

# TRIGONOMETRY-05

## TRIGONOMETRIC IDENTITIES

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MATHS EXPERT

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# TRIGONOMETRY (Practice Sheet - 5)

## Questions Based on Basic Trigonometric Identities

1. The numerical value of

$$\frac{5}{\sec^2\theta} + \frac{2}{1 + \cot^2\theta} + 3\sin^2\theta \text{ is :}$$

*SSC CGL 13 June 2019 (Evening)*

- (a) 5                      (b) 2  
 (c) 3                      (d) 4

2. The numerical value of

$$\left( \frac{1}{1 + \cot^2\theta} + \frac{3}{1 + \tan^2\theta} + 2\sin^2\theta \right) \text{ is :}$$

- (a) 2                      (b) 5  
 (c) 6                      (d) 3

3. The numerical value of

$$\left( \frac{1}{\cos\theta} + \frac{1}{\cot\theta} \right) \left( \frac{1}{\cos\theta} - \frac{1}{\cot\theta} \right) \text{ is :}$$

- (a) 0                      (b) -1  
 (c) 1                      (d) 2

4. The value of  $\frac{\sin A}{1 + \cos A} + \frac{\sin A}{1 - \cos A}$  is

$(0^\circ < A < 90^\circ)$  :

- (a) 2 cosecA              (b) 2 secA  
 (c) 2 sinA                (d) 2 cosA

5. The numerical value of

$$1 + \frac{1}{\cot^2 63^\circ} - \sec^2 27^\circ + \frac{1}{\sin^2 63^\circ} - \cosec^2 27^\circ$$

is :

- (a) 1                      (b) 2  
 (c) -1                    (d) 0

6. If  $\tan 9^\circ = \frac{p}{q}$ , then the value of  $\frac{\sec^2 81^\circ}{1 + \cot^2 81^\circ}$  is :

- (a)  $\frac{p}{q}$                     (b) 1  
 (c)  $\frac{p^2}{q^2}$                 (d)  $\frac{q^2}{p^2}$

7.  $\sin^6\theta + \cos^6\theta + 3\sin^2\theta \cos^2\theta = ?$

- (a) 0                      (b)  $-\frac{1}{2}$   
 (c) 1                      (d)  $\frac{1}{3}$

8. What is the value of

$$\frac{1}{\sin^4(90^\circ - \theta)} + \frac{1}{[\cos^2(90^\circ - \theta) - 1]} = ?$$

- (a)  $\tan^2\theta \sec^2\theta$               (b)  $\sec^4\theta$   
 (c)  $\tan^4\theta$                       (d)  $\tan^2\theta \sin^2\theta$

9. What is the value of

$$\frac{1 + 2\cot^2(90^\circ - x) - 2\cosec(90^\circ - x)\cot(90^\circ - x)}{\cosec(90^\circ - x) - \cot(90^\circ - x)} ?$$

- (a)  $\cos x + \sin x$   
 (b)  $\sin x - \cos x$   
 (c)  $\sec x + \tan x$   
 (d)  $\sec x - \tan x$

10.  $\frac{2 + \tan^2\theta + \cot^2\theta}{\sec\theta \cosec\theta}$  is equal to :

*SSC CGL 4 June 2019 (Morning)*

- (a)  $\cot\theta$                     (b)  $\cos\theta \cdot \sin\theta$   
 (c)  $\sec\theta \cdot \cosec\theta$         (d)  $\tan\theta$

11. If  $(1 + \tan^2\theta) + [1 + (\tan^2\theta)^{-1}] = k$ , then  $\sqrt{k} = ?$

*SSC CGL 6 June 2019 (Evening)*

- (a)  $\sec\theta \cdot \cosec\theta$         (b)  $\cos\theta \cdot \cosec\theta$   
 (c)  $\sin\theta \cdot \cos\theta$             (d)  $\sec\theta \cdot \sin\theta$

12.  $\frac{(\sec\theta + \tan\theta)(1 - \sin\theta)}{\cosec\theta(1 + \cos\theta)(\cosec\theta - \cot\theta)}$  is equal to :

*SSC CHSL 2 July 2019 (Morning)*

- (a)  $\sin\theta$                       (b)  $\sec\theta$   
 (c)  $\cos\theta$                       (d)  $\cosec\theta$

13. If  $\frac{(\sin\theta - \cosec\theta)(\cos\theta - \sec\theta)}{\tan^2\theta - \sin^2\theta} = r^2$ , then  $r = ?$

*SSC CHSL 3 July 2019 (Morning)*

- (a)  $\sin\theta \cdot \cos\theta$

- (b)  $\tan\theta$

- (c)  $\cot\theta$

- (d)  $\cosec\theta \cdot \sec\theta$

14. If  $\left( \frac{\tan\theta - \sec\theta + 1}{\tan\theta + \sec\theta - 1} \right) \sec\theta = \frac{1}{k}$ , then  $k = ?$

*SSC CGL 7 June 2019 (Afternoon)*

- (a)  $1 + \sin\theta$                 (b)  $1 - \cos\theta$   
 (c)  $1 + \cos\theta$                 (d)  $1 - \sin\theta$

15. If  $\frac{\tan\theta}{1 - \cot\theta} + \frac{\cot\theta}{1 - \tan\theta} = 1 + k$ , then  $k = ?$   
**SSC CGL 7 June 2019 (Evening)**
- (a)  $\cot\theta + \sec\theta$     (b)  $\tan\theta \cdot \cosec\theta$   
(c)  $\tan\theta + \sec\theta$     (d)  $\cosec\theta \cdot \sec\theta$
16. If  $\left(\frac{1}{1 + \cosec\theta} - \frac{1}{1 - \cosec\theta}\right) \cos\theta = 2$ ,  $0^\circ < \theta < 90^\circ$ ,  
then the value of  $\sin^2\theta + \cot^2\theta + \sec^2\theta$  is :  
**SSC CHSL 3 July 2019 (Evening)**
- (a) 1                          (b)  $2\frac{1}{2}$   
(c)  $3\frac{1}{2}$                       (d) 2
17. It is given that  $\sqrt{\frac{1 - \sin x}{1 + \sin x}} = a - \tan x$ ,  
then  $a$  is equal to :  
**SSC CHSL 10 July 2019 (Evening)**
- (a)  $\cos x$                       (b)  $\sin x$   
(c)  $\cosec x$                       (d)  $\sec x$
18.  $\frac{(1 + \cos\theta)^2 + \sin^2\theta}{(\cosec^2\theta - 1) + \sin^2\theta} = ?$   
**SSC CGL Tier-II (11 September 2019)**
- (a)  $\cos\theta(1 + \sin\theta)$   
(b)  $2\cos\theta(1 + \sec\theta)$   
(c)  $\sec\theta(1 + \sin\theta)$   
(d)  $2\sec\theta(1 + \sec\theta)$
19.  $\left(\frac{1 - \tan\theta}{1 - \cot\theta}\right)^2 + 1 = ?$   
**SSC CGL Tier-II (11 September 2019)**
- (a)  $\cosec^2\theta$   
(b)  $\sec^2\theta$   
(c)  $\sin^2\theta$   
(d)  $\cos^2\theta$
20.  $\sqrt{\frac{\cot\theta + \cos\theta}{\cot\theta - \cos\theta}}$  is equal to :  
**SSC CGL Tier-II (11 September 2019)**
- (a)  $\sec\theta + \tan\theta$     (b)  $1 + \sec\theta \cdot \tan\theta$   
(c)  $1 - \sec\theta \cdot \tan\theta$     (d)  $\sec\theta - \tan\theta$
21. The value of  
 $\left(\frac{\sin A}{1 - \cos A} + \frac{1 - \cos A}{\sin A}\right) \div \left(\frac{\cot^2 A}{1 + \cosec A} + 1\right)$  is :  
**SSC CGL Tier-II (12 September 2019)**
- (a)  $\frac{3}{2}$                           (b)  $\frac{1}{2}$   
(c) 1                                  (d) 2
22. The value of  
 $\frac{\sin\varphi(1 - \sin\varphi)(\sin\varphi + \cos\varphi)(\sec\varphi + \tan\varphi)}{\sin\varphi(1 + \tan\varphi) + \cos\varphi(1 + \cot\varphi)}$  is :  
**SSC CGL Tier-II (12 September 2019)**
- (a)  $2\cos\varphi$                       (b)  $\cosec\varphi \cdot \sec\varphi$   
(c)  $2\sin\varphi$                         (d)  $\sin^2\varphi \cdot \cos^2\varphi$   
 $(\sec\varphi - \tan\varphi)^2(1 + \sin\varphi)^2 \div \sin^2\varphi = ?$   
**SSC CGL Tier-II (12 September 2019)**
- (a)  $\cos\varphi$                         (b)  $\cot^2\varphi$   
(c)  $\sec\varphi$                         (d)  $\cos^2\varphi$
23. The value of  $(1 + \cot\theta - \cosec\theta)(1 + \cos\theta + \sin\theta)\sec\theta = ?$   
**SSC CGL Tier-II (13 September 2019)**
- (a) -2                              (b) 2  
(c)  $\sec\theta \cdot \cosec\theta$             (d)  $\sin\theta \cdot \cos\theta$
24. The value of  $\sqrt{\frac{\cosec\varphi - \cot\varphi}{\cosec\varphi + \cot\varphi}} \div \frac{\sin\varphi}{1 + \cos\varphi}$   
is equal to :  
**SSC CGL Tier-II (12 September 2019)**
- (a)  $\cosec\varphi$                       (b)  $\frac{1}{2}$   
(c)  $\sec\varphi$                         (d) 1
25. Find the value  
 $\frac{(\sin\theta - \cos\theta) - (1 + \tan\theta + \cot\theta)}{1 + \sin\theta \cos\theta} = ?$   
**SSC CGL Tier-II (13 September 2019)**
- (a)  $\sec\theta - \cosec\theta$             (b)  $\cosec\theta - \sec\theta$   
(c)  $\sin\theta + \cos\theta$                 (d)  $\tan\theta + \cot\theta$
26. Find the value of  
 $\frac{\sin\theta + \cos\theta - 1}{\sin\theta - \cos\theta + 1} \times \frac{\tan^2\theta(\cosec^2\theta - 1)}{\sec\theta - \tan\theta}$ .  
**SSC CGL Tier-II (13 September 2019)**
- (a) 0                                (b) -1  
(c) 1                                (d)  $\frac{1}{2}$
27. The value of  $\frac{1 - 2\sin^2\theta\cos^2\theta}{\sin^4\theta + \cos^4\theta} - 1$  is :  
**SSC CGL 7 March 2020 (Morning)**
- (a)  $-2\sin^2\theta \cdot \cos^2\theta$     (b) -1  
(c) 0                                (d) 1
28. The value of  $(\cosec A + \cot A + 1)(\cosec A - \cot A + 1) - 2\cosec A$  is  
**SSC CGL 9 March 2020 (Afternoon)**
- (a) 4cosecA                        (b) 2  
(c) 2cosecA                        (d) 0
29. If  $117\cos^2 A + 129\sin^2 A = 120$  and  $170\cos^2 B + 158\sin^2 B = 161$ , then the value of  $\cosec^2 A \cdot \sec^2 B$  is :  
**SSC CHSL 13/10/2020 (Morning)**
- (a) 1                                (b) 9  
(c) 4                                (d) 16
30. If  $\tan^4 x - \tan^2 x = 1$ , then the value of  $\sin^4 x + \sin^2 x = ?$   
**SSC CHSL 14/10/2020 (Afternoon)**

- (a)  $\frac{3}{4}$       (b)  $\frac{1}{2}$   
(c) 1      (d)  $\frac{3}{2}$
32. The value of  $\sin^4\theta + \cos^4\theta + 2\sin^2\theta\cos^2\theta$  is  
SSC CHSL 19/10/2020 (Evening)  
(a) 1      (b) 2  
(c) 4      (d) 0
33.  $\cos A(\sec A - \cosec A)(\cot A + \tan A) = ?$   
SSC CGL 2019, Tier-II (15/10/2020)  
(a) secA      (b) cotA  
(c) sinA      (d) tanA
34.  $\left(\frac{1}{\cos\theta} - \frac{1}{\sin\theta}\right) + \frac{1}{\cosec\theta - \cot\theta} - \frac{1}{\sec\theta + \tan\theta} = ?$   
SSC CGL 2019, Tier-II (15/10/2020)  
(a)  $\sec\theta.\cosec\theta$       (b)  $\sin\theta.\tan\theta$   
(c)  $\cosec\theta.\cot\theta$       (d)  $\sin\theta.\cos\theta$
35. The value of  

$$\frac{\sec^2\theta(2 + \tan^2\theta + \cot^2\theta)}{(\cosec^2\theta + \sec^2\theta)(1 + \cot^2\theta)^2}$$
 is  
SSC CGL 2019, Tier-II (15/10/2020)  
(a) -1      (b) 1  
(c) -2      (d) 2
36. The value of  

$$\frac{\cos^6\theta + \sin^6\theta + 3\sin^2\theta\cos^2\theta}{\cosec\theta\sec\theta(\sin\theta + \cos\theta - 1)(\sin\theta + \cos\theta + 1)}$$
 is  
SSC CGL 2019, Tier-II (15/10/2020)  
(a) 1      (b) 2  
(c)  $\frac{1}{2}$       (d) 3
37. The value of  $\frac{\sin\theta + \cos\theta - 1}{\sin\theta - \cos\theta + 1} \times \sqrt{\frac{1 + \sin\theta}{1 - \sin\theta}}$   
SSC CGL 2019, Tier-II (16/10/2020)  
(a) 1      (b) -1  
(c) -2      (d) 2
38. If  $0^\circ < \theta < 90^\circ$ ,  
 $3b\cosec\theta = a\sec\theta$  and  $3a\sec\theta - b\cosec\theta = 8$ , then the value of  $9b^2 + a^2$  is :  
SSC CHSL 19/10/2020 (Afternoon)  
(a) 6      (b) 8  
(c) 9      (d) 7
39. If  $x\sin^3\theta + y\cos^3\theta = \sin\theta.\cos\theta$  and  $x\sin\theta = y\cos\theta$  then the value of  $x^2 + y^2$  is :  
SSC CHSL 20/10/2020 (Morning)  
(a) 0      (b) 4  
(c) 1      (d) 2
40. If  $4 - 2\sin^2\theta - 5\cos\theta = 0$ ,  $0^\circ < \theta < 90^\circ$ , then the value of  $\sin\theta + \tan\theta$  is :  
SSC CGL 4 June 2019 (Morning)  
(a)  $\frac{3\sqrt{2}}{2}$       (b)  $\frac{3\sqrt{3}}{2}$   
(c)  $3\sqrt{2}$       (d)  $2\sqrt{3}$
41. If  $\cos^2\theta - 3\cos\theta + 2 = \sin^2\theta$ ,  $0^\circ < \theta < 90^\circ$ , then the value of  $2\cosec\theta + 4\cot\theta$  is :  
SSC CGL 7 June 2019 (Afternoon)  
(a)  $\frac{8\sqrt{3}}{3}$       (b)  $\frac{4\sqrt{3}}{4}$   
(c)  $2\sqrt{3}$       (d)  $4\sqrt{3}$
42. For  $\theta$  being an acute angle,  $4(2\sin^2\theta + 7\cos^2\theta) = 13$ . What is the value of  $\theta$ ?  
SSC CHSL 10 July 2019 (Morning)  
(a)  $60^\circ$       (b)  $45^\circ$   
(c)  $30^\circ$       (d)  $0^\circ$
43. If  $\frac{\sin^2\phi - 3\sin\phi + 2}{\cos^2\phi} = 1$ , where  $0^\circ < \phi < 90^\circ$ , then the value of  $(\cos 2\phi + \sin 3\phi + \cosec 2\phi)$  is :  
SSC CGL Tier-II (12 September, 2019)  
(a)  $\frac{2+\sqrt{3}}{3}$       (b)  $\frac{3+\sqrt{3}}{6}$   
(c)  $\frac{9+4\sqrt{3}}{6}$       (d)  $\frac{3+2\sqrt{3}}{3}$
44. If  $2\cos^2\theta - 3\sin\theta = 3$ ,  $0^\circ < \theta < 90^\circ$ , then What is the value of  $\sin^2 2\theta + \cos^2\theta + \tan^2 2\theta + \cosec^2 2\theta$  is :  
SSC CGL Tier-II (13 September, 2019)  
(a)  $\frac{35}{12}$       (b)  $\frac{29}{3}$   
(c)  $\frac{35}{6}$       (d)  $\frac{29}{6}$

## Answer Key

|               |               |               |               |               |               |               |               |               |               |
|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
| <b>1.(a)</b>  | <b>2.(d)</b>  | <b>3.(c)</b>  | <b>4.(a)</b>  | <b>5.(d)</b>  | <b>6.(d)</b>  | <b>7.(c)</b>  | <b>8.(a)</b>  | <b>9.(d)</b>  | <b>10.(c)</b> |
| <b>11.(a)</b> | <b>12.(c)</b> | <b>13.(c)</b> | <b>14.(a)</b> | <b>15.(d)</b> | <b>16.(c)</b> | <b>17.(d)</b> | <b>18.(d)</b> | <b>19.(b)</b> | <b>20.(a)</b> |
| <b>21.(d)</b> | <b>22.(d)</b> | <b>23.(b)</b> | <b>24.(b)</b> | <b>25.(d)</b> | <b>26.(a)</b> | <b>27.(c)</b> | <b>28.(c)</b> | <b>29.(b)</b> | <b>30.(d)</b> |
| <b>31.(c)</b> | <b>32.(a)</b> | <b>33.(d)</b> | <b>34.(a)</b> | <b>35.(a)</b> | <b>36.(c)</b> | <b>37.(a)</b> | <b>38.(c)</b> | <b>39.(c)</b> | <b>40.(b)</b> |
| <b>41.(a)</b> | <b>42.(a)</b> | <b>43.(c)</b> | <b>44.(c)</b> |               |               |               |               |               |               |

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