

UNIT DIGIT

इकाई अंक

PRACTICE SHEET

WITH SOLUTIONS

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Unit Digit/ इकाई अंक

(Practice Sheet With Solutions)

16. The unit digit in the square root of 66049 is
66049 के वर्गमूल में इकाई अंक है
(a) 3 (b) 7
(c) 8 (d) 2
17. If in a two digit number, the digit at units place is z and the digit at tens place is 8, then the number is
यदि एक दो अंकों की संख्या में, इकाई के स्थान पर अंक z है और दहाई के स्थान पर अंक 8 है, तो संख्या है
(a) $80z + z$ (b) $80 + z$
(c) $8z + 8$ (d) $80 z + 1$
18. If the unit digit of $(433 \times 456 \times 43N)$ is $(N+2)$, then value of N is?
यदि $(433 \times 456 \times 43N)$ का इकाई अंक $(N+2)$ है, तो N का मान क्या है?
(a) 1 (b) 8
(c) 3 (d) 6
19. The unit digit of $(7^{95} - 3^{58})$
 $(7^{95} - 3^{58})$ में इकाई के अंक ज्ञात कीजिये?
(a) 3 (b) 4
(c) 5 (d) 6
20. What is the units digit of $1! + 2! + 3! + \dots + 99! + 100!$ is?
 $1! 2! 3! \dots 99! + 100!$ का इकाई अंक क्या होता है?
(a) 3 (b) 1
(c) 5 (d) 6
21. Find the unit digit of $4^{5^6 7^8 9^{10}}$ is?
 $4^{5^6 7^8 9^{10}}$ का इकाई अंक ज्ञात कीजिये?
(a) 4 (b) 6
(c) 0 (d) 2
22. What is the unit of $973^{234!} \times 234^{973!}$?
 $973^{234!} \times 234^{973!}$ का इकाई अंक क्या है?
(a) 2 (b) 6
(c) 7 (d) 9
23. Find the unit digit of $(32)^{37^{38}}$ का इकाई अंक क्या है?
(a) 2 (b) 3
(c) 9 (d) 5
24. The unit digit in the expression :
 $(36^{234}) (33^{512}) (39^{180}) - (54^{29}) (25^{123}) (31^{512})$ will be/व्यंजक में इकाई अंक क्या होगा?
(a) 8 (b) 0
(c) 6 (d) 5

25. Find the unit digit of the expression/व्यंजक में इकाई अंक क्या होगा?
 $31^2 + 32^2 + 33^2 + 34^2 + 35^2 + 36^2 + 37^2 + 38^2 + 39^2$
(a) 1 (b) 4
(c) 5 (d) 9
26. Find the unit digit of $29^{42!} + 44^{21!}$ /इकाई अंक क्या होगा?
(a) 6 (b) 7
(c) 9 (d) 3
27. Find the unit digit of $5555^{2345} + 6666^{5678}$ /इकाई अंक क्या होगा?
(a) 1 (b) 3
(c) 5 (d) 7
28. If x is a positive integer, what is the unit digit of $(24)^{2x+1} \times (33)^{x+1} \times (17)^{x+2} \times (9)^{2x}$?
यदि x एक धनात्मक पूर्णांक है, तो $(24)^{2x+1} \times (33)^{x+1} \times (17)^{x+2} \times (9)^{2x}$ का इकाई अंक क्या है?
(a) 4 (b) 6
(c) 7 (d) 8
29. What is the ten's digit in the expression/व्यंजक में दहाई का अंक क्या है?
 $943268 \times 147347 \times 9164 \times 3285 \times 1139$
(a) 5 (b) 0
(c) 6 (d) 8
30. What is the ten's digit in 7^{400} ?
 7^{400} में दहाई का अंक क्या है?
(a) 1 (b) 0
(c) 2 (d) 9
31. If a and b are positive integers and $x = 4^a$ and $y = 9^b$, which of the following is a possible unit digit of xy ?
यदि a और b धनात्मक पूर्णांक हैं और $x = 4^a$ और $y = 9^b$, तो निम्नलिखित में से कौन सा xy का संभावित इकाई अंक है?
(a) 1 (b) 4
(c) 8 (d) 7
32. Find unit digit of $1!^{100!} + 2!^{99!} + 3!^{98!} + \dots + 100!^{1!}$ का इकाई का अंक क्या है?
(a) 6 (b) 4
(c) 9 (d) 7
33. Find the unit digit in the expression:
 $(1!)^{100!} + (2!)^{99!} + (3!)^{98!} + \dots + 100!^{1!}$
व्यंजक में इकाई अंक ज्ञात कीजिए:
 $(1!)^{100!} + (2!)^{99!} + (3!)^{98!} + \dots + 100!^{1!}$
(a) 3 (b) 9
(c) 6 (d) 5

34. What is the unit digit of इकाई अंक ज्ञात कीजिए:
 $1.(1!)^{1!} + 2.(2!)^{2!} + 3.(3!)^{3!} + \dots + 101.(101!)^{101!}$
 (c) 6 (d) 2
 (c) 0 (d) 1

35. Find the unit digit of $4^{198!} + 6^{12345!} + 348^{66!} + 24^{11!} + 1$.
 $4^{198!} + 6^{12345!} + 348^{66!} + 24^{11!} + 1$ का इकाई अंक ज्ञात कीजिए।
 (a) 3 (b) 2
 (c) 1 (d) 0

36. What is the right most integer of the expression $6577^{6759} + 5469^{7467} + 6577^{6759} + 5469^{7467}$?
 व्यंजक का सबसे दाहिना पूर्णांक क्या है।
 $6577^{6759} + 5469^{7467} + 6577^{6759} + 5469^{7467}$
 (a) 4 (b) 6
 (c) 9 (d) 0

37. The unit digit in the sum of $(124)^{372} + (124)^{373}$ is.
 $(124)^{372} + (124)^{373}$ के योग में इकाई अंक है।
 (a) 5 (b) 4
 (c) 20 (d) 0

38. What is the unit digit $217^{413} \times 819^{547} \times 414^{624} \times 342^{812}$?
 इकाई का अंक $217^{413} \times 819^{547} \times 414^{624} \times 342^{812}$ क्या है।
 (a) 2 (b) 4
 (c) 6 (d) 8

39. The unit digit in the sum of $(124)^{372} + (124)^{373}$ is.
 इकाई का अंक $(124)^{372} + (124)^{373}$ क्या है।
 (a) 5 (b) 4
 (c) 2 (d) 0

40. What is the unit digit in the product $(3547)^{153} \times (251)^{72}$?
 इकाई का अंक $(3547)^{153} \times (251)^{72}$ क्या है।
 (a) 5 (b) 6
 (c) 7 (d) 1

Answer Key

1.(b)	2.(c)	3.(d)	4.(a)	5.(a)	6.(b)	7.(c)	8.(d)	9.(c)	10.(b)
11.(c)	12.(d)	13.(a)	14.(b)	15.(a)	16.(b)	17.(b)	18.(d)	19.(a)	20.(a)
21.(b)	22.(b)	23.(a)	24.(c)	25.(c)	26.(b)	27.(a)	28.(d)	29.(c)	30.(b)
31.(b)	32.(d)	33.(b)	34.(d)	35.(c)	36.(a)	37.(d)	38.(c)	39.(d)	40.(c)

SOLUTIONS

1. (b)

\therefore unit digit of $(0,5,6,1)^n$ is same
 \Rightarrow unit digit of $(6736)^{32567}$ is 6.

2. (c)

$$\begin{aligned} & (23)^{21} \times (24)^{22} \times (26)^{23} \times (27)^{24} \times (25)^{25} \\ & = 3^1 \times 4^2 \times 6 \times 7^4 \times 5 \\ & = 3 \times 6 \times 6 \times 1 \times 5 \\ & = 0 \end{aligned}$$

3. (d)

$$\begin{aligned} & (235)^{215} + (314)^{326} + (6736)^{213} + (3167)^{112} \\ & = 5 + 4^2 + 6 + 7^4 \\ & = 5 + 6 + 6 + 1 = 8 \end{aligned}$$

4. (a)

$$\begin{aligned} & \frac{12^{55}}{3^{11}} + \frac{8^{48}}{16^{18}} \\ & = \frac{3^{55} \cdot 4^{55}}{3^{11}} + \frac{2^{144}}{2^{72}} \\ & = 3^{44} \cdot 4^{55} + 2^{72} \\ & = 3^4 \cdot 4^3 + 2^4 \\ & = 1 \times 4 + 6 \\ & = 0 \end{aligned}$$

5. (a)

$$\begin{aligned} & 7^{95} - 3^{58} \\ & = 7^3 - 3^2 \\ & = 3 - 9 = 4 \end{aligned}$$

6. (b)

$$\begin{aligned} & 17^{1999} + 11^{1999} - 7^{1999} \\ & = 7^3 + 1 - 7^3 \\ & = 3 + 1 - 3 = 1 \end{aligned}$$

7. (c)

$$\begin{aligned} & 1! + 2! + 3! + 4! + 5! + \dots + 3333! \\ & 5! \text{ onwards unit digit will zero.} \\ & \text{unit digit} = 1 + 2 + 6 + 4 + 0 + 0 \dots \\ & = 3 \end{aligned}$$

8. (d)

111!

Since, any factorial number greater than or equal to 5! has zero at unit's place.
 \Rightarrow '0' is the required answer.

9. (c)

$$\begin{aligned} & (888)^{92351} + (222)^{92351} + (666)^{23591} + (9999)^{99991} \\ & = 8^4 + 2^4 + 6^4 + 9^4 \text{ [factorials are multiple of 4]} \\ & = 6 + 6 + 6 + 1 \\ & = 9 \end{aligned}$$

10. (b)

Square root of 15876 is 126

 \Rightarrow unit digit 6

'OR'

We know,

$4^2 = 16$

$6^2 = 36$

$$\begin{array}{r} 15876 \\ \swarrow \quad \searrow \\ 158 > 12^2 \\ \Rightarrow 124 \text{ or } 126 \end{array}$$

We know, $125^2 = 15625 < 15876$

$\Rightarrow \sqrt{15876} = 126$

 \Rightarrow unit digit is 6.

11. (c)

$1^5 + 2^5 + \dots + 99^5$

$= (1 + 2 + 3 + \dots + 9) + (1 + 2 + 3 + \dots + 9) + \dots 10 \text{ times}$

$\Rightarrow 9 \times \frac{9+1}{2} \times 10 = 450$

 \Rightarrow unit digit = 0

12. (d)

$x = (164)^{169} + (333)^{337} - (727)^{726}$

$\Rightarrow 4^{169} + 3^{337} - 7^{726}$

$\Rightarrow 4^1 + 3^1 - 7^2$

$\Rightarrow 4 + 3 - 9 = 7 - 9 \Rightarrow 17 - 9 = 8$

13. (a)

$$\begin{aligned} & (25^{43} \times 56^{42}) + (456)^{25} + 23^{42} + 76^{23} \\ & = (5 \times 6) + 6 + 9 + 6 \\ & = 30 + 6 + 9 + 6 = 51 \end{aligned}$$

14. (b)

$$\text{Sum} = \frac{n(n+1)}{2}$$

whole numbers = 0, 1, 2, 3, ..., 149

$$\Rightarrow \text{Sum} = 149 \times \frac{150}{2} = 11175$$

15. (a)

$$(1570)^2 + (1571)^2 + (1572)^2 + (1573)^2 \\ = 0 + 1 + 4 + 9 \\ = 14 \Rightarrow \text{unit digit} = 4$$

16. (b)

$$\begin{array}{r} 660 \\ 49 \\ \hline 660 > 25^2 \end{array}$$

$$660 > 25^2 \\ \Rightarrow \sqrt{66049} \text{ is either } 253 \text{ or } 257$$

Consider

$$255^2 = 65025 < 66049$$

\Rightarrow number is 257

\Rightarrow unit digit = 7

17. (b)

Unit place = z

then number $\rightarrow 10x + z$ and ten's digit is 8

$$\Rightarrow x = 8$$

\therefore it is of the form $80 + z$

18. (d)

Consider, $(433 \times 456 \times 43N)$ in $433 \times 456 \rightarrow$ unit digit is '8'So, unit digit of $(8 \times 43N)$ is 'N'

According to Question

Unit digit of $8N$ is $N + 2$

$$\Rightarrow N = 6 \text{ satisfies.}$$

19. (a)

Unit Digit = $7^{95} - 3^{58}$

$$7^3 - 3^2$$

$$3 - 9 = -6$$

Unit Digit = 4

20. (a)

All numbers starting with 5! will end in zero.

\therefore unit digit of $1! + 2! + 3! + \dots + 100!$ is same as unit digit of $1! + 2! + 3! + 4! = 1 + 2 + 6 + 24 = 33$.

$$\Rightarrow \text{unit digit} = 3$$

21. (b)

Unit digit of $4^{56+8+9+10}$ Consider, the power of 4 \Rightarrow since it is completely divisible by 2

$$\Rightarrow 4^{\text{even}} \Rightarrow \text{unit digit} = 6$$

\Rightarrow Here unit digit = 6.

22. (b)

$$973^{234!} \times 234^{973!}$$

$$\text{unit digit} = 3^4 \times 4^4 \quad \frac{234!}{4} = \text{Remainder } 0$$

$$1 \times 6 = 6 \quad \frac{973!}{4} = \text{Remainder } 0$$

23. (a)

We know, (even)^{even/odd} = even.

$$(32)^{37^{38}} \Rightarrow \text{even}$$

\Rightarrow even unit digit
from options only option (a) is even.

24. (c)

$$(36)^{234} (33^{512}) (39^{180}) - (54)^{29} (25^{123}) (31^{512})$$

$$\Rightarrow 6 \times 3^0 \times 1 - 4 \times 5 \times 1$$

$$\Rightarrow 6 - 0 = 6$$

25. (c)

$$31^2 + 32^2 + 33^2 + 34^2 + 35^2 + 36^2 + 37^2 + 38^2 + 39^2 \\ = 1 + 4 + 9 + 6 + 5 + 6 + 9 + 4 + 1 \\ = 45$$

$$\Rightarrow \text{unit digit} = 5$$

26. (b)

$$29^{42!} + 44^{21!}$$

$$\Rightarrow 9^4 + 4^4 = 1 + 6 = 7$$

27. (a)

$$5555^{2345} + 6666^{5678}$$

$$\Rightarrow 5 + 6 = 11 \Rightarrow \text{unit digit} = 1$$

28. (d)

$$(24)^{2x+1} \times (33)^{x+1} \times (17)^{x+2} \times (9)^{2x}$$

$$= 4^1 \times 3^{x+1} \times 7^{x+2} \times 1 = 4 \times (3 \times 7)^{x+1} \cdot 7 \times 1 = 4 \times (21)^{x+1} \times 7 = 4 \times 1 \times 7 = 28$$

29. (c)

for ten's digit divide given expression by 100,
the remainder will be ten's digit

$$\Rightarrow \frac{943268 \times 147347 \times 9164 \times 3285 \times 1139}{100}$$

$$= \frac{943268 \times 147347 \times 2291 \times 657 \times 1139}{5}$$

$$= \frac{3 \times 2 \times 1 \times 2 \times 4}{5} = \frac{3}{5} \times \frac{20}{20} = \frac{60}{100}$$

$\Rightarrow 60$ is remainder \Rightarrow ten's digit = 6

30. (b)

Divide 7^{400} by 100

$$\Rightarrow \frac{7^{400}}{100} = \frac{(7^4)^{100}}{100} = \frac{(2401)^{100}}{100} = \frac{01}{100}$$

 \Rightarrow tens digit = '0'.

31. (b)

$x = 4^a, y = 9^b$

unit digit of $x = 4$ or 6unit digit of $y = 9$ or 1 \therefore possibilities are:-

$4 \times 1 = 4$

$4 \times 9 = 6$

$6 \times 9 = 4$

$6 \times 1 = 6$

The unit digits of xy will be 4 or 6 \therefore by options, (B) is correct.

32. (d)

Unit digit of $n!^{n!}$ for $n! \geq 5!$ is zero.

Now consider:

1! 2! 3! 4!

1! + 2! + 3! + 4! + ...

$= 1^1 + 2^2 + 6^6 + 24^{24} + 0 \dots$

$= 1 + 4 + 6 + 6 = 7$ unit digit

33. (b)

$(1!)^{100!} + (2!)^{99!} + (3!)^{98!} + \dots \dots \dots (99!)^{1!}$

$1^{100!} + 2^{99!} + 6^{98!} + 24^{97!} + (120)^{96!} + \dots \dots \dots$

$$\begin{array}{c} \boxed{} \\ \downarrow \end{array}$$

unit digit = 0

unit digit = $1 + 2^4 + 6^4 + 4^4 + 0$

$= 1 + 6 + 6 + 6$

$= 9$

34. (d)

$1.(1!)^{1!} + 2.(2!)^{1!} + 3.(3!)^{1!} + \dots \dots \dots + 101.(101!)^{101!}$

5! onwards unit digit will zero.

unit digit $1 \times 1 + 2 \times (2)^2 + 3 \times (6)^6 + 4 \times (24)^4$

$1 + 8 + 8 + 4$

$= 1$

35. (c)

Consider,

$4^{198} + 6^{12345} + 348^{66} + 24^{11} + 1$

We know,

$\Rightarrow \frac{198}{2} = 0, \frac{12345}{2} = 1$

$\frac{66}{4} = 2, \frac{11}{2} = 1$

 \therefore Unit digits:

$= 6 + 6 + 4 + 4 + 1$

$= 1$

36. (a)

$6577^{6759} + 5469^{7467} + 6577^{6759} + 5469^{7467}$

$\frac{6759}{4} = 3$ Remainder

$\frac{7467}{4} = 3$

Unit digit = $7^3 + 9^3 + 7^3 + 9^3$

$= 3 + 9 + 3 + 9$

$= 4$

37. (d)

$124^{372} + 124^{373}$

$\Rightarrow 124^{372} [1 + 124]$

$\Rightarrow 127^{372} [125]$

Even no. \times multiple of 5 = unit digit '0' \Rightarrow '0' is the unit digit.

38. (c)

$217^{413} \times 819^{547} \times 414^{624} \times 342^{812}$

$\frac{413}{4} = 1, \frac{547}{2} = 1, \frac{624}{2} = 0, \frac{812}{4} = 0$

 \therefore Unit's digits are:-

$\Rightarrow 9 \times 9 \times 6 \times 6$

$\Rightarrow 6$

39. (d)

$(124)^{372} + (124)^{373}$

Unit digit = $(4)^4 + (4)^1$

$= 6 + 4 = 0$

40. (c)

$(3547)^{153} + (251)^{72}$

Unit digit = $7^1 \times 1^4$

$= 7 \times 1 = 7$