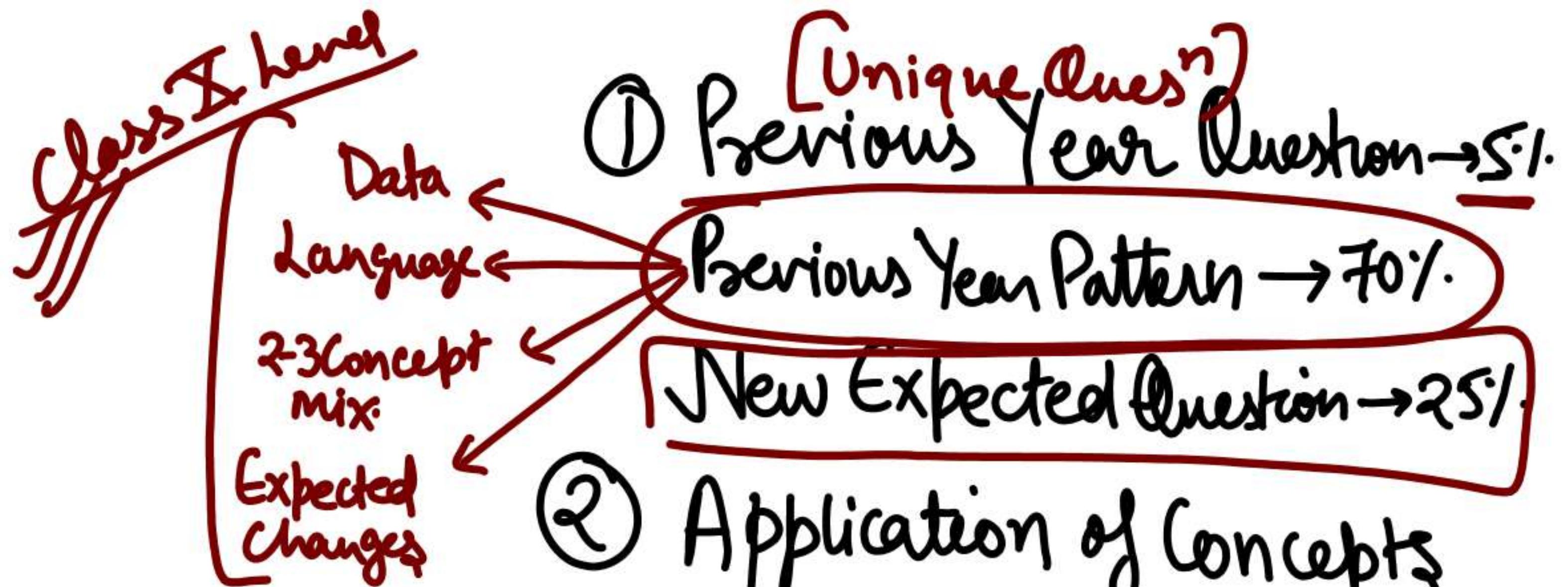


MAINS SPECIAL BATCH

CGL 2022

Only प्र०१८

For Serious Students



तिक्ते उपाय | Importance

MAINS ORIENTED CONTENT ONLY

ALGEBRA
MAINS SPECIAL

①

$$a+2022 = \frac{1}{2022}$$

$\frac{1}{a+2022} = 2022$, $\frac{1}{a+2023} = ?$

(a) $\frac{2023}{2022}$ (b) $-\frac{2002}{2023}$

$$a+2023 = \frac{1}{2022} + 1$$

$$= \frac{2023}{2022}$$

$$a+2023 = \frac{2022}{2023}$$

②

$$\frac{2022}{2023}$$

③

$$(d) \frac{2021}{2022}$$

$$x = \frac{1}{2022}$$

$$x+1 = \frac{2023}{2022}$$

{

$$x + \frac{1}{x} + 4 = 7$$

$$x + \frac{1}{x} = 3$$

$$\underbrace{x^2 + \frac{1}{x^2}}_{=} + 16 = 7 + 16$$

$$= 23$$

$$f\left(x + \frac{1}{x} + 4\right) = x^2 + \frac{1}{x^2} + 16$$

$$f(7) = ?$$

(a) 17

(b) 25

(c) 23

(d) 47

© ans

$$2(27+45)$$

$$144$$

$$\sqrt{144} = 12$$

(B)

Find the square root of

$$(3 + \sqrt{5})^3 + (3 - \sqrt{5})^3.$$

(a) 9

~~(b)~~ 12

(c) 14

(d) 6

Trending Formula

$$(a+b)^3 + (a-b)^3 = 2(a^3 + 3ab^2)$$

$$(a+b)^3 - (a-b)^3 = 2(b^3 + 3ba^2)$$

If ~~$18x + 3y = 36$~~ , $\frac{xy}{12} = 3$ then find the value of $216x^3 + y^3 + 2x^3y^3$.

$$6x+y=12$$

$$xy=3$$

- (a) 1134 (b) 1156
(c) 1206 (d) 1210

$$12^3 = ?? + 18 \times 3(12)$$

$$\begin{array}{r} 1728 \\ -648 \\ \hline 1080 \end{array}$$

$$1080$$

$$1080 + 2 \times 27$$

$$1134$$

A

Creation
करा
दुआ॥

$$1+2+3+4=5x$$

$$x=2$$

$$4x^2$$

$$4 \times 4 = 16 \text{ (B)}$$

$$a, b, c, d > 0$$

$$4x^2 = ?$$

$$(a) 4$$

$$(c) 32$$

$$(b) 16$$

$$(d) 12$$

$$\frac{1}{a+1} + \frac{2}{b+1} + \frac{3}{c+1} + \frac{4}{d+1} = x$$

$$\frac{a}{a+1} + \frac{2b}{b+1} + \frac{3c}{c+1} + \frac{4d}{d+1} = 4x$$

$$\frac{a+1}{a+1} + \frac{2(b+1)}{b+1} +$$

$$\frac{3(c+1)}{c+1} +$$

$$\frac{4(d+1)}{d+1} = 5$$

Value Pnt

$a + b = 5, \underline{a^3 + 15ab + b^3} = ?$

(a) 125 (b) 140 $\underline{-a, b \neq 0}$

(c) 135 (d) 115

$$5^3 = \underline{a^3 + b^3 + 3ab(5)}$$

$$125 = a^3 + b^3 + 15ab$$

① Change

Māmūlī Ques.

Ⓐ

② $a + b = \frac{5}{3}$

$\frac{125}{27}$

$a^3 + b^3 + 3 \cdot 6ab = ??$

$a^3 + b^3 + 5ab = ??$

1.728

$$3x + \frac{1}{2x} = \sqrt{3}, \quad 6x^2 + \frac{1}{6x^2} = ?$$

$$\left(\frac{3x+1}{2x}\right)\left(\frac{2x+1}{3x}\right)$$

(a) 1

(b) 0

(c) 2

(d) None

$$\frac{6x^2+1+1}{6x^2} = x$$

$$\frac{6x^2+1}{6x^2} = 0$$

$$\frac{2x+1}{3x} = \frac{2\sqrt{3}}{3}$$

③

$x + \frac{1}{x} = 4$, $x^3 = A + B\sqrt{3}$ then find the

value of AB

$$\frac{x-1}{x} = \sqrt{12}$$

$$\frac{x}{x} = 2\sqrt{3}$$

$$x = \frac{4+2\sqrt{3}}{2}$$

$$x = 2+\sqrt{3}$$

~~(a) 390~~

(c) 333

(b) 430

(d) None

$$(2+\sqrt{3})^3 = 8 + 3\sqrt{3} + 12\sqrt{3} + 18$$

$$= 26 + 15\sqrt{3}$$

A

$$26 \times 15 = 390$$

$$3^x = k$$

$$3 = k^{\frac{1}{x}}$$

$$y = k^{\frac{1}{y}}$$

$$12 = k^{-1}z$$

$$k^{\frac{1}{x} + \frac{1}{y}} = k^{\frac{1}{z}}$$

$$\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 0$$

One step.

If $3^x = 4^y = 12^{-z}$ then find the value
of $(x^{-3} + y^{-3} + z^{-3})$

(a) $3xy^{-1}z^{-1}$ (b) $3x^{-1}y^{-1}z^{-1}$

(c) $x^{-1}y^{-1}z^{-1}$ (d) $3x^{-3}y^{-3}z^3$

Attention
Seeker

B

$$\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 0$$

$$\frac{1}{x^3} + \frac{1}{y^3} + \frac{1}{z^3} = \frac{3}{xyz}$$

$$\frac{1}{x} + \frac{1}{y} = -\frac{1}{z}$$

$$x^3 + y^3 = 3xyz + 8, \underline{x + y + z = 0}$$

$$xz + yz = ?$$

$\underline{-z}$

(a) 2

(b) 4

(d) 1

$$x+y+z=0 \quad \cancel{x+y} -4$$

$$x^3 + y^3 - 8 = 3xyz$$

$$z^3 = -8$$

$$\boxed{z = -2}$$

$$z(x+y)$$

$$-z^2$$

$$= -4 \text{ Ans } \textcircled{c}$$

$$\frac{4}{4x+\frac{7}{x}-8} + \frac{3}{4x+\frac{7}{x}-10} = \frac{4x}{4x^2 - 8x + 7} + \frac{3x}{4x^2 - 10x + 7} = 1$$

$4x + \frac{7}{x}$ could be

$$\boxed{\frac{4}{x-8} + \frac{3}{x-10} = 1}$$

(a) 9
(c) 6

- (b) 7
(d) 5

option

$4-3=1$ (A) ✓

$$xyz = \frac{(x+y+z)}{\cancel{x}} \cdot \frac{1}{x}$$

$$\frac{1}{x+y+z} + \frac{1}{x} + \frac{1}{y} + \frac{1}{z} \text{ then } x^3 + y^3 + z^3 =$$

?

- (a) $3xyz$
- (b) $(x+y+z)^3$
- (c) $-3xyz$
- (d) $-(x+y+z)^3$

B

$$\begin{aligned}
 & \cancel{x^3 + y^3 + z^3 - 3xyz} = (x+y+z) \left((x+y+z)^2 - 3(xy+yz+zx) \right) \\
 & = (x+y+z)^3 - 3(x+y+z) \cancel{(xy+yz+zx)} - 3\cancel{xyz}
 \end{aligned}$$

$a + b = 1, a^2 + b^2 = 2, a^8 + b^8 = ?$

$$ab = -\frac{1}{2}$$

$$a^4 + b^4 = 4 - 2\left(\frac{1}{4}\right)$$

$$= \frac{7}{2}$$

$$a^8 + b^8 = \frac{49}{4} - 2\left(\frac{1}{168}\right)$$

$$= \frac{97}{8} \text{ (B)}$$

(a) $\frac{7}{2}$

(c) $\frac{87}{8}$

(b) $\frac{97}{8}$

(d) $\frac{15}{8}$

~~निर्णय दर्शक~~
~~नियम उत्तर~~
गोली उत्तर

$$x^2 + x + 1 = 0$$

$$\left(x + \frac{1}{x}\right)^2 + \left(x^2 + \frac{1}{x^2}\right)^2 + \left(x^3 + \frac{1}{x^3}\right)^2 + \dots \left(x^{27} + \frac{1}{x^{27}}\right)^2$$

$\overbrace{\qquad\qquad\qquad}$

$x + \frac{1}{x} = -1$

$= ?$ terms

$$x^2 + \frac{1}{x^2} = -1$$

(a) 54 (b) 36

$$x^3 + \frac{1}{x^3} = -1 + 3 = 2$$

(c) 18 (d) 45 1, 2,

$$\begin{aligned} & (-1)^2 \times 9 \\ & (-1)^2 \times 9 \\ & \underline{2^2 \times 9} \end{aligned}$$

54 Ans

$$x^2 + xy = 28, y^2 + xy = 21, xy = ?$$

- (a) 12 (b) 10
(c) 20 (d) -12

कागज करते
वाले Ques

$$(x+y)^2 = 49$$

$$x^2 - y^2 = 7$$

$$x+y = 7$$

$$\cancel{(x+y)}(x-y) = 7$$

$$x+y = 7$$

$$\cancel{x-y} = 1$$

$$4 \times 3 = 12$$

$$x^2 = 17x + y, y^2 = x + 17y, x \neq y$$

$$x^2 + y^2 = 18(x + y)$$

$$\sqrt{x^2 + y^2 + 1} = ?$$

$$x^2 - y^2 = 16(x - y)$$

(a) 13

(b) 26

$$(x+y)(x-y) = 16(x-y)$$

(c) 17

(d) 19

$$\sqrt{18x16+1}$$
$$\sqrt{289} = 17 \textcircled{C}$$

Add
Sub.

Find the coefficient of xy^{-4} in the expression $(\sqrt{3}y^{-2} + 2x)^3$.

~~(a) 18~~

(b) 16

(c) $18\sqrt{3}$

(d) $16\sqrt{3}$

A

$3 \times 3 \times 2$

If ~~$(4x + 3y)^3 - (4x - 3y)^3 = my^3 + 288x^2y$~~ ,
then $m = ?$

①

$$2(b^3 + 3ba^2)$$

$$2(27y^3 + 144x^2y)$$

$$54y^3 + 288x^2y$$

C

(a) 16

(c) 54

(b) 13

(d) 42

② केवल y^3

$$\frac{2(27y^3)}{54}$$

③ $x=0$
 $y=1$
 $54=m$

C

Coefficients
of same terms
are equal

If $(2x-3)^2 + (2y - 5)^2 + (6z-24)^2 = 0$
then find the value of $x^3 + y^3 - z^3 = ?$

- (a) 0
(c) -45

- (b) -1
(d) 40

② $x+y-z=0$

① $\left(\frac{3}{2}\right)^3 + \left(\frac{5}{2}\right)^3 - 4^3$

~~$-3 \times \frac{3}{2} \times \frac{5}{2} \times 4 = -45$~~ C

$$\sqrt{2}x = -1$$

$$\sqrt{3}y = -2$$

$$2z = -3$$

If $(2x^2 + 10) + (3y^2 + 3) + (4z^2 + 1) = -2(\sqrt{2}x + 2\sqrt{3}y + 6z)$ then the value of $z^2 - x^2 - y^2$ = ? (approx.)

- (a) 0.41 ~~(b) 0.42~~
(c) 0.43 (d) 0.44

$$\frac{9}{4} - \frac{1}{2} - \frac{4}{3} = \frac{5}{12}$$
 B

$$\frac{1}{12} = 8\frac{1}{3}\%$$

$$\frac{5}{12} = 41\frac{2}{3}\%$$

• 4166

$$a-b+c = \sqrt{6}$$

$$a^3 + c^3 - b^3 = -3abc$$

If $a - b + c = \sqrt{6}$ and $a^3 + 3abc = b^3 - c^3$ find the value of $a(a+b) + b(b+c) + c(c-a) = ?$

$$a-b+c \neq 0$$

$$a-b+c \neq 0$$

$$a-b+c \neq 0$$

(b) 1

(d) None

Correct

$$\cancel{a^3 - b^3 + c^3 + 3abc} = (\cancel{a-b+c})(a(a+b) + b(b+c) + (c-a))$$

A

Question
Basic

$$a^3 + b^3 + c^3 - 3abc = (a+b+c)(a(a-b) +$$

$b(b-c) + c(c-a)$

$$a^3 + b^3 + c^3 + 3abc = (a-b+c)(a(a+b) + b(b+c) + c(c-a))$$

$b(b-c)$

$-b(-b-c) = b(b+c)$

\times

\checkmark

$a=b=c$

$a(a+b) + b(b+c) + c(c-a)$

If $x - x^{-1} = x^o$ then find the value of

$$x - \frac{1}{x} = 1$$

$$x + \frac{1}{x} = \sqrt{5}$$

$$x = \frac{\sqrt{5} + 1}{2}$$

$$\frac{1}{x} = \frac{\sqrt{5} - 1}{2}$$

$$x^2 - \frac{1}{x}$$

(a) 4

(c) 2

(b) $2\sqrt{5}$

(d) None of these

$$\begin{aligned} & \frac{6+2\sqrt{5}}{4} - \frac{\sqrt{5}-1}{2} \\ &= \frac{6+2}{4} = \frac{2}{2} \text{ C} \end{aligned}$$

If $x^4(x-4) = x^8$ then find the value of

$$x(x-4)=1$$

$$\left(\frac{x-1}{x}\right)^2 = 4$$

$$\left(\frac{x+1}{x}\right)^2 = 25$$

$$\frac{(x^6 + 1)}{(x^4 + \sqrt{5}x^3 + x^2)} = ?$$

÷ x^8 (a) $\frac{34}{3}$

(c) $\frac{34}{5}$

(b) $\frac{31}{3}$

(d) None

$$\frac{x^3 + 1}{x^8} = \frac{25\sqrt{5}(17)}{3\sqrt{5}} = \frac{34}{3} \textcircled{A}$$

$$\frac{n^3 - 3^n}{n(n^2 - 3)}$$

$$y^2 = xz$$

If $z = y^2 x^{-1}$, $x + y + z = 8$ and $x^2 + y^2 + z^2 = 16$ then find the value of $y^2 =$

$$8^2 = 16 + 2(xy + yz + zx)$$

$$\text{? } y^2$$

$$3 \cancel{xy} = 2y(x)$$

(a) 24

(c) 17

(b) 16

(d) 9

$$y=3$$

$$y=9$$

D

Important

$$\begin{aligned}y^2 &= xz \\x^{-1}z^{-1} &= y^{-2}\end{aligned}$$

टेलग्राम
सेक्युरिटी

$$x = \frac{\sqrt{3}-1}{2}$$

$$y = \frac{\sqrt{3}+1}{2}$$

$$xy = \frac{1}{2}$$

$$x+y = \sqrt{3}$$

$$(\sqrt{3})^3 = ?? + \frac{3}{2}(\sqrt{3})$$

$\sqrt{2}x = \sqrt{2-\sqrt{3}}$ and $\sqrt{2}y = \sqrt{2+\sqrt{3}}$ find

the value of (x^3+y^3) of $\frac{2}{3}$

(a) $\frac{\sqrt{3}}{2}$

(c) $\sqrt{3}$

(b) $\frac{1}{2}$

(d) $\sqrt{2}$

$$\sqrt{2-\sqrt{3}}$$

$$= \frac{\sqrt{3}-1}{\sqrt{2}}$$

$$?? = \frac{3\sqrt{3}}{2}$$

$$\textcircled{C} \frac{\frac{3\sqrt{3}}{2} \times 2}{8} \sqrt{3}$$

If $a^2 + b^2 - ab\sqrt{2} = 5.25$, $a^4 + b^4 = \frac{273}{16}$

$$\underline{a^2+b^2+ab\sqrt{2}} = \frac{273}{16} \div \frac{21}{4} = \frac{273}{16} \times \frac{4}{21} = \frac{21}{4}$$

~~then~~ find the value of $\frac{1}{(a-b)^2} = ?$

$$a^2 + b^2 = \frac{17}{4}$$

$$\sqrt{2} = 1.4$$

$$ab\sqrt{2} = -1$$

(a) 6.55

(b) 5.65

$$(a-b)^2 = a^2 + b^2 - 2ab$$

$$\rightarrow 2ab = -\sqrt{2}$$

(c) 5.29

(d) 5.45

$$\frac{17}{4} + \sqrt{2}$$

① Deemed
Q. Ans

$$4.25 + 1.4 = 5.65$$

(B) $a^4 + b^4 = (a^2 + b^2 - ab\sqrt{2})(a^2 + b^2 + ab\sqrt{2})$

If $x^2(x^2 - \sqrt{7}) = -1$ and

$$x^2 + \frac{1}{x^2} = \sqrt{7}$$

$x^6(x^6 - A\sqrt{B}) = -1$ then find the value

of $A + B = ?$

$$x^6 + \frac{1}{x^6} = A\sqrt{B}$$

(a) 28

(b) 11

(c) $4 + \sqrt{7}$

(d) $\sqrt{7} + 7$

$$\underbrace{7\sqrt{7}-3\sqrt{7}}$$

$$4\sqrt{7}$$

$$\begin{array}{cc} A & B \\ \downarrow & \downarrow \\ 4+7 & \infty \\ \textcircled{B} & \end{array}$$

$$\frac{(A^3x^3 - B^3y^3)}{(16x^2 + ABxy + 25y^2)} = (Ax - By) \text{ then}$$

the value of $(A + B)^2 = ?$

(a) 64

(c) 36

~~(b)~~ ^(c)+5) 81

(d) None

Simple Ones

If $a + b = 2\frac{2}{5}$ and $a^2 + b^2 = 3\frac{3}{50}$ then

the value of $8a - 10b = ? \quad a > b$

(a) 6

(c) 3.0

(b) 4.7

(d) 7.3

$a - b \checkmark$

$\begin{array}{r} a \\ b \\ \hline 1.5 \\ 0.9 \end{array}$

$a + b = 2.4 \checkmark$

$5.76 = 3.06 + 2ab$

$ab = 1.35 \checkmark$

$\begin{array}{r} a^2 + b^2 = 3.06 \\ 12 - 9 \\ = 3 @ \end{array}$

If $x^2(x^2+1) = 728$ and $\underline{x^2 - x + 1} = 9$
then find the value of 3.33% of
 $x^4 + x^2 = 728$ (x²+1).

↓

x⁴ + x² + 1 = 729

(a) $\frac{4}{5}$ (b) $\frac{4}{3}$

(c) $\frac{3}{2}$ (d) $\frac{2}{3}$

81 + 9 × 1
2 30 729

Interest
Overs

⑥

$(x^4 + x^2 + 1) = (x^2 + x + 1)(x^2 - x + 1)$

Y/N ✓

If $(3x+2y)^3 - (2x+3y)^3 = M(x^3-y^3) + Nxy(x-y)$
(x-y) then find the value of $(M-N) = ?$

- ~~(a)~~ 1 (b) 7
(c) 4 (d) 8

$$27x^3 + 8y^3 + 18xy(3x+2y) - 8x^3 - 27y^3 - 18xy(2x+3y)$$

$$19(x^3 - y^3) + 18xy(x-y)$$

$\downarrow M$ $\downarrow N$

A