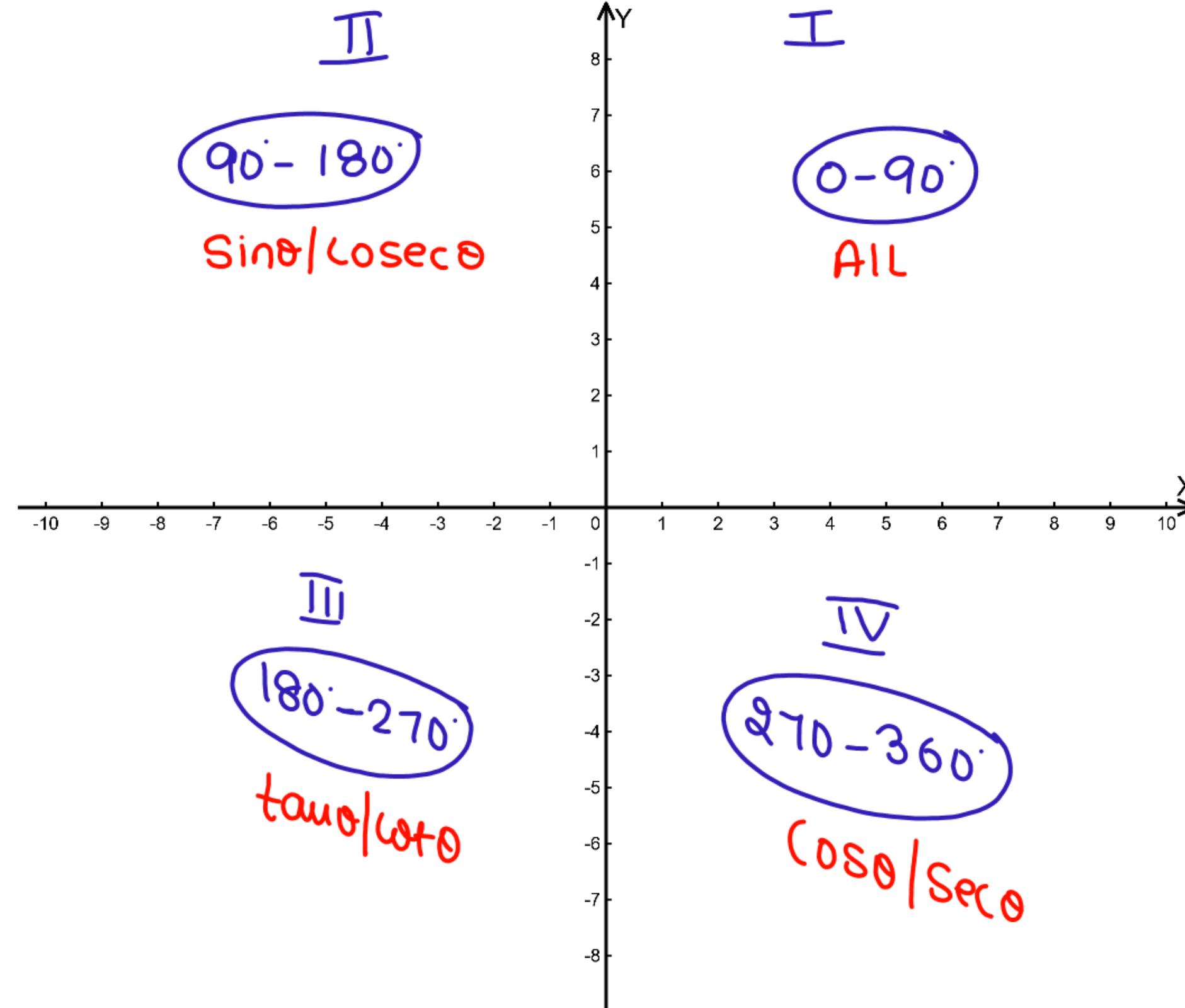


TRIGONOMETRY

SHEET 03

**Basic Questions Based on Values of Trigonometric
Ratio in Different Quadrants**

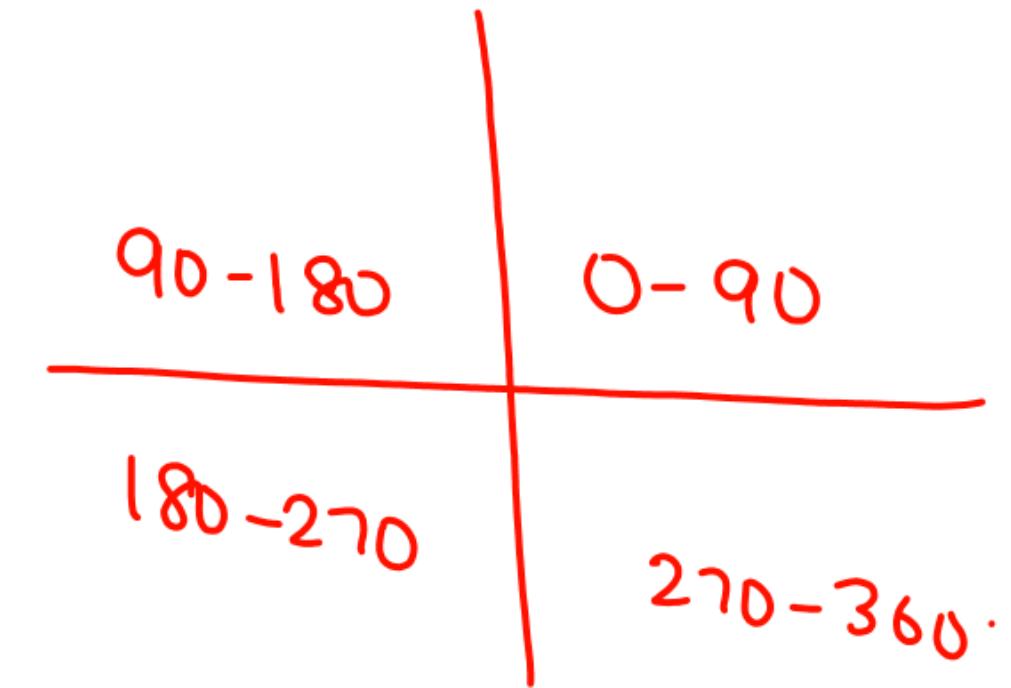


Trick:-

Add sugar +
coffee.

Quadrants

- change $(90 - \theta) \rightarrow I$
 $(90 + \theta) \rightarrow II$
 $(180 - \theta) \rightarrow II$
 $(180 + \theta) \rightarrow III$
change $(270 - \theta) \rightarrow III$
 $(270 + \theta) \rightarrow IV$
 $(360 - \theta) \rightarrow IV$
 $(360 + \theta) \rightarrow I$.



Note:- 90° के odd multiple पर

$$\sin \theta \iff \cos \theta$$

$$\csc \theta \iff \sec \theta$$

$$\tan \theta \iff \cot \theta$$

$$\begin{aligned} 90 \times 1 &= 90^\circ \rightarrow \checkmark \\ 90 \times 2 &= 180^\circ \times \\ 90 \times 3 &= 270^\circ \checkmark \\ &\downarrow \quad \downarrow \\ &\text{odd} \quad \text{odd} \end{aligned}$$

(-θ)

* $\sin(-\theta) = -\sin\theta$

* $\cos(-\theta) = \cos\theta$

* $\tan(-\theta) = -\tan\theta$

* $\operatorname{cosec}(-\theta) = -\operatorname{cosec}\theta$

* $\sec(-\theta) = \sec\theta$

* $\cot(-\theta) = -\cot\theta$

for $(90-\theta)$

* $\sin(90-\theta) = \cos\theta$

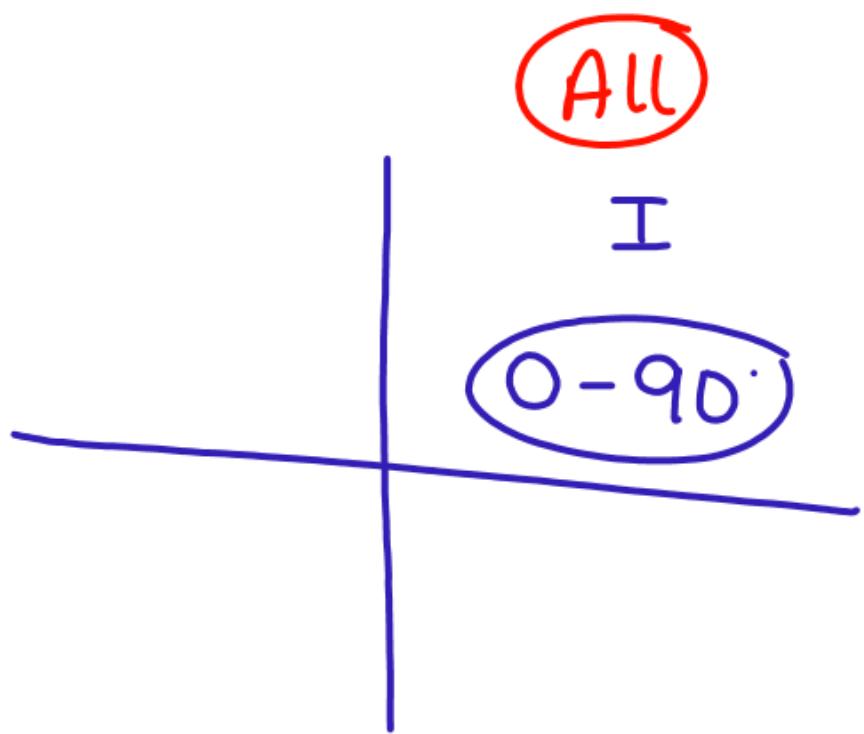
* $\cos(90-\theta) = \sin\theta$

* $\tan(90-\theta) = \cot\theta$

* $\operatorname{cosec}(90-\theta) = \sec\theta$

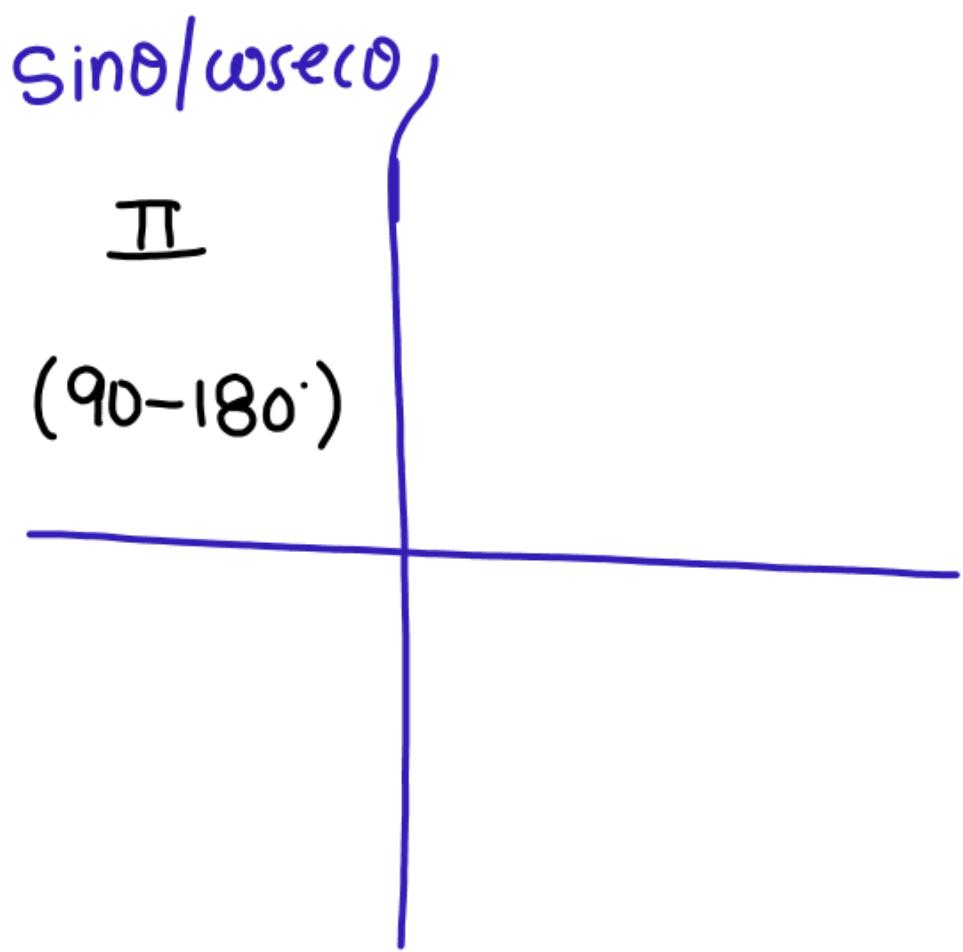
* $\sec(90-\theta) = \operatorname{cosec}\theta$

* $\cot(90-\theta) = \tan\theta$



for $(90 + \theta)$

- * $\sin(90 + \theta) = \cos \theta$
- * $\cos(90 + \theta) = -\sin \theta$
- * $\tan(90 + \theta) = -\cot \theta$
- * $\operatorname{cosec}(90 + \theta) = \sec \theta$
- * $\sec(90 + \theta) = -\operatorname{cosec} \theta$
- * $\cot(90 + \theta) = -\tan \theta$



For $(180 - \theta)$

* $\sin(180 - \theta) = \sin\theta$

* $\cos(180 - \theta) = -\cos\theta$

* $\tan(180 - \theta) = -\tan\theta$

* $\csc(180 - \theta) = \csc\theta$

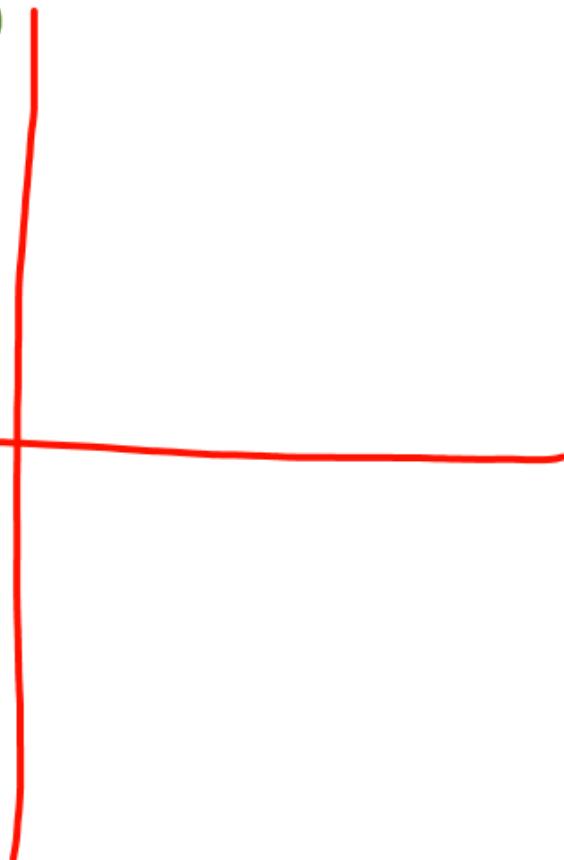
* $\sec(180 - \theta) = -\sec\theta$

* $\cot(180 - \theta) = -\cot\theta$

$\sin\theta / \csc\theta$

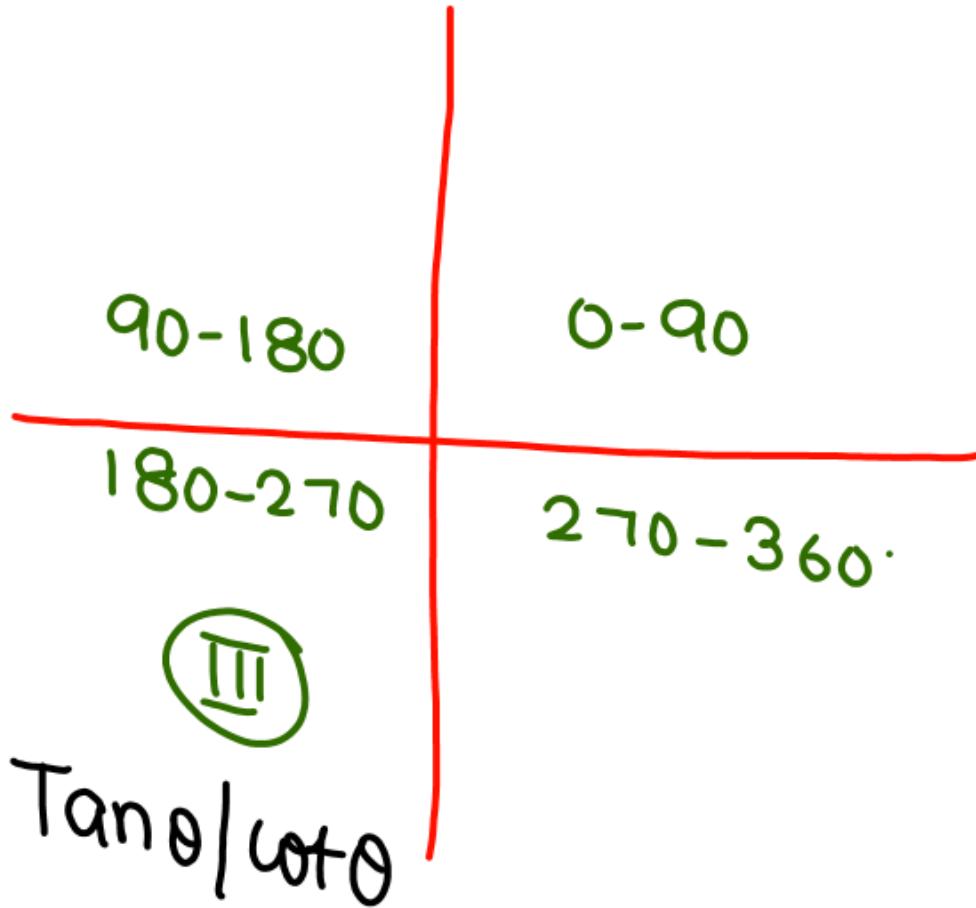
II

$(90 - 180^\circ)$



For $(180 + \theta)$

- * $\sin(180 + \theta) = -\sin\theta$
- * $\cos(180 + \theta) = -\cos\theta$
- * $\tan(180 + \theta) = \tan\theta$
- * $\operatorname{cosec}(180 + \theta) = -\operatorname{cosec}\theta$
- * $\sec(180 + \theta) = -\sec\theta$
- * $\cot(180 + \theta) = \cot\theta$



For $(270 - \theta)$

* $\sin(270 - \theta) = - \cos \theta$

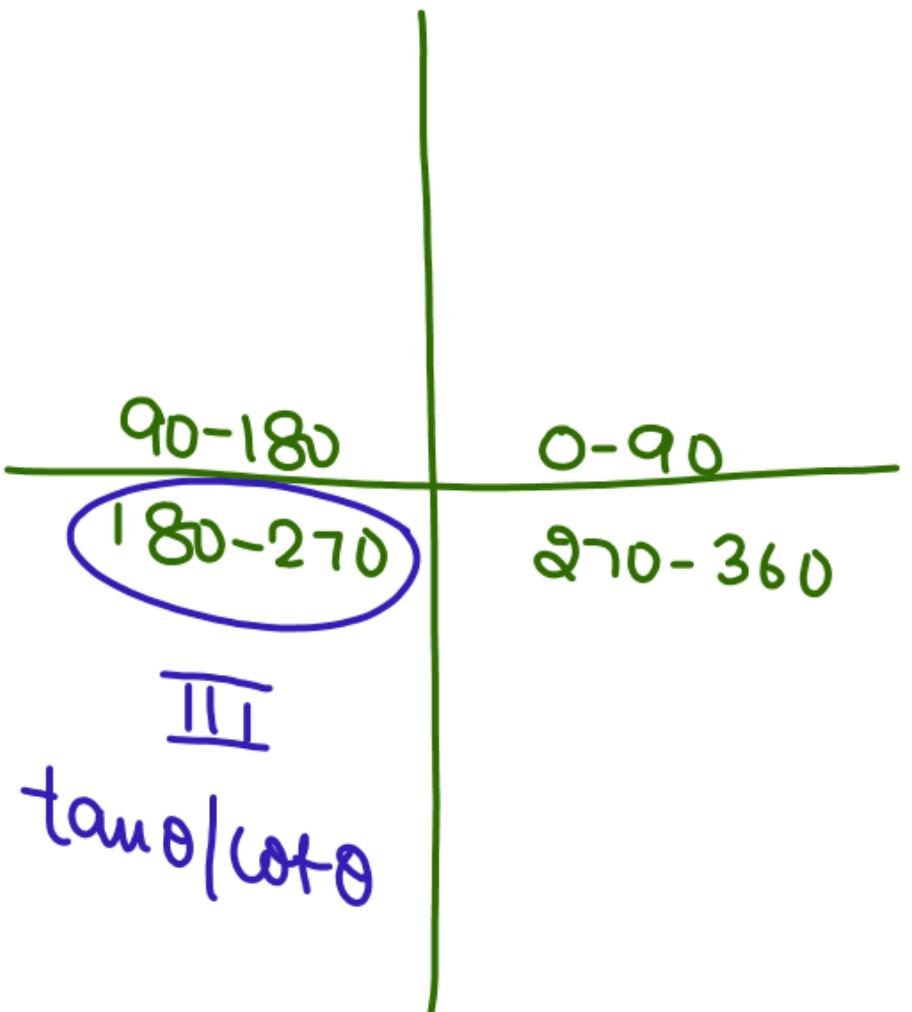
* $\cos(270 - \theta) = - \sin \theta$

* $\tan(270 - \theta) = \cot \theta$

* $\operatorname{cosec}(270 - \theta) = - \sec \theta$

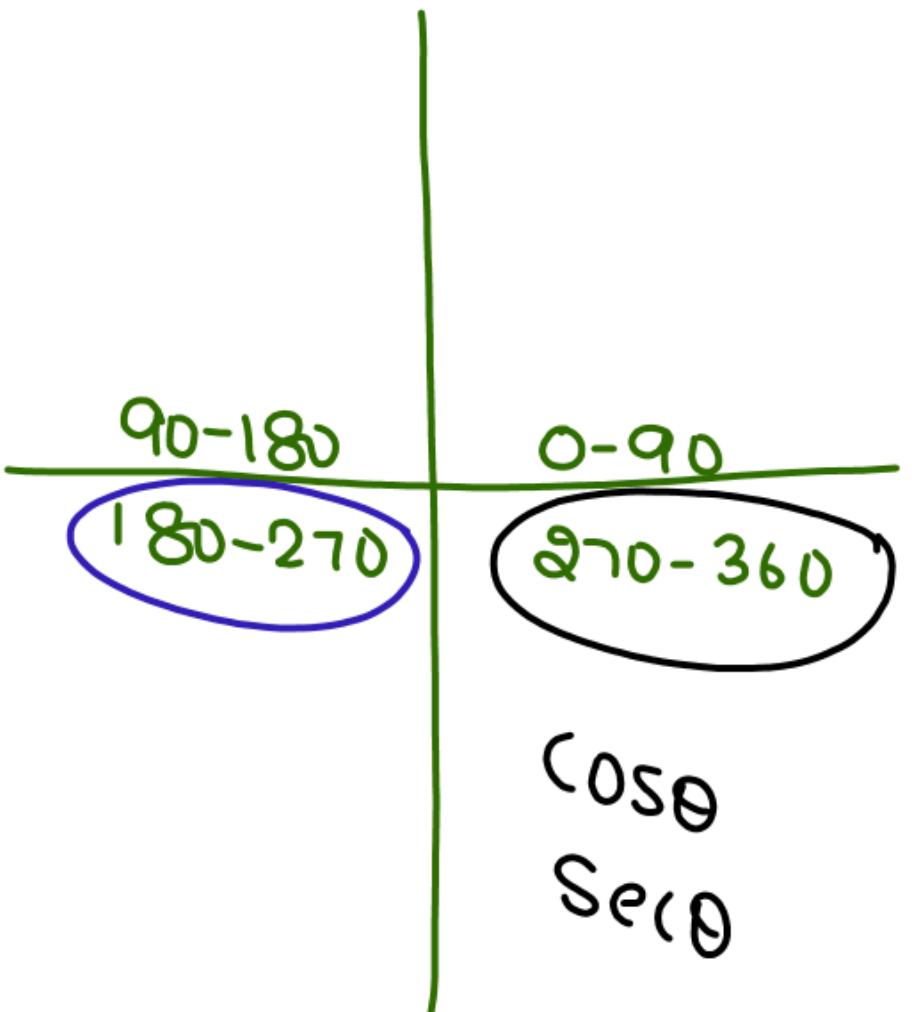
* $\sec(270 - \theta) = - \operatorname{cosec} \theta$

* $\cot(270 - \theta) = \frac{\operatorname{cosec} \theta}{\tan \theta}$



For $(270 + \theta)$

- * $\sin(270 + \theta) = -\cos\theta$
- * $\cos(270 + \theta) = \sin\theta$
- * $\tan(270 + \theta) = -\cot\theta$
- * $\operatorname{cosec}(270 + \theta) = -\sec\theta$
- * $\sec(270 + \theta) = \operatorname{cosec}\theta$
- * $\cot(270 + \theta) = -\tan\theta$



for $(360 - \theta)$

$$* \sin(360 - \theta) = -\sin\theta$$

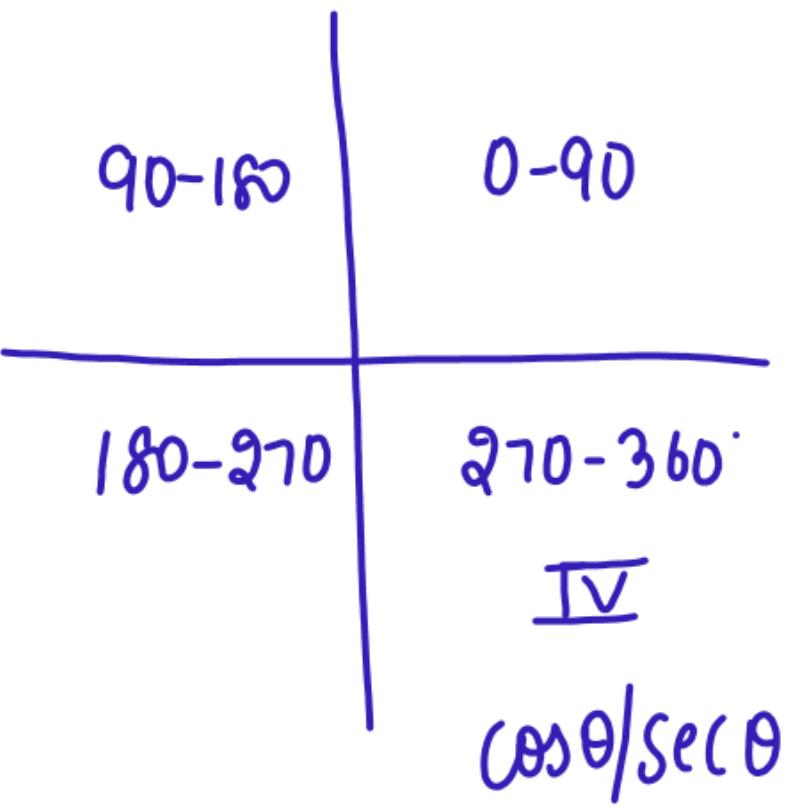
$$\cancel{*} \cos(360 - \theta) = \cos\theta$$

$$* \tan(360 - \theta) = -\tan\theta$$

$$* \csc(360 - \theta) = -\csc\theta$$

$$\cancel{*} \sec(360 - \theta) = \sec\theta$$

$$* \cot(360 - \theta) = -\cot\theta$$



for $(360+\theta)$

$0 \leq 90^\circ$

* $\sin(360+\theta) = \sin\theta$

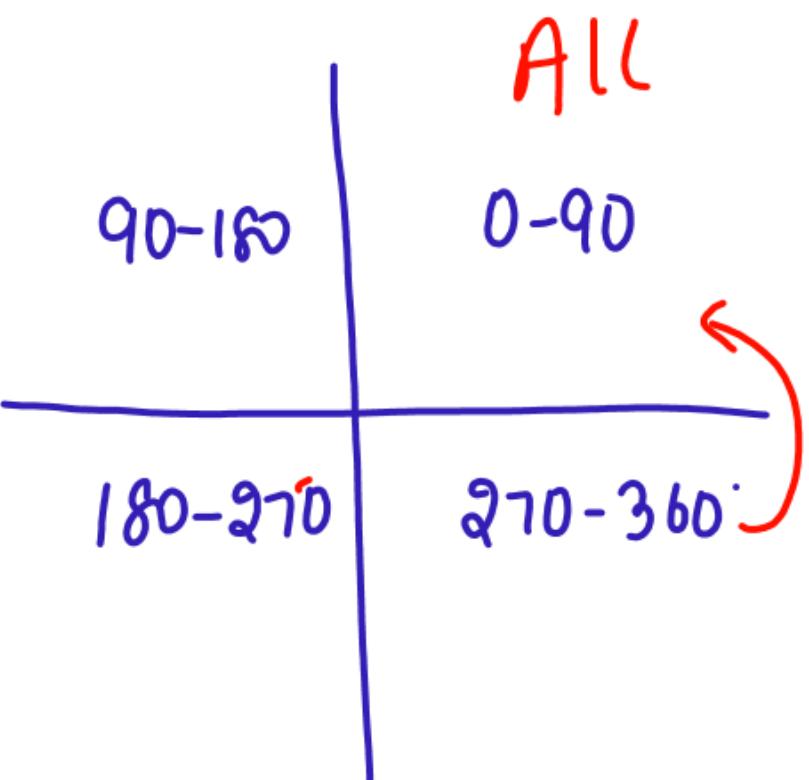
* $\cos(360+\theta) = \cos\theta$

* $\tan(360+\theta) = \tan\theta$

* $\csc(360+\theta) = \csc\theta$

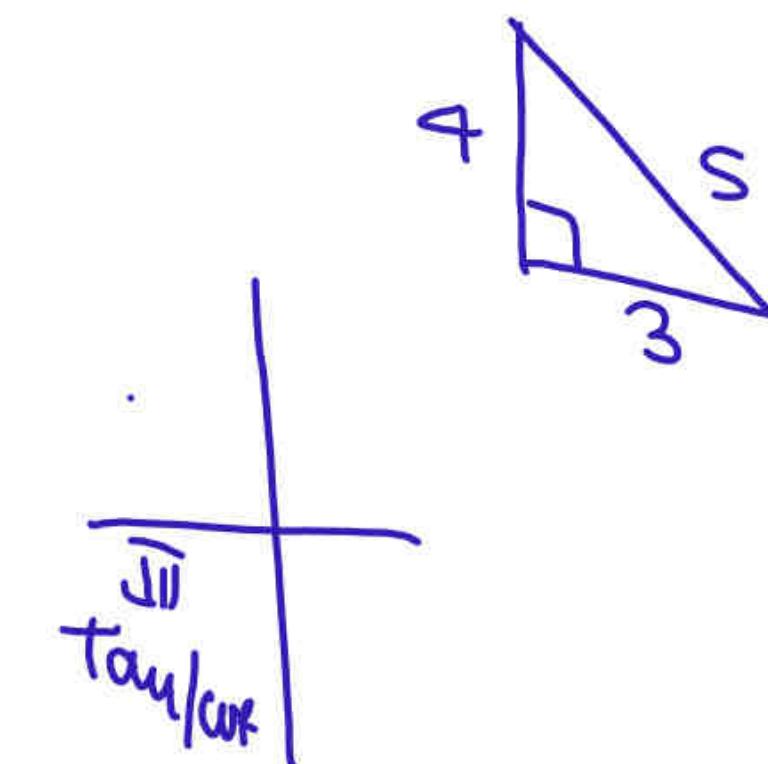
* $\sec(360+\theta) = \sec\theta$

* $\cot(360+\theta) = \cot\theta$



$$\begin{aligned}\sin x &= -\frac{4}{5} \\ \checkmark \tan x &= \frac{4}{3} \\ \cosec x &= -\frac{5}{4} \\ \sec x &= -\frac{5}{3} \\ \checkmark \cot x &= \frac{3}{4}\end{aligned}$$

1. If $\cos x = -\frac{3}{5}$, x lies in the third quadrant, find the values of other five trigonometric functions.



$$\sin \theta = \frac{12}{13}$$

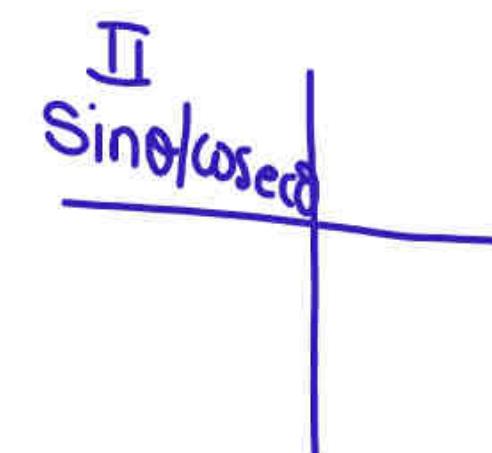
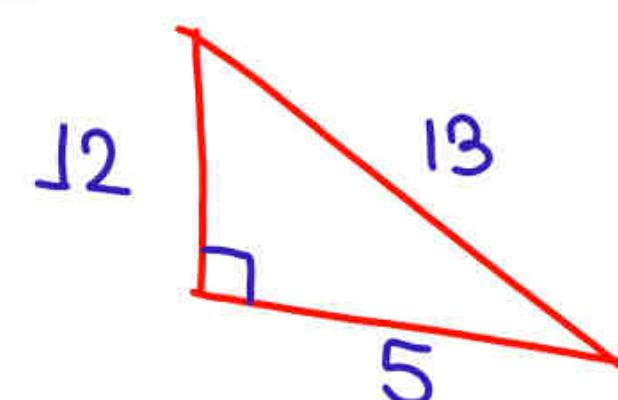
$$\operatorname{cosec} \theta = \frac{13}{12}$$

$$\sec \theta = -\frac{13}{5}$$

$$\tan \theta = -\frac{12}{5}$$

$$\cot \theta = -\frac{5}{12}$$

2. If $\cos x = -\frac{5}{13}$, x lies in the second quadrant, find the values of other five trigonometric functions.



* $\sin 210^\circ$

$$= \sin(180 + 30^\circ)$$

$$= -\sin 30^\circ$$

$$= -\frac{1}{2}$$

or

$\sin 210^\circ$

$$= \sin(270^\circ - 60^\circ)$$

$$= -\cos 60^\circ$$

$$= -\frac{1}{2}$$

* $\sin 150^\circ$

$$= \sin(90 + 60^\circ)$$

$$= \cos 60^\circ$$

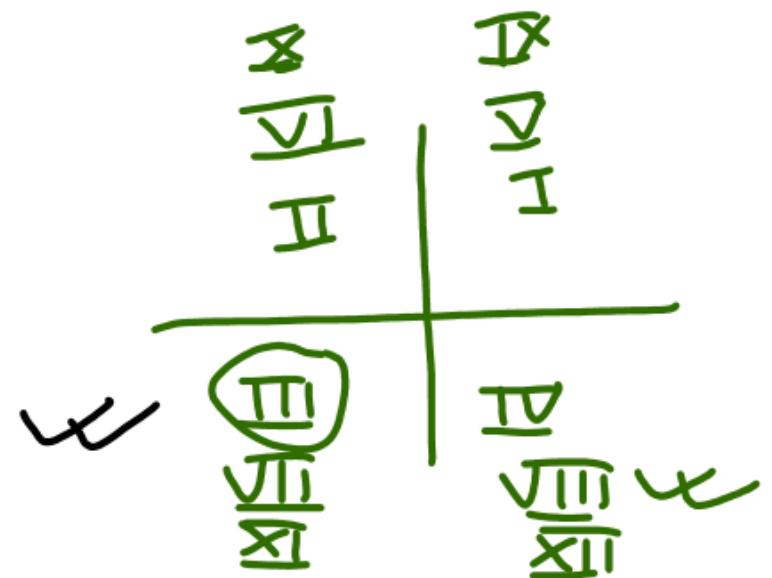
$$= \frac{1}{2}$$

* $\sin 390^\circ$

$$= \sin(360 + 30^\circ)$$

$$= \sin 30^\circ$$

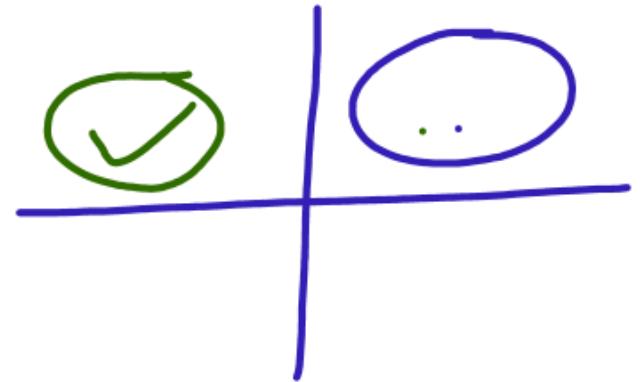
$$= \frac{1}{2}$$



- * $\sin 100^\circ = +\cos 10^\circ$
- * $\sin 190^\circ = -\sin 10^\circ$
- * $\sin 200^\circ = -\sin 20^\circ$
- * $\sin 280^\circ = -\cos 10^\circ$
- * $\sin 390^\circ = +\sin 30^\circ$
- * $\sin 570^\circ = -\sin 30^\circ$
- * $\sin 680^\circ = -\cos 50^\circ$
- * $\sin 930^\circ = -\sin 30^\circ$

$$\begin{aligned}
 \text{II} &\leftarrow 100^\circ = 90 \times 1 + 10^\circ \\
 \text{III} &\leftarrow 190^\circ = 90 \times 2 + 10^\circ \\
 \text{III} &\leftarrow 200^\circ = 90 \times 2 + 20^\circ \\
 \text{IV} &\leftarrow 280^\circ = 90 \times 3 + 10^\circ \\
 \text{V} &\leftarrow 390^\circ = 90 \times 4 + 30^\circ \\
 \text{VI} &\leftarrow 570^\circ = 90 \times 6 + 30^\circ \\
 \text{VII} &\leftarrow 680^\circ = 90 \times 7 + 50^\circ \\
 \text{VIII} &\leftarrow 930^\circ = 90 \times 10 + 30^\circ
 \end{aligned}$$

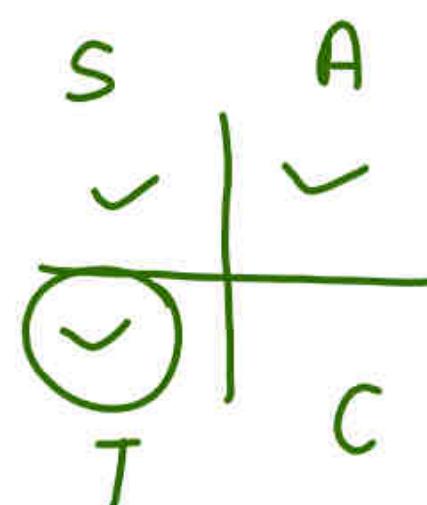
$$\sin(1450^\circ) = \sin 10^\circ$$



* $\tan(1540^\circ) = -\cot 10^\circ$

$$1450 = 90 \times 16 + 10^\circ$$

$$18 < 1540 = 90 \times 17 + 10^\circ$$



3. The value of $\sin 960^\circ \cos 330^\circ + \cos 120^\circ \sin 150^\circ$ is :

(a) -1

(b) 1

(c) $\frac{1}{\sqrt{2}}$

(d) $\frac{\sqrt{3}}{2}$

$$\begin{aligned}
 &= \sin 960^\circ \cdot \cos 330^\circ + \cos 120^\circ \cdot \sin 150^\circ \\
 &= \sin(90 \times 10 + 60^\circ) \cdot \cos(90 \times 3 + 60^\circ) + \cos(90 \times 1 + 30^\circ) \cdot \sin(90 \times 1 + 60^\circ) \\
 &= -\sin 60^\circ \cdot \sin 60^\circ - \sin 30^\circ \cos 60^\circ \\
 &= -\frac{\sqrt{3}}{2} \cdot \frac{\sqrt{3}}{2} - \frac{1}{2} \cdot \frac{1}{2} \\
 &= -\frac{3}{4} - \frac{1}{4} = -\frac{4}{4} = -1
 \end{aligned}$$

$$\begin{aligned}& \sin \frac{31\pi}{3} \\&= \sin \frac{31 \times 180}{3}^{\circ} \\&= \boxed{\sin 1860^{\circ}} \\&= \sin (90 \times 20 + 60^{\circ}) \\&= + \sin 60^{\circ} \\&= \frac{\sqrt{3}}{2}\end{aligned}$$

4.

Find the value of $\sin \frac{31\pi}{3}$.

(a) 1

(b) $\frac{1}{2}$ (c) $\frac{\sqrt{3}}{2}$

(d) 0

$$\begin{aligned}&= \cos 110^\circ \\&= \cos(90^\circ + 19^\circ) \\&= -\sin 19^\circ \\&= 0\end{aligned}$$

5.

Find the value of $\cos (-1710^\circ)$.

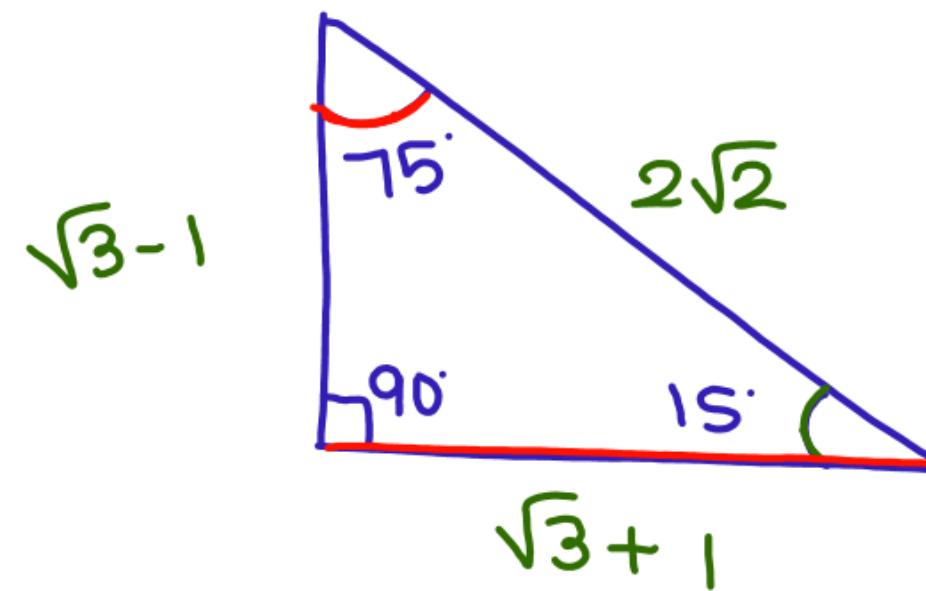
(a) 0

(b) 1

(c) -1

(d) $\frac{1}{2}$

Value of 15° & 75°



$$\sin 15^\circ = \frac{\sqrt{3}-1}{2\sqrt{2}}$$

$$\cos 15^\circ = \frac{\sqrt{3}+1}{2\sqrt{2}}$$

$$\sin 75^\circ = \frac{P}{H} = \frac{\sqrt{3}+1}{2\sqrt{2}}$$

$$= \tan \frac{13 \times 180}{12}^{\circ}$$

$$= \tan 195^{\circ}$$

$$= \tan (90 \times 2 + 15^{\circ})$$

$$= \tan 15^{\circ}$$

$$= \frac{\sqrt{3}-1}{\sqrt{3}+1} \times \frac{\sqrt{3}-1}{\sqrt{3}-1} = \frac{(\sqrt{3}-1)^2}{(\sqrt{3})^2 - (1)^2}$$

$$= \frac{4-2\sqrt{3}}{2} = 2-\sqrt{3}$$

6.

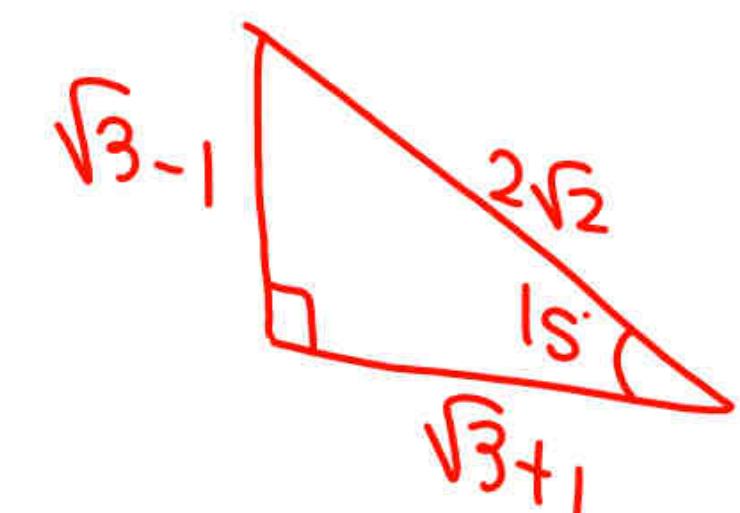
Solve $\tan \frac{13\pi}{12}$.

(a) $2 + \sqrt{3}$

(c) $\sqrt{3}$

(b) $2 - \sqrt{3}$

(d) $\sqrt{3} + 1$



$$\sin(90 + 60^\circ)$$

7.

$$\text{Find } 3\sin \frac{\pi}{6} \sec^2 \frac{\pi}{3} - 4\sin \frac{5\pi}{6} \cot \frac{\pi}{4}$$

- (a) 4 (b) 0
 (c) -1 (d) 2

$$\begin{aligned}
 &= 3 \sin 30^\circ \cdot \sec^2 60^\circ - 4 \sin 180^\circ \cdot \cot 45^\circ \\
 &= 3 \times \frac{1}{2} \cdot 4^2 - 4 \times \frac{1}{2} \cdot 1 \\
 &= 6 - 2 = 4
 \end{aligned}$$

$$\begin{aligned}\sin^2 60^\circ + \cos^2 45^\circ \\= \frac{3}{4} + \frac{1}{2} \\= \frac{10}{8} = \frac{5}{4}\end{aligned}$$

8.

Find $\sin^2 \frac{\pi}{3} + \cos^2 \frac{\pi}{4} = ?$

- (a) $\frac{1}{2}$
(c) 1

(b) $\frac{5}{4}$

(d) -1

$$\begin{aligned} & \sin(90+45^\circ) \\ &= \cos 45^\circ \end{aligned}$$

9. Find $2\sin^2 \frac{3\pi}{4} + 2\cos^2 \frac{\pi}{4} + 2\cos^2 \frac{\pi}{3} = ?$

(a) 4

(c) $\frac{5}{2}$

(b) 5

(d) 6

$$\begin{aligned} &= 2 \times \sin^2 135^\circ + 2 \cos^2 45^\circ + 2 \cos^2 60^\circ \\ &= 2 \times \left(\frac{1}{\sqrt{2}}\right)^2 + 2 \times \left(\frac{1}{\sqrt{2}}\right)^2 + 2 \times \left(\frac{1}{2}\right)^2 \\ &= 2 \times \frac{1}{2} + 2 \times \frac{1}{2} + 2 \times \frac{1}{4} \\ &= 1 + 1 + \frac{1}{2} = 2 + \frac{1}{2} = \frac{5}{2} \end{aligned}$$

10.

H.W

Find $2\sin^2 \frac{\pi}{6} + \operatorname{cosec}^2 \frac{7\pi}{6} \cos^2 \frac{\pi}{3} = ?$

(a) 1

(b) $\frac{1}{2}$

(c) $-\frac{1}{2}$

(d) $\frac{3}{2}$

11.

H.W

Find $\cot^2 \frac{\pi}{6} + \operatorname{cosec}^2 \frac{5\pi}{6} + 3\tan^2 \frac{\pi}{6}$ = ?

- (a) 6
(c) 5

- (b) 4
(d) 3

$$= \frac{-\cos x \times \cos x}{\sin x (-\sin x)}$$

$$= \frac{\cos^2 x}{\sin^2 x} = \cot^2 x$$

12.

Find $\frac{\cos(\pi + x)\cos(-x)}{\sin(\pi - x)\cos\left(\frac{\pi}{2} + x\right)} = ?$

- (a) $\sin^2 x$
 (c) $-\cot^2 x$

- (b) $\tan^2 x$
 (d) $\cot^2 x$

$$\begin{aligned}\cos(180 + \theta) &= \cos(90 \times 2 + \theta) \\ &= -\cos \theta\end{aligned}$$

at

13. $\sin 15^\circ + \cos 105^\circ =$

- (a) 0 (b) $2 \sin 15^\circ$
(c) $\cos 15^\circ + \sin 15^\circ$ (d) $2 \cos 15^\circ$

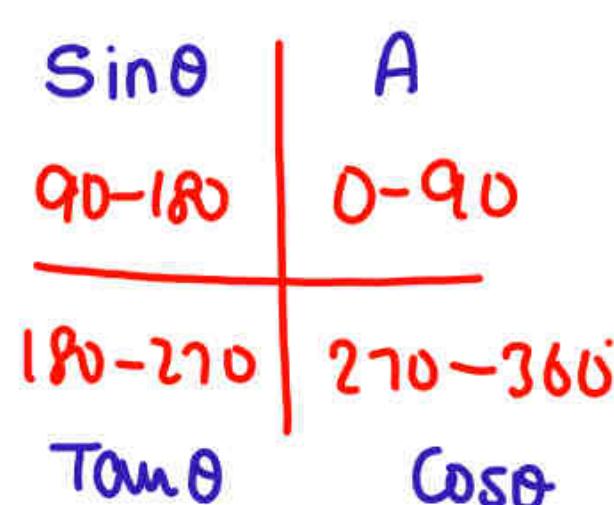
$$= \sin 15^\circ + \cos(90 + 15^\circ)$$

$$= \sin 15^\circ - \sin 15^\circ$$

$$= 0$$

$-\cos\theta$

and $\cos(-\theta) = \cos\theta$



14. $\cos 25^\circ + \cos 5^\circ + \cos 175^\circ + \cos 205^\circ + \cos 300^\circ = ?$

(a) $\frac{1}{2}$

(b) $-\frac{1}{2}$

(c) $\frac{\sqrt{3}}{2}$

(d) 1

$$\begin{aligned}
 &= \cos 25^\circ + \cos 5^\circ + \cos(180^\circ - 5^\circ) + \cos(180^\circ + 25^\circ) + \cos(360^\circ - 60^\circ) \\
 &= \cancel{\cos 25^\circ} + \cancel{\cos 5^\circ} - \cancel{\cos 5^\circ} - \cancel{\cos 25^\circ} + \cos 60^\circ \\
 &= \frac{1}{2}
 \end{aligned}$$

$$= \frac{\cos(90-3A) - \cos(90+A)}{\cos A + \cos(180+3A)}$$

$$= \frac{\sin 3A + \sin A}{\cos A - \cos 3A}$$

$$= \frac{2 \sin\left(\frac{3A+A}{2}\right) \cdot \cos\left(\frac{3A-A}{2}\right)}{2 \sin\left(\frac{A+3A}{2}\right) \cdot \sin\left(\frac{3A-A}{2}\right)}$$

~~$$= \frac{\cancel{2} \sin 2A \cdot \cos A}{\cancel{2} \sin 2A \cdot \sin A} = \cot A$$~~

15.

$$\frac{\cos\left(\frac{\pi}{2} - 3A\right) - \cos\left(\frac{\pi}{2} + A\right)}{\cos A + \cos(\pi + 3A)} = ?$$

(a) $\tan 2A$ (c) $\tan 2A$ (b) $\cot A$ (d) $\cot 2A$

$$* \sin C + \sin D = 2 \sin\left(\frac{C+D}{2}\right) \cdot \cos\left(\frac{C-D}{2}\right)$$

$$* \sin C - \sin D = 2 \sin\left(\frac{C-D}{2}\right) \cdot \cos\left(\frac{C+D}{2}\right)$$

$$* \cos C + \cos D = 2 \cos\left(\frac{C+D}{2}\right) \cos\left(\frac{C-D}{2}\right)$$

$$* \cos C - \cos D = 2 \sin\left(\frac{C+D}{2}\right) \cdot \sin\left(\frac{D-C}{2}\right)$$

$$= \cos A + \cos B + \cos C + \cos D$$

$$= \cos A + \cos(180 - D)$$

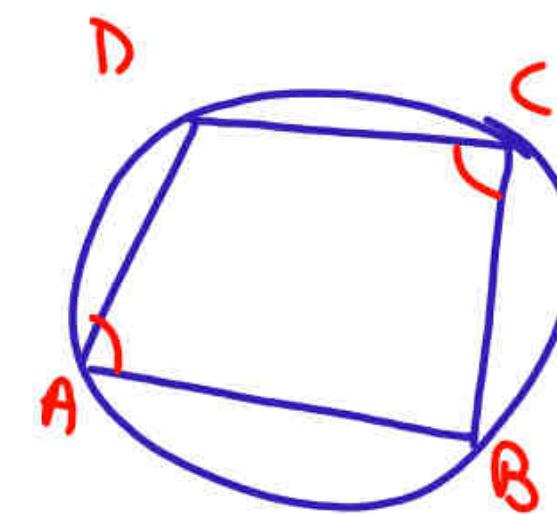
$$+ \cos(180 - A) + \cos D$$

$$= \cancel{\cos A} - \cancel{\cos D} - (\cancel{\cos A} + \cancel{\cos D})$$

$$= 0$$

16.

- If ABCD is a cyclic quadrilateral then
 $\cos A + \cos B + \cos C + \cos D = ?$
- (a) $2(\cos A + \cos C)$ (b) $2(\cos D + \cos B)$
(c) $2(\sin A + \sin C)$ (d) 0



$$\angle A + \angle C = 180^\circ$$

$$\angle B + \angle D = 180^\circ$$

$$17. \quad \tan\theta \sin\left(\frac{\pi}{2} + \theta\right) \cos\left(\frac{\pi}{2} - \theta\right) = ?$$

$$= \frac{\sin \theta \cdot \cos \theta}{\cos \theta} \cdot \sin \theta$$

18. $\tan A + \tan(180^\circ + A) + \cot(90^\circ + A)$
 $+ \cot(360^\circ - A) = ?$

$$\tan A + \tan A - \tan A - \cot A$$

$$= \tan A - \cot A$$

$$\begin{aligned} & \cot \frac{6\pi}{7} \\ &= \cot(\pi - \frac{\pi}{7}) \\ &= -\cot \frac{\pi}{7} \end{aligned}$$

$$\begin{aligned} & \cot \frac{5\pi}{7} \\ &= \cot(\pi - \frac{2\pi}{7}) \\ &= -\cot \frac{2\pi}{7} \end{aligned}$$

19. $\cot \frac{\pi}{7} + \cot \frac{2\pi}{7} + \cot \frac{3\pi}{7} + \dots + \cot \frac{6\pi}{7} = ?$
- (a) 0 (b) 1 (c) -1 (d) 2

$$\begin{aligned} & \cot \frac{\pi}{7} + \cot \frac{2\pi}{7} + \cot \frac{3\pi}{7} + \cot \frac{4\pi}{7} + \cot \frac{5\pi}{7} + \cot \frac{6\pi}{7} \\ &= \cancel{\cot \frac{\pi}{7}} + \cancel{\cot \frac{2\pi}{7}} + \cancel{\cot \frac{3\pi}{7}} - \cancel{\cot \frac{4\pi}{7}} - \cancel{\cot \frac{5\pi}{7}} - \cancel{\cot \frac{6\pi}{7}} \\ &= 0 \end{aligned}$$

$$\cos\theta + 2\cos\theta + 4\omega\sin\theta$$

$$= \cos\theta(1+2+4) \checkmark$$

$$\cos 10^\circ + \cos 20^\circ + \cos 30^\circ$$

$$\cos 10^\circ(1+2+3) \times$$

$$= \frac{1 - \cos \frac{\pi}{4}}{2} + \frac{1 - \cos \frac{3\pi}{4}}{2}$$

$$+ \frac{1 - \cos \frac{5\pi}{4}}{2} + \frac{1 - \cos \frac{7\pi}{4}}{2}$$

$$= \frac{1}{2} \left[1 - \cancel{\cos \frac{\pi}{4}} + 1 - \cancel{\cos \frac{3\pi}{4}} + 1 + \cancel{\cos \frac{\pi}{4}} \right. \\ \left. + 1 + \cancel{\cos \frac{3\pi}{4}} \right]$$

$$= \frac{1}{2} [4]_2$$

$$= 2$$

20.

$$\sin^2 \frac{\pi}{8} + \sin^2 \frac{3\pi}{8} + \sin^2 \frac{5\pi}{8} + \sin^2 \frac{7\pi}{8} = ?$$

(a) $\frac{1}{2}$

(c) $\frac{3}{2}$

(b) 2

(d) $\frac{3}{4}$

$$\cos 2\theta = 1 - 2 \sin^2 \theta$$

$$2 \sin^2 \theta = 1 - \cos 2\theta$$

$$\sin^2 \theta = \frac{1 - \cos 2\theta}{2}$$

$$A + B = 90^\circ$$

$$\sin^2 A + \sin^2 B = 1$$

Ex:- $\underbrace{\sin^2 10^\circ + \sin^2 80^\circ}_{} = 1$

8π 1 sec
= 2 $\left(\sin^2 \frac{\pi}{8} + \sin^2 \frac{3\pi}{8} \right)$

= 2 × 1

20. $\sin^2 \frac{\pi}{8} + \sin^2 \frac{3\pi}{8} + \sin^2 \frac{5\pi}{8} + \sin^2 \frac{7\pi}{8} = ?$

(a) $\frac{1}{2}$

(c) $\frac{3}{2}$

(b) 2

(d) $\frac{3}{4}$

$$\frac{4}{3} \cot^2 30^\circ + 3 \cos^2 (90+60^\circ) - 4 \times 2 \\ + 8 \times 1$$

21. What is the value of $\frac{4}{3} \cot^2 \frac{\pi}{6} + 3 \cos^2 150^\circ$

$$= \cancel{\frac{4}{3}} \times 3 + 3 \times \sin^2 60^\circ - \cancel{8} + \cancel{8} \\ = 4 + 3 \times \frac{3}{4} = \frac{25}{4}$$

$$- 4 \operatorname{cosec}^2 45^\circ + 8 \sin \frac{\pi}{2} ?$$

(a) $\frac{25}{4}$

(c) $-\frac{7}{2}$

(b) 1

(d) $\frac{13}{2}$

$$\sin 2\theta = 2 \sin \theta \cdot \cos \theta$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta$$

$$= \frac{2 \times \sin 2A \times \cos 2A}{-\sin 4A}$$

$$= \frac{\cancel{-\sin 4A}}{\cancel{-\sin 4A}} = -1$$

22.

What is the value of

$$\frac{\left[\{4\cos(90 - A)\sin^3(90 + A)\} - \{4\sin(90 + A)\cos^3(90 - A)\} \right]}{\cos\left(\frac{180 + 8A}{2}\right)}$$

(a) 1

(c) 0

(b) -1

(d) 2

$$\begin{aligned}
 & \frac{4\sin A \cos^3 A - 4\cos A \cdot \sin^3 A}{-\sin 4A} \\
 &= 2 \times 2 \frac{\sin A \cos A (\cos^2 A - \sin^2 A)}{-\sin 4A}
 \end{aligned}$$

$$\begin{aligned}
 &= -\cancel{4} \times \frac{1}{2} \left(\frac{3}{4} - \frac{1}{4} \right) \\
 &= -2 \times \frac{2}{4} = \textcircled{-1}
 \end{aligned}$$

22. What is the value of

$$\frac{\left[\{4\cos(90 - A)\sin^3(90 + A)\} - \{4\sin(90 + A)\cos^3(90 - A)\} \right]}{\cos\left(\frac{180 + 8A}{2}\right)}$$

let $A = 30^\circ$

- (a) 1
- (c) 0
- (b) -1
- (d) 2

$$\begin{aligned}
 &= \frac{4\cos 60^\circ \cos^3 30^\circ - 4\cos 30^\circ \cdot \cos^3 60^\circ}{-\cos 30^\circ} \\
 &= \frac{4\cos 30^\circ \cos 60^\circ (\cos^2 30^\circ - \cos^2 60^\circ)}{-\cos 30^\circ}
 \end{aligned}$$

$$\tan \frac{\pi}{4} \times \tan \frac{3\pi}{4}$$

$$\begin{aligned}
 &= \tan \frac{\pi}{4} \times \tan \left(\pi - \frac{\pi}{4} \right) \\
 &= 1 \times \left(-\tan \frac{\pi}{4} \right) \\
 &= 1 \times (-1) = -1
 \end{aligned}$$

23.

What is the value of

$$\tan \left(\frac{\pi}{4} + A \right) \times \tan \left(\frac{3\pi}{4} + A \right) ?$$

(a) 0

(b) 1

(c) $\frac{\cot A}{2}$

(d) -1

24. What is the value of $\sin(630^\circ + A) + \cos A$?

(a) $\sqrt{\frac{3}{2}}$

(b) $\frac{1}{2}$

(c) 0

(d) $2\sqrt{3}$

$$= \sin(630^\circ + A) + \cos A$$

$$= \sin(90^\circ \times 7 + A) + \cos A$$

$$= -\cos A + \cos A$$

$$0$$

$$\begin{array}{l} A = D \\ B = 0 \end{array}$$

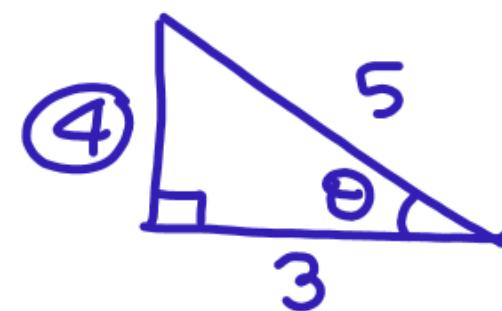
25. What is the value of $\cos(90 - B) \sin(C - A) + \sin(90 + A)\cos(B + C) - \sin(90 - C) \cos(A + B)$?

$$\begin{aligned}
 &= \cancel{\sin B} \cdot \sin(C-A) + \cos A \cdot \cos(B+C) - \cos C \cdot \cos(A+B) \\
 &= 0 + \cancel{\cos C} - \cancel{\cos C} \\
 &= 0
 \end{aligned}$$

$$\cos \theta = \frac{3}{5}$$

$$\sin \theta = \frac{4}{5}$$

$$\tan \theta = \frac{4}{3}$$

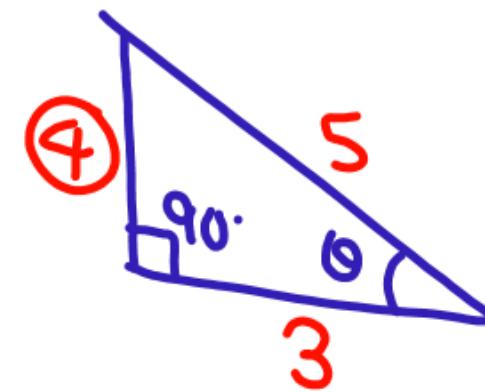
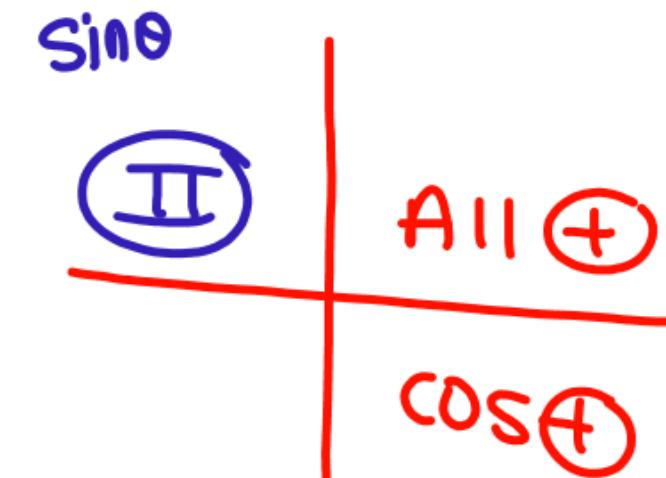


$$\cos \theta = -\frac{3}{5}$$

$$90^\circ < \theta < 180^\circ$$

$$\sin \theta = +\frac{4}{5}$$

$$\tan \theta = -\frac{4}{3}$$



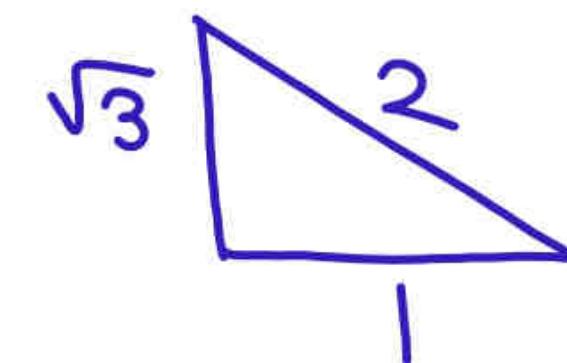
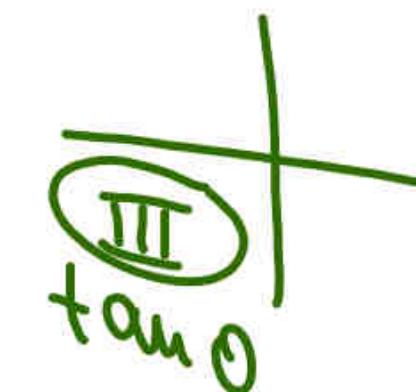
$$\begin{aligned}
 & 2\tan^2x - 3\cosec^2x \\
 &= 2x \left(\frac{\sqrt{3}}{1}\right)^2 - 3x \left(-\frac{2}{\sqrt{3}}\right)^2 \\
 &= 2x 3 - 3x \frac{4}{3} \\
 &= \textcircled{2}
 \end{aligned}$$

26.

If $\cos x = -\frac{1}{2}$ and $\pi < x < \frac{3\pi}{2}$, then the value of $2\tan^2x - 3\cosec^2x$ is :

SSC CHSL 8 July 2019 (Morning)

- (a) 2
- (b) 10
- (c) 8
- (d) 4



$$\begin{aligned}
 &= 2\omega^2x + 3\sec^2x \\
 &= 2x \left(\frac{\sqrt{3}}{1}\right)^2 + 3 \left(-\frac{2}{\sqrt{3}}\right)^2 \\
 &= 2x \cdot 3 + 3 \cdot \frac{4}{3} \\
 &= 2x + 4 \\
 &= 10
 \end{aligned}$$

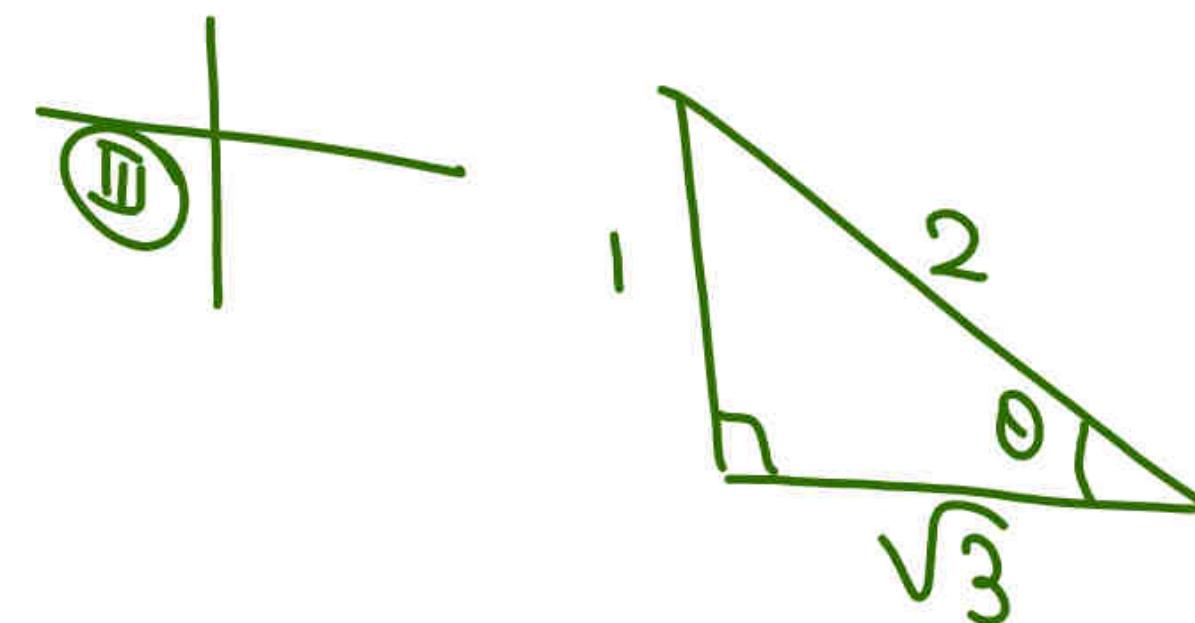
27.

If $\cos x = -\frac{\sqrt{3}}{2}$ and $\pi < x < \frac{3\pi}{2}$, then the value of $2\cot^2x + 3\sec^2x$ is :

SSC CHSL 8 July 2019 (Afternoon)

- (a) 10
- (c) 8

- (b) 4
- (d) 16



Use Option

(a) $\cos(180+90^\circ) = -\cos 90^\circ$
 $= 0$

(b) $\cos(90+30^\circ) = -\sin 30^\circ$
 $= -\frac{1}{2}$

28. Find x if $\cos x = -\frac{1}{2}$.

SSC CHSL 15/10/2020 (Evening)

(a) ~~$\frac{3\pi}{2} = 270^\circ$~~

(c) $\frac{5\pi}{2} = 450^\circ$

(b) $\frac{2\pi}{3} = 120^\circ$

(d) $\frac{4\pi}{3} = 240^\circ$

By Method

$$\cos x = -\cos 60^\circ$$

$$= \cos(180^\circ - 60^\circ)$$

$$= \cos 120^\circ$$

28.

Find x if $\cos x = -\frac{1}{2}$

$$x < \pi$$

SSC CHSL 15/10/2020 (Evening)

$$(a) \frac{3\pi}{2} = 270^\circ$$

$$(c) \frac{5\pi}{2} = 450^\circ$$

$$(b) \frac{2\pi}{3} = 120^\circ$$

$$(d) \frac{4\pi}{3} = 240^\circ$$