If $x = \csc A + \cos A$ and $y = \csc A - \cos A$, then find the value of

$$\left(\frac{x}{\csc A}\right)^2 + \left(\frac{y}{\cos A}\right)^2 - 1$$

$$= (\sin A)^2 + (\cos A)^2 - 1$$

$$= 1 - 1 = 0$$

$$\left(\frac{2}{x+y}\right)^2 + \left(\frac{x-y}{2}\right)^2 - 1.$$

SSC CHSL 19/10/2020 (Morning)

- (a) 3
- (c) 2

- (b) 0
- (d) 1

$$\begin{aligned}x &= \csc A + \cos A \\y &= \csc A - \cos A\end{aligned}$$

$$A = 45^\circ$$

17. The value of $(\tan^2 A + \cot^2 A - 2) - \sec^2 A \cosec^2 A$ is :

- (a) - 4 (b) - 1
 (c) 1 (d) 4

CGL 2019 Tier-II (16/10/2020)

$$(1+1-2)-(2 \times 2)$$

$$\left(\frac{\frac{3}{5} + \frac{4}{5} - 1}{\frac{3}{5} - \frac{4}{5} + 1} \right) \times \sqrt{\frac{1 + \frac{3}{5}}{1 - \frac{3}{5}}}$$

18. The value of

$$= \left(\frac{\frac{7}{5} - 1}{-\frac{1}{5} + 1} \right) \times \sqrt{\frac{4}{\frac{4}{5} / \frac{3}{5}}} =$$

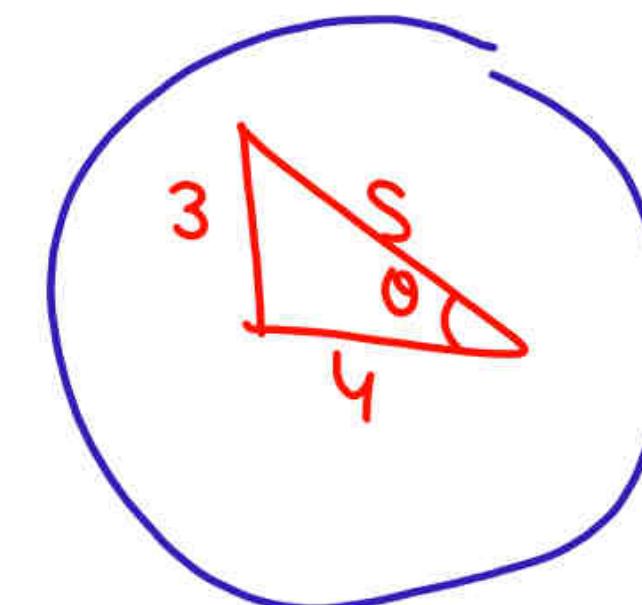
- (a) 1
(c) - 2

$$= \frac{2}{\frac{4}{5}} \times 2 = \frac{4}{\frac{4}{5}} = ①$$

$$\frac{\sin\theta + \cos\theta - 1}{\sin\theta - \cos\theta + 1} \times \sqrt{\frac{1 + \sin\theta}{1 - \sin\theta}}$$

CGL 2019 Tier-II (16/10/2020)

- (b) - 1
(d) 2



$$\frac{\frac{5}{4} \left(\frac{5}{4} + \frac{3}{4} \right) \times \left(1 - \frac{3}{5} \right)}{\left(\frac{4}{5} \right)^2}$$

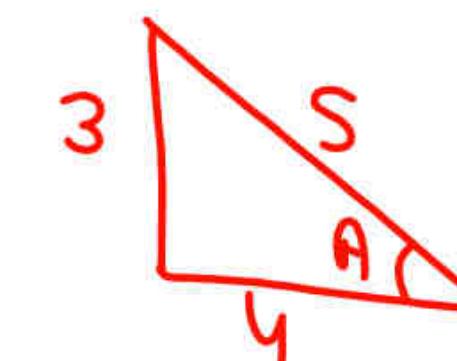
$$= \frac{\frac{5}{4} \times \frac{8}{4} \times \frac{2}{5}}{\frac{4}{5} \times \frac{4}{5}} = \frac{25}{16}$$

19.

$$\frac{\sec A (\sec A + \tan A)(1 - \sin A)}{(\csc^2 A - 1) \sin^2 A}$$

is equal to : **CGL 2019 Tier-II (16/10/2020)**

- (a) ~~$\sec^2 A$~~ = $\frac{25}{16}$
- (b) $\cos^2 A$
- (c) $\cot A$
- (d) $\cos A$



$$= 3(0-1)^4 + 6(0+1)^2 + 4(0+1)$$
$$= \boxed{3+6+4}$$

$$| \quad x=0 \quad s=0 \quad c=$$

$$= 3 + 2 + 0$$

21. The value of the following is : $3(\sin^4\theta + \cos^4\theta) + 2(\sin^6\theta + \cos^6\theta) + 12\sin^2\theta.\cos^2\theta$

$$\theta = 0^\circ \quad s = 0 \quad c = 1$$

$$\frac{x}{a} = \sin\theta + \omega \cos\theta$$

$$\Rightarrow \boxed{\frac{x}{a} = 1}$$

$$\frac{y}{b} = \sin\theta - \omega \cos\theta$$

$$\boxed{\frac{y}{b} = -1}$$

$$1^2 + (-1)^2 = 2$$

22. If $x = a(\sin\theta + \cos\theta)$, $y = b(\sin\theta - \cos\theta)$,

then the value of $\frac{x^2}{a^2} + \frac{y^2}{b^2}$ is :

- (a) 0
(c) 2

- (b) 1
(d) -2

$$\theta = 0^\circ \quad S = 0 \quad C = 1$$

$$\theta = \phi = 45^\circ$$

$$x = a \times \sqrt{2} \times \frac{1}{\sqrt{2}} \Rightarrow \frac{x}{a} = 1$$

$$y = b \times \sqrt{2} \times \frac{1}{\sqrt{2}} \Rightarrow \frac{y}{b} = 1$$

$$z = c + a \tan \theta \Rightarrow \frac{z}{c} = 1$$

23. If $x = a \sec \theta \cos \phi$, $y = b \sec \theta \sin \phi$,

$\text{then the value of } \frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} \text{ is :}$

SSC CHSL 15/10/2020 (Evening)

- (a) 1
- (c) 9

- (b) 4
- (d) 0

~~1 + / - /~~

$$(1 + \sin\alpha)(1 + \sin\beta)(1 + \sin\gamma) = R$$

$$(1 - \sin\alpha)(1 - \sin\beta)(1 - \sin\gamma) = R$$

$$(1 - \sin^2\alpha)(1 - \sin^2\beta)(1 - \sin^2\gamma) = R^2$$

$$\Rightarrow \cos^2\alpha \cdot \cos^2\beta \cdot \cos^2\gamma = R^2$$

$$\Rightarrow \boxed{\pm \cos\alpha \cos\beta \cos\gamma = R}$$

$\alpha = \beta = \gamma = 0$

24. If $(1 + \sin\alpha)(1 + \sin\beta)(1 + \sin\gamma) = (1 - \sin\alpha)(1 - \sin\beta)(1 - \sin\gamma)$, then each side is equal to :

- (a) $\pm \cos\alpha \cdot \cos\beta \cdot \cos\gamma$
- (b) $\pm \sin\alpha \cdot \sin\beta \cdot \sin\gamma$
- (c) $\pm \sin\alpha \cdot \cos\beta \cdot \cos\gamma$.
- (d) $\pm \sin\alpha \cdot \sin\beta \cdot \cos\gamma$

$$\theta = 45^\circ$$

$$x = \sqrt{2} - \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$

$$y = \sqrt{2} - \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$

$$x = \sqrt{2} - \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$

25. If $\csc\theta - \sin\theta = x$ and $\sec\theta - \cos\theta = y$, then

$$x^{\frac{2}{3}}y^{\frac{2}{3}} \left(x^{\frac{2}{3}} + y^{\frac{2}{3}} \right) = ?$$

- (a) 0
(c) -1

- ~~(b) 1~~
(d) 2

$$\begin{aligned} x^{\frac{4}{3}} \cdot 2 \cdot x^{\frac{2}{3}} &= 2 \cdot x^{\frac{4}{3} + \frac{2}{3}} \\ &= 2 \cdot x^{\frac{6}{3}} \\ &= 2 \cdot x^2 = 2 \times \frac{1}{2} \end{aligned}$$

$$\theta = 0^\circ$$

$$x = 0+0 = 0$$

$$y = 1+1 = 2$$

$$(x^2 + y^2)(x^2 + y^2 - 3)$$

$$= (0+4)(0+4-3)$$

$$= 4 \times 1 = 4$$

26. If $\sin\theta + \sin 2\theta = x$ and $\cos\theta + \cos 2\theta = y$,

then $(x^2 + y^2)(x^2 + y^2 - 3) = ?$

(a) $2y = 4$

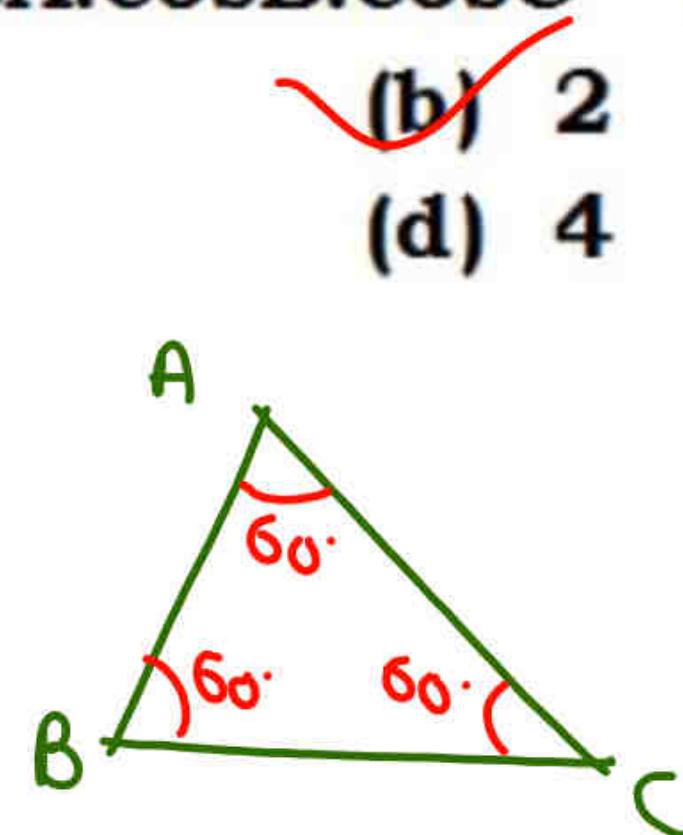
(b) $3y = 6$

(c) $-2y = -4$

(d) $4y = 8$

$$\begin{aligned}
 & \text{Given: } \sin^2 A + \sin^2 B + \sin^2 C - 2\cos A \cos B \cos C \\
 &= 3 \sin^2 A - 2 \cos^3 A \\
 &= 3 \times \frac{3}{4} - 2 \times \frac{1}{8} \\
 &= \frac{8}{4} = 2
 \end{aligned}$$

27. If A, B, C are the angles of a triangle, then the value of expression $\sin^2 A + \sin^2 B + \sin^2 C - 2\cos A \cos B \cos C = ?$
- (a) 1 (b) 2 (c) 3 (d) 4

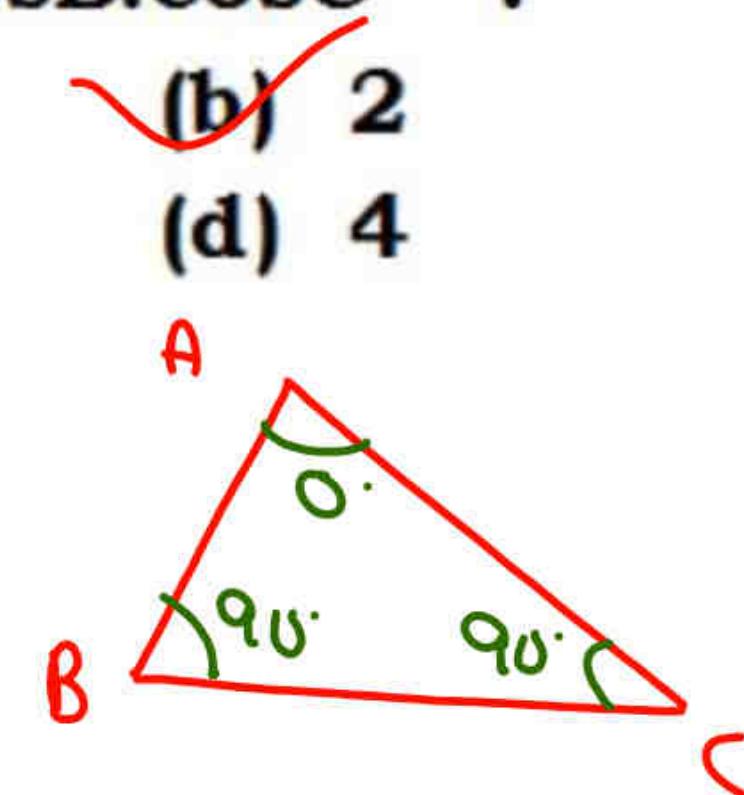


$$\begin{aligned} & \sin^2 A + \sin^2 B + \sin^2 C - \\ & 2\cos A \cos B \cdot \cos C \end{aligned}$$

$$\begin{aligned} &= 0 + 1 + 1 - 2 \times 1 \times 0 \times 0 \\ &= 2 - 0 \end{aligned}$$

27. If A, B, C are the angles of a triangle, then the value of expression $\sin^2 A + \sin^2 B + \sin^2 C - 2\cos A \cos B \cos C = ?$

- (a) 1
- (b) 2
- (c) 3
- (d) 4



$$\chi = 0^\circ$$

$$= 1+1+1+1$$

$$= \textcircled{4}$$

28. $1 + \cos 2x + \cos 4x + \cos 6x = ?$

- (a) $2\cos x \cdot \cos 2x \cdot \cos 3x$
- (b) $4\sin x \cdot \cos 2x \cdot \cos 3x$
- (c) $4\cos x \cdot \cos 2x \cdot \cos 3x$
- (d) $\cos x \cdot \cos 2x \cdot \cos 3x$

$$A = B = C = D = 0^\circ$$

29. What is the value of $\sin(B - C) \cos(A - D)$
+ $\sin(A - B) \cos(C - D)$ + $\sin(C - A) \cos(B - D)$?

- (a) $\frac{3}{2}$ (b) - 3
(c) 1 (d) 0

$$= \cancel{\sin(B-C)} \cdot \cancel{\cos(A-D)} + \cancel{\sin(A-B)} \cos(C-D) + \sin(C-A) \cdot \cos(B-D)$$

$$= 0 + 0 + 0$$

30. If $P + Q + R = 60^\circ$, then what is the value of $\cos Q \cdot \cos R (\cos P - \sin P) + \sin Q \cdot \sin R (\sin P - \cos P)$

(a) $\frac{1}{2}$

(b) $\frac{\sqrt{3}}{2}$

(c) $\frac{1}{\sqrt{2}}$

(d) $\sqrt{2}$

$$\begin{aligned}
 &= \frac{1}{2} \times 1 \left(1 - 0\right) + \frac{\sqrt{3}}{2} \times 0 \times \\
 &\quad \left(\frac{1}{2} + 0\right)
 \end{aligned}$$

$$X = Y = Z = 45^\circ$$

$$\frac{\sin 0 + \sin 90 + 2\sin 45}{\sin 0 + \sin 90 + 2\sin 45} = 1$$

31. What is the value of

$$\frac{[\sin(y - z) + \sin(y + z) + 2\sin y]}{[\sin(x - z) + \sin(x + z) + 2\sin x]}.$$

$$\frac{1}{2} (a) \cos x \cdot \sin y$$

$$\frac{1}{\sqrt{2}} (c) \sin z$$

$$(b) \frac{\sin y}{\sin x}$$

$$\frac{1}{\sqrt{2}} (d) \sin x \cdot \tan y$$

Note:- $(1+\tan\theta)$ or $(1+\cot\theta)$

Take $\rightarrow \theta = 135^\circ$

$$\tan 135^\circ = \cot 135^\circ = -1$$

$$\sin 135^\circ = \frac{1}{\sqrt{2}}$$

$$\cos 135^\circ = -\frac{1}{\sqrt{2}}$$

32. If $\frac{\tan\theta}{1-\cot\theta} + \frac{\cot\theta}{1-\tan\theta} = 1+k$, then $k = ?$

SSC CGL 7 June 2019 (Evening)

(a) $\cot\theta + \sec\theta$

(c) $\tan\theta + \sec\theta$

(b) $\tan\theta \cdot \cosec\theta$

(d) $\cosec\theta \cdot \sec\theta$

$$\sqrt{2} \cdot (-\sqrt{2}) = -2$$

$$\begin{aligned} &\Rightarrow \frac{-1}{1-(-1)} + \frac{-1}{1-(-1)} = 1+k \\ &\Rightarrow \frac{-1}{2} - \frac{1}{2} = 1+k \\ &\Rightarrow -1 = 1+k \\ &\Rightarrow -2 = k \end{aligned}$$

$$A=0^\circ \Rightarrow S=0, C=1$$

$$\theta = \frac{\alpha}{2}$$

33.

$$\frac{(2\sin A)(1 + \sin A)}{1 + \sin A + \cos A} \text{ is equal to :}$$

SSC CGL Tier-II (11 September 2019)

- (a) $\frac{1 + \theta - 1}{1 + \sin A - \cos A}$ (b) $1 - \sin A \cos A$
 (c) $1 + \cos A - \sin A$ (d) $1 + \sin A \cos A$
- $1 + 1 - \theta$

$$\phi = 45^\circ$$

34. The value of $\tan^2\phi + \cot^2\phi - \sec^2\phi \cdot \cosec^2\phi$
is equal to : $1 + 1 - 2 \times 2 = -2$

SSC CGL Tier-II (12 September 2019)

- (a) - 2
- (b) 1
- (c) 0
- (d) - 1

$\theta = 45^\circ$

$$\begin{aligned}1+1-(2+2) \\= 2-4 = -2\end{aligned}$$

35. The value of

1
$$\frac{\sec^2 \theta}{\csc^2 \theta} + \frac{1}{\sec^2 \theta} - (\sec^2 \theta + \csc^2 \theta)$$
 is :

SSC CGL Tier-II (13 September 2019)

- (a) 0
- (b) -2
- (c) 2
- (d) 1

$\theta = 0^\circ$

$$\begin{array}{l} S=0 \\ C=1 \end{array}$$

36. The value of

$$\frac{2(\sin^6\theta + \cos^6\theta) - 3(\sin^4\theta + \cos^4\theta)}{\cos^4\theta - \sin^4\theta - 2\cos^2\theta} \text{ is :}$$

SSC CGL Tier-II (13 September 2019)

- (a) - 1
 (c) 2

- (b) - 2
 (d) 1

$$= \frac{2(0+1) - 3(0+1)}{1-0-2 \times 1}$$

$$\therefore \frac{-1}{-1} = \cancel{\frac{-1}{-1}} = 0$$

$$\theta = 45^\circ$$

37. The expression $\underline{3\sec^2\theta \cdot \tan^2\theta + \tan^6\theta - \sec^6\theta}$
is equal to :

SSC CGL 4 March 2020 (Afternoon)

- (a) - 2
- (c) 2

- (b) 1
- (d) \checkmark - 1

$$\begin{aligned} (\sqrt{2})^6 &= \\ &= 2^{\frac{1}{2} \times 6} \\ &= 2^3 \\ &= 8 \end{aligned}$$

$$\begin{aligned} 3 \times 2 \times 1 + 1 - (\sqrt{2})^6 &= \\ &= 7 - 8 \\ &= -1 \end{aligned}$$

$$\theta = 45^\circ$$

$$= \frac{(\sqrt{2})^6 - 1 - 3 \times 2 \times 1 + 1}{\cancel{2} \times \frac{1}{\cancel{2}} + 2}$$

$$= \frac{\cancel{8} - \cancel{6} + \cancel{1}}{3} = \frac{2}{3}$$

38.

The value of

$$\frac{\sec^6 \theta - \tan^6 \theta - 3 \sec^2 \theta \tan^2 \theta + 1}{\cos^4 \theta - \sin^4 \theta + 2 \sin^2 \theta + 2} \text{ is :}$$

SSC CGL 5 March 2020 (Morning)

- (a) $\frac{2}{3}$
- (b) 1
- (c) $\frac{3}{4}$
- (d) $\frac{1}{2}$

$$\begin{aligned} A &= 0^\circ \\ \cos 0^\circ &= 1 \\ \sec 0^\circ &= 1 \end{aligned}$$

39. The value of $4 \left[\frac{(1 - \sec A)^2 + (1 + \sec A)^2}{1 + \sec^2 A} \right]$ is :

SSC CGL 6 March 2020 (Evening)

- (a) 2
- (b) 4
- (c) 8
- (d) 1

$$\begin{aligned} &= 4 \left[\frac{(1-1)^2 + (1+1)^2}{1+1} \right] \\ &= \frac{4 \times 4}{2} \end{aligned}$$

40.

Repeat
of Q.

If $x = \csc A + \cos A$ and $y = \csc A - \cos A$, then find the value of

$$\left(\frac{2}{x+y}\right)^2 + \left(\frac{x-y}{2}\right)^2 - 1.$$

SSC CHSL 19/10/2020 (Morning)

A=45°

41. The value of $(\tan^2 A + \cot^2 A - 2) - \sec^2 A$ cosec²A is :

SSC CGL 2019, Tier-II (16/10/2020)

- (a) - 4
- (b) - 1
- (c) 1
- (d) 4

$$(1+1-2) - 2 \times 2$$

$$0 - 4$$

$$\theta = 45^\circ$$

$H \cdot w$

42.

If $(\sin \theta + \operatorname{cosec} \theta)^2 + (\cos \theta + \sec \theta)^2 = k + \tan^2 \theta + \cot^2 \theta$, then the value of k is equal to :

SSC CGL 2019, Tier-II (18/10/2020)