

ALGEBRA-01

SOME BASIC CONCEPTS

BY ADITYA RANJAN



Maths By Aditya Ranjan



Rankers Gurukul



MATHS EXPERT

PDF की विशेषताएं
INDIA में पहली बार

- UPDATED CONTENT
- TYPE WISE
- LEVEL WISE
- BILINGUAL
- ERROR FREE

MATHS SPECIAL BATCH
में Enroll करने के लिए

DOWNLOAD
RG VIKRAMJEET APP

GET IT ON
Google Play





UPDATED SHEETS नौकरी आपकी जिद हमारी



<https://youtube.com/c/RankersGurukul>

For Free PDFs Join Telegram <https://t.me/RankersGurukulLive>

SSC CGL 19 Maths-227/200



MATHS BY ADITYA RANJAN SIR

ALGEBRA (Practice Sheet - 1) Some Basic Concepts

1. If $x + \frac{1}{x} = 3$ Find

- (i) $x^2 + \frac{1}{x^2}$
- (ii) $x^3 + \frac{1}{x^3}$
- (iii) $x^4 + \frac{1}{x^4}$
- (iv) $x^5 + \frac{1}{x^5}$
- (v) $x^6 + \frac{1}{x^6}$
- (vi) $x^7 + \frac{1}{x^7}$

2. If $x - \frac{1}{x} = 4$, Find

- (i) $x^2 + \frac{1}{x^2}$
- (ii) $x^2 - \frac{1}{x^2}$
- (iii) $x^3 - \frac{1}{x^3}$
- (iv) $x^4 + \frac{1}{x^4}$
- (v) $x^5 - \frac{1}{x^5}$
- (vi) $x^6 - \frac{1}{x^6}$

3. If $a + \frac{1}{a} = 3$, then $\left(a^4 + \frac{1}{a^4}\right)$ is equal to :

SSC CGL 6 June 2019 (Evening)

- (a) 77
- (b) 47
- (c) 81
- (d) 27

4. If $x + \frac{1}{x} = \sqrt{5}$, then $x^3 + \frac{1}{x^3}$ is equal to :

SSC CGL 10 June 2019 (Evening)

- (a) $3\sqrt{5}$
- (b) $4\sqrt{5}$
- (c) $2\sqrt{5}$
- (d) $5\sqrt{5}$

5. If $x + \frac{1}{x} = 3$, then $x^3 + \frac{1}{x^3}$ is equal to :

SSC CGL 10 June 2019 (Afternoon)

- (a) 27
- (b) 36
- (c) 24
- (d) 18

6. If $\sqrt{x} + \frac{1}{\sqrt{x}} = \sqrt{6}$, then $x^2 + \frac{1}{x^2}$ is equal to :

SSC CGL 11 June 2019 (Morning)

- (a) 62
- (b) 14
- (c) 16
- (d) 36

7. If $\sqrt{x} + \frac{1}{\sqrt{x}} = \sqrt{7}$, then $x^3 + \frac{1}{x^3}$ is equal to :

SSC CGL 11 June 2019 (Evening)

- (a) 140
- (b) 130
- (c) 120
- (d) 110

8. $\sqrt{x} + \frac{1}{\sqrt{x}} = 2\sqrt{2}$, then $x^2 + \frac{1}{x^2}$ is equal to :

SSC CGL 12 June 2019 (Morning)

- (a) 34
- (b) 64
- (c) 36
- (d) 32

9. If $x^2 + 1 = 3x$, then the value of $\frac{x^4 + x^{-2}}{x^2 + 5x + 1}$ is:

SSC CHSL 2 July 2019 (Evening)

- (a) $2\frac{1}{2}$
- (b) $2\frac{1}{4}$
- (c) $4\frac{1}{2}$
- (d) $3\frac{1}{2}$

10. If $a + \frac{1}{a} = 3$, then $a^6 + \frac{1}{a^6}$ is equal to :

SSC CHSL 210 July 2019 (Afternoon)

- (a) 319
- (b) 322
- (c) 780
- (d) 730

11. If $x^2 + 3x + 1 = 0$, then what is the value of $x^6 + \frac{1}{x^6}$?

SSC CGL 3 March 2020 (Afternoon)

- (a) 324
- (b) 322
- (c) 318
- (d) 327

12. If $x^2 - 2\sqrt{5}x + 1 = 0$, then what is the value of $x^5 + \frac{1}{x^5}$?

SSC CGL 5 March 2020 (Morning)

- (a) $610\sqrt{5}$
- (b) $408\sqrt{5}$
- (c) $612\sqrt{5}$
- (d) $406\sqrt{5}$

13. If $x + \frac{1}{x} = 8$, then find the value of $\frac{5x}{x^2 + 1 - 6x}$.

SSC CHSL 14/10/2020 (Evening)

SSC CHSL 4 July 2019 (Afternoon)

31. If $x^4 + \frac{1}{x^4} = 23$, find
- (i) $x + \frac{1}{x}$ (ii) $x^3 + \frac{1}{x^3}$
32. If $x^4 + x^{-4} = 2207$, ($x > 0$), then the value of $x + x^{-1}$ is :
SSC CHSL 4 July 2019 (Afternoon)
- (a) 19 (b) 7
(c) 11 (d) 9
33. If $x^4 + x^{-4} = 1442$, ($x > 0$), then the value of $x - x^{-1}$ is :
SSC CHSL 4 July 2019 (Evening)
- (a) 7 (b) 8
(c) 6 (d) 15
34. If $x^4 + x^{-4} = 47$, ($x > 0$), then the value of $(2x - 3)^2$ is :
SSC CHSL 8 July 2019 (Evening)
- (a) 2 (b) 3
(c) 5 (d) 4
35. If $x^4 + x^{-4} = 194$, ($x > 0$), then the value of $(2x - 4)^2$ is :
SSC CHSL 9 July 2019 (Morning)
- (a) 15 (b) 20
(c) 12 (d) 16
36. If $x^4 + x^{-4} = 1154$, ($x > 0$), then the value of $2(x - 3)^2$ is :
SSC CHSL 9 July 2019 (Afternoon)
- (a) 16 (b) 12
(c) 20 (d) 15
37. If $x^8 - 1442x^4 + 1 = 0$, then a possible value of $x - \frac{1}{x}$ is :
SSC CGL Tier-II (11 September 2019)
- (a) 5 (b) 8
(c) 4 (d) 6
38. If $x^4 + \frac{1}{x^4} = 14159$, then the value of $x + \frac{1}{x}$ is
SSC CHSL 19 March 2020 (Afternoon)
- (a) 9 (b) 12
(c) 10 (d) 11
39. If $x^4 + x^{-4} = 194$, ($x > 0$), then the value of $(x - 2)^2$ is :
SSC CGL 4 June 2019 (Morning)
- (a) 1 (b) 6
(c) 2 (d) 3
40. If $x^4 + \frac{1}{x^4} = 322$, find $x^3 - \frac{1}{x^3}$
41. If $a + \frac{1}{a} = 2$, then $a^4 - \frac{1}{a^4}$ is equal to :
SSC CHSL 10 July 2019 (Morning)
- (a) 0 (b) $\frac{1}{4}$
(c) 1 (d) 4
42. If $x + x^{-1} = 2$, then the value of $x^3 + x^{-3}$ is :
SSC CPO 16 March 2019 (Evening)
- (a) 1 (b) 2
(c) 3 (d) 4
43. If $a + \frac{1}{a} + 2 = 0$, then the value of $a^{15} - \frac{1}{a^{100}}$ is:
SSC CHSL 21 October 2020 (Evening)
- (a) 0 (b) 2
(c) -2 (d) 1
44. If $p + \left(\frac{1}{p}\right) = 2$, then find the value of $p \times p \times p$.
SSC CHSL 18 March 2020 (Afternoon)
- (a) 4 (b) 8
(c) 1 (d) 2
45. If $x + \frac{1}{x} = 2$, find
- (i) $x^{20} + x^{19} + x^{18} + \dots + x^2 + x + 1$
(ii) $x^{49} - x^{48} + x^{47} - x^{46} + \dots + x^3 - x^2 + x + 1$
(iii) $x^{12} + \frac{1}{x^{12}}$
(iv) $x^{17} + \frac{1}{x^9}$
(v) $x^{15} - \frac{1}{x^{17}}$
46. If $x + \frac{1}{x} = -2$
- (i) $x^{39} + x^{38} + \dots + x^2 + x + 1$
(ii) $x^{100} - x^{99} + x^{98} - x^{97} + \dots + x^2 - x + 1$
(iii) $x^5 - \frac{1}{x^5}$
(iv) $x^{18} + \frac{1}{x^{18}}$
(v) $x^7 - \frac{1}{x^9}$
47. If $x + \frac{1}{x} = 1$, find
- (i) $x^{18} + x^{12} + x^6 + 1$
(ii) $x^{99} + x^{96} + x^{93} + x^{90} + \dots + x^6 + x^3 + 1$
(iii) $x^{45} - x^{42} + x^{39} - x^{36} + \dots + x^9 - x^6 + x^3 + 1$
(iv) $x^{32} + x^{46} + x^{90} + 2$
48. If $x = 2 + \sqrt{3}$, find $x + \frac{1}{x}$
- (a) 5 (b) 4
(c) -4 (d) $2\sqrt{3}$
49. If $x = 3 + 2\sqrt{2}$, find $x^2 + \frac{1}{x^2}$
- (a) 36 (b) 30
(c) 34 (d) 32
50. If $m = \frac{\sqrt{3}+1}{\sqrt{3}-1}$ & $n = \frac{\sqrt{3}-1}{\sqrt{3}+1}$ then the value of

- (c) $\sqrt{2(1+\sqrt{13})}(-1-2\sqrt{13})$
(d) $\sqrt{2(1+\sqrt{13})} + (-1+2\sqrt{13})$
85. If $x^4 + \frac{1}{x^4} = \frac{257}{16}$, then find $\frac{8}{13}\left(x^3 + \frac{1}{x^3}\right)$, where $x > 0$.
CHSL 13/10/2020 (Afternoon)
(a) 5 (b) 4 (c) 6 (d) 8
86. If $a^2 + \frac{2}{a^2} = 16$, then find the value of $\frac{72a^2}{a^4 + 2 + 8a^2}$.
CHSL 19/10/2020 (Afternoon)
(a) 3 (b) 1 (c) 4 (d) 2
87. If $x\left(5 - \frac{2}{x}\right) = \frac{5}{x}$, then the value of $x^2 + \frac{1}{x^2}$ is equal to :
CHSL 21/10/2020 (Morning)
(a) $2\frac{4}{25}$ (b) $2\frac{1}{25}$
(c) $\frac{4}{25}$ (d) $2\frac{3}{25}$
88. Given that $x^8 - 34x^4 + 1 = 0$, $x > 0$, what is the value of $(x^3 + x^{-3})$?
CGL 2019 Tier II (15/11/2020)
(a) $5\sqrt{8}$ (b) $6\sqrt{6}$
(c) $5\sqrt{6}$ (d) $6\sqrt{8}$
89. If $3x^2 - 5x + 1 = 0$, then the value of $\left(x^2 + \frac{1}{9x^2}\right)$ is :
CGL 2019 Tier II (15/11/2020)
(a) $1\frac{2}{3}$ (b) $1\frac{1}{3}$
(c) $2\frac{1}{3}$ (d) $2\frac{1}{9}$
90. If $2x^2 - 7x + 5 = 0$, then what is the value of $\left(x^2 + \frac{25}{4x^2}\right)$ is :
CGL 2019 Tier II (16/11/2020)
(a) $9\frac{1}{2}$ (b) $7\frac{1}{4}$
- (c) $9\frac{3}{4}$ (d) $5\frac{1}{2}$
91. If $x - \frac{1}{x} = 5$, $x \neq 0$, then what is the value of $\frac{x^6 + 3x^3 - 1}{x^6 - 8x^3 - 1}$?
CGL 2019 Tier II (16/11/2020)
(a) $\frac{13}{12}$ (b) $\frac{11}{13}$
(c) $\frac{3}{8}$ (d) $\frac{4}{9}$
92. If $x + \frac{16}{x} = 8$, then the value of $x^2 + \frac{32}{x^2}$ is :
CGL 2019 Tier II (16/11/2020)
(a) 24 (b) 18 (c) 20 (d) 16
93. If $x\left(3 - \frac{2}{x}\right) = \frac{3}{x}$, then the value of $x^3 - \frac{1}{x^3}$ is equal to :
CGL 2019 Tier II (18/11/2020)
(a) $\frac{61}{27}$ (b) $\frac{52}{27}$
(c) $\frac{8}{27}$ (d) $\frac{62}{27}$
94. If $x^2 + \frac{1}{x^2} = 7$, then the value of $x^3 + \frac{1}{x^3}$ where $x > 0$ is equal to :
CGL 2019 Tier II (18/11/2020)
(a) 15 (b) 16 (c) 12 (d) 18
95. If $\sqrt{x} + \frac{1}{\sqrt{x}} = 3$, then the value of $x^3 + \frac{1}{x^3}$ is :
CGL 2019 Tier II (18/11/2020)
(a) 324 (b) 322 (c) 326 (d) 422
96. If $x - \frac{3}{x} = 6$, $x \neq 0$, then the value of $\frac{x^4 - \frac{27}{x^2}}{x^2 - 3x - 3}$ is :
CGL 2019 Tier II (18/11/2020)
(a) 90 (b) 270 (c) 80 (d) 54
97. If $x^2 - 3x + 1 = 0$, then the value of $\left(x^5 + \frac{1}{x^3}\right) \div (x^2 + 1)$ is :
CGL 2019 Tier II (18/11/2020)

CPO 2019 24/11/2020 (Morning)

98. If $x + y = 1$ and $xy(xy - 2) = 12$, then the value of $x^4 + y^4$ is :

SSC CGL 4 June 2019 (Evening)

99. If $x^4 - 6x^2 - 1 = 0$, then the value of

$$x^6 - 5x^2 + \frac{5}{x^2} - \frac{1}{x^6} + 5 = ?$$

SSC CGL 4 June 2019 (Morning)

100. If $x + \frac{1}{x} = 4\sqrt{3}$, then find the value of $x^2 + \frac{1}{x^2}$.

SSC CPO 14 March 2019 (Morning)

Answer Key

1.(i) 7	(ii) 18	(iii) 47	(iv) 123	(v) 322	(vi) 843				
2.(i) 18	(ii) $\pm 8\sqrt{5}$	(iii) 76	(iv) 322	(v) 1364	(vi) $\pm 2584\sqrt{5}$				
3.(b)	4.(c)	5.(d)	6.(b)	7.(d)	8.(a)	9.(b)	10.(b)	11.(b)	12.(a)
13.(a)	14.(a)	15.(a)	16.(c)	17.(b)	18.(c)	19.(c)	20.(c)	21.(c)	22.(c)
23.(d)	24.(a)	25.(b)	26.(c)	27.(a)	28.(a)	29.(b)			
30.(i) $\sqrt{29}$	(ii) 5	31.(i) $\sqrt{7}$	(ii) $4\sqrt{7}$						
32.(b)	33.(c)	34.(c)	35.(c)	36.(a)	37.(d)	38.(d)	39.(d)	40. ± 76	
41.(a)	42.(c)	43.(c)	44.(c)						
45.(i) 21	(ii) 2	(iii) 2	(iv) 2	(v) 0					
46.(i) 0	(ii) 101	(iii) 0	(iv) 2	(v) 0					
47.(i) 4	(ii) 0	(iii) -14	(iv) 2						
48.(b)	49.(c)	50.(a)	51.(a)	52.(b)	53.(c)	54.(c)	55.(b)	56.(a)	57.(d)
58.(c)	59.(a)	60.(b)	61.(b)	62.(b)	63.(d)	64.(b)	65.(b)	66.(c)	
67.(i). -2	(ii). -1	(iii). 0		(iv). 2		(v). 0			
68.(a)	69.(c)	70.(d)	71.(b)	72.(a)	73.(c)	74.(c)	75.(a)	76.(a)	77.(d)
78.(a)	79.(b)	80.(b)	81.(d)	82.(c)	83.(b)	84.(a)	85.(a)	86.(a)	87.(a)
88.(a)	89.(d)	90.(b)	91.(a)	92.(b)	93.(d)	94.(d)	95.(b)	96.(a)	97.(b)
98.(b)	99.(b)	100.(a)							

All The Best

