

MAINS SPECIAL ALGEBRA

Next Class
Monday

① If $x^2 + y^2 + z^2 = 198x + 202y + 200$
 $z - 30002$, then $x^3 + y^3 + z^3 - 3xyz$ equal
 to

- (a) 80
 (c) 100

- (b) 900
 (d) 950

$$\frac{1}{2}[(x-y)^2 + (y-z)^2 + (z-x)^2] = 3$$

$n, n+1, n+2$

$$\frac{300}{2} \left(\frac{3}{6} \right)$$

(B)

② If $a - \frac{1}{a} = 5\sqrt{3}$ & $a^4 - Xa^2 + 1 = 0$ and $\underbrace{a^2 + \frac{1}{a^2}}_{=77} = X = \frac{n^2+2}{=77}$

$a^3 - \frac{1}{a^3} = Y$ then $Y - X$ equals to.

(a) $390\sqrt{3} - 77$ $5\sqrt{3}(78)$ $390\sqrt{3}$

(b) $380\sqrt{3} - 70$

(c) $390\sqrt{3} + 77$

(d) $395\sqrt{3} - 70$

$390\sqrt{3} - 77$

Ⓐ

③ $(x+a)(x+b)(x+c) = x^3 - 8x^2 + 75x + 25$, then

$\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = ?$

a, b, c roots

(a) 1

(b) 2

(c) -3

(d) 4

$$\frac{ab+bc+ca}{abc}$$

$$\frac{\frac{75}{1}}{-25} = -3$$

©

$$\begin{aligned} \alpha + \beta + \gamma &= -b \\ \alpha\beta\gamma &= -\frac{d}{a} \\ \alpha\beta + \beta\gamma + \gamma\alpha &= \frac{c}{a} \end{aligned}$$

④

$$x + 25x^{-1} = 15\sqrt{2}, \frac{x^2}{5} + \frac{125}{x^2} = ?$$

(a) 26

(c) 40

(b) 90

☒ (d) 80

$$x + \frac{25}{x} = 15\sqrt{2}$$

$$\frac{1}{5} [450 - 50] = 80$$

$$\frac{1}{5} \left[x^2 + \frac{625}{x^2} \right]$$

①

⑤

If $\frac{a}{bc} = \frac{1}{ac} + \frac{1}{ab}$, $\frac{b}{ac} = \frac{1}{ab} + \frac{1}{bc}$, $\frac{c}{ab} = \frac{1}{bc} + \frac{1}{ac}$

$\frac{a}{bc} = \frac{b+c}{abc}$

then $\left(\frac{a-1}{a^2-1} \right) + \left(\frac{b-1}{b^2-1} \right) + \left(\frac{c-1}{c^2-1} \right) = ?$

(a) 2

✓ (b) 1

(c) 0

(d) 3

③

$\frac{1}{a+1} + \frac{1}{b+1} + \frac{1}{c+1}$

$\frac{c}{a+b+c} + \frac{b}{a+b+c} + \frac{a}{a+b+c}$

$\frac{1}{\frac{a+b+c}{a}}$

⑥

If $a + x^2 = 2006$, $b + x^2 = 2007$ and $c + x^2 = 2008$, $abc = 3$. Find the value of

$$\frac{a}{bc} + \frac{b}{ca} + \frac{c}{ab} - \frac{1}{a} - \frac{1}{b} - \frac{1}{c}$$

यदि $a + x^2 = 2006$, $b + x^2 = 2007$ तथा $c + x^2 = 2008$, तथा $abc = 3$. तो

$$\frac{a^2 + b^2 + c^2 - bc - cb - ca}{abc}$$

$$abc$$

$$\frac{(a-b)^2 + (b-c)^2 + (c-a)^2}{2abc}$$

$$2abc$$

$$\frac{3}{3} = 1 \quad \text{① A}$$

$$\frac{a}{bc} + \frac{b}{ca} + \frac{c}{ab} - \frac{1}{a} - \frac{1}{b} - \frac{1}{c} \text{ का मान होगा।}$$

(a) 1

(b) 2

(c) 1/2

(d) None of these

a, b, c लगातार No. है

$$\begin{aligned}x &= 1.278 \\ y &= 2.278 \\ z &= 3.278\end{aligned}$$

$$\begin{aligned}x &= \frac{5}{4} \\ y &= \frac{9}{4} \\ z &= \frac{13}{4}\end{aligned}$$

$$\frac{(x-y)^2 + (y-z)^2 + (z-x)^2}{2} = 3$$

$$\frac{1^2 + 1^2 + 2^2}{2} = 3$$

7

If $a^2 + 2b = 7$, $b^2 + 4c = -7$, $c^2 + \underline{6a} = -14$,
 $(a^2 + b^2 + c^2)$ then the value is.

यदि $a^2 + 2b = 7$, $b^2 + 4c = -7$, $c^2 + 6a = -14$

$(-3)^2 + (-1)^2 + (2)^2$ $(a^2 + b^2 + c^2)$ तो निम्न का मान बताओं।

~~(a) 14~~

(b) 25

(c) 36

(d) 46

14
A

$\rightarrow a^2 + b^2 + c^2 + 6a + 2b + 4c + 14 = 0 \times$

-3

-1

2

⑧ If a, b, c are real numbers such that

$$\left(a + \frac{1}{b}\right)\left(b + \frac{1}{c}\right)\left(c + \frac{1}{a}\right) = a + \frac{1}{b} = \frac{7}{3}, b + \frac{1}{c} = 4, c + \frac{1}{a} = 1, \text{ find } abc.$$

यदि a, b, c तथा $a + \frac{1}{b} = \frac{7}{3}, b + \frac{1}{c} = 4, c + \frac{1}{a} = 1$ तो $\frac{abc}{abc}$ का मान ज्ञात करें।

$$\frac{7 \times 4 \times 1}{3} = \frac{7}{3} + 5 + x + \frac{1}{x} \quad (a) 2$$

$$2 = x + \frac{1}{x}$$

$$x = 1 \quad abc = 1$$

(c) 1

©

(b) 0

(d) None of these

9

$$\frac{x+y}{yz+zx}$$

$$\frac{x+y}{z(x+y)}$$

$$\frac{1}{z} + \frac{1}{x} + \frac{1}{y}$$

$$\frac{xy+yz+zx}{xyz} = \frac{1}{xyz}$$

D

If $xy + yz + zx = 1$, then the equation

$$\frac{x+y}{1-xy} + \frac{y+z}{1-yz} + \frac{z+x}{1-xz} \text{ is equal to.}$$

यदि $xy + yz + zx = 1$, तो समीकरण का

$$\frac{x+y}{1-xy} + \frac{y+z}{1-yz} + \frac{z+x}{1-xz} \text{ मान होगा।}$$

(a) $\frac{1}{x+y+z}$

(b) xyz

(c) $x+y+z$

(d) $\frac{1}{xyz}$

10

Possible value of x for equation

$$3^{2x^2} - 2 \cdot 3^{x^2+x+2} + 3^{2(x+2)} = 0$$

$$(3^{x^2} - 3^{x+2})^2 = 0$$

$$x^2 = x + 2$$

-1 ✓
2 ✓

(A)

x के संभव मान क्या होंगे यदि समीकरण

$$3^{2x^2} - 2 \cdot 3^{x^2+x+2} + 3^{2(x+2)} = 0$$

✓ (a) (-1, 2)

~~(b) (0, 2)~~

~~(c) (0, -1)~~

~~(d) (2, 4)~~

Option से

-1 ✓ X (A)

⑪

If $3^x + y = 81$, $81^{x-y} = 3$ then x and y are.

यदि $3^x + y = 81$ तथा $81^{x-y} = 3$ हो तो x तथा y के संभव मान ज्ञात करें।

①

$$\begin{aligned} x+y &= 4 \\ x-y &= \frac{1}{4} \end{aligned}$$

①

~~(a)~~ no solution

~~(b)~~ $x = \frac{21}{2}, y = \frac{21}{2}$

~~(c)~~ $x = 2, y = \frac{2}{3}$

✓ ~~(d)~~ $x = \frac{17}{8}, y = \frac{15}{8}$

①

②

$$3(x^2 - y^2) = 3$$

$$(x+y)(x-y) = 1$$

12

If $\sqrt{512}=2^x$, $\sqrt{15625}=5^y$ and $\sqrt{343}=7^z$ then

what will be the value of $x - y + z$.

यदि $\sqrt{512} = 2^x$, $\sqrt{15625} = 5^y$ और $\sqrt{343} = 7^z$ तो $x - y$

+ z का मान होगा

(a) 4

(b) 6

(c) 9

✓ (d) 3

$$\begin{aligned} x &= \frac{9}{2} \\ y &= 3 \\ z &= \frac{3}{2} \end{aligned}$$

3 (D)

$$\begin{aligned} &\sqrt{(25^3)} \\ &\sqrt{5^6} = 5^3 \end{aligned}$$

(13) If $1960 = 2^a \times 5^b \times 7^c$ then find the value of $2^{-a} \times 7^b \times 5^{-c}$.

यदि $1960 = 2^a \times 5^b \times 7^c$ तो $2^{-a} \times 7^b \times 5^{-c}$ का मान बताओं।

$$2^3 \times 5^1 \times 7^2$$

(a) $\frac{175}{8}$

☒ (b) $\frac{7}{200}$

(c) $\frac{7}{2000}$

(d) $\frac{56}{25}$

$$\frac{1 \times 7 \times 1}{8 \times 25} = \frac{7}{200} \quad \text{(B)}$$

14

$$\begin{pmatrix} \alpha & \alpha \\ \beta_1 & \beta_2 \end{pmatrix}$$

$$\frac{\alpha \beta_1}{\alpha \beta_2} = \frac{3}{4}$$

$$\frac{6}{c} = \frac{3}{4}$$

$$c = 8$$

One root of the quadratic equation $x^2 - bx + 6 = 0$ and $x^2 - 6x + c = 0$ is equal.

The ratio of the remaining roots is 3: 4. If all the root are positive integers. Find the value of b and c respectively.

यदि द्विघात समीकरण $x^2 - bx + 6 = 0$ और $x^2 - 6x + c = 0$ के एक मूल समान हो तथा दूसरे मूलों का अनुपात 3: 4 हो तो b तथा c का मान बताओं यदि दिया हो कि सभी मूल घनात्मक पूर्णांक हैं।

(a) 3, 4

(c) 1, 6

✓ (b) 5, 8

(d) 8, 5

(B)

15

If $(x+k)$ is a common factor of (x^2+px+q) and (x^2+lx+m) , then the value of k is:

यदि $(x+k)$, (x^2+px+q) और (x^2+lx+m) समान गुणनखंड है। तो k का मान होगा।

$$\cancel{(x+k)}^2 - pk + q = \cancel{(x+k)}^2 - lk + m$$

$$(l-p)k = m-q$$

$$k = \frac{m-q}{l-p}$$

(a) $u+p$

(b) $m-q$

(c) $\frac{l-p}{m-q}$

☒ (d) $\frac{m-q}{l-p}$

$x = -k$

D

16

① $2x = a + \frac{1}{a}$
 $2y = b + \frac{1}{b}$

$4xy = \left(a + \frac{1}{a}\right)\left(b + \frac{1}{b}\right)$

long
quesn

If $2x = a + a^{-1}$ and $2y = b + b^{-1}$ find the value of $xy + \sqrt{(x^2 - 1)(y^2 - 1)}$.

यदि $2x = a + a^{-1}$ तथा $2y = b + b^{-1}$ तो निम्न का मान बताओ $xy + \sqrt{(x^2 - 1)(y^2 - 1)}$. ②

(a) $\frac{1}{2}(ab + a^{-1}b^{-1})$

(b) $\frac{1}{2}(ab)$

(c) $\frac{1}{2}a$

(d) $\frac{1}{2}b$

$a = b = x = y = 1$

1
A

①

17

$$ab+bc+ca = \frac{0^2-10}{2} = -5$$

$$(a+b+c)^2 = a^2+b^2+c^2 + 2(ab+bc+ca)$$

$$25 = ?? + 2 \times 0$$

$$?? = 25$$

If $a + b + c = 0$, $a^2 + b^2 + c^2 = 10$, then the value of $a^4 + b^4 + c^4$ is

यदि $a + b + c = 0$, $a^2 + b^2 + c^2 = 10$, तो निम्न का मान होगा $a^4 + b^4 + c^4$.

(a) 50

(b) 25

(c) 75

(d) 100

$$(a^2+b^2+c^2)^2 = 2(a^4+b^4+c^4) + 2abc(a+b+c)$$

$$10^2 = 2 \times ?? + 2 \times 0$$

$$100 = 2 \times ??$$

$$?? = 50 \text{ (A)}$$

17

If $a + b + c = 0$, $a^2 + \underline{b^2} + \underline{c^2} = \underline{10}$, then the value of $a^4 + b^4 + c^4$ is

$$a = 0$$

$$b = \sqrt{5}$$

$$c = -\sqrt{5}$$

यदि $a + b + c = 0$, $a^2 + b^2 + c^2 = 10$, तो निम्न का मान होगा $a^4 + b^4 + c^4$.

✓ (a) 50

(b) 25

(c) 75

(d) 100

$$0 + 25 + 25$$

50 (A)

18

$$\frac{1}{y} - \frac{1}{x} = 5$$

$$\frac{1}{y} + \frac{1}{x} = 7$$

$$\frac{1}{y} = 6$$

$$y = \frac{1}{6}$$

If $\frac{x^2 - xy}{x^2 y} = 5$ and $\frac{xy + y^2}{xy^2} = 7$ then the value of y is.

यदि $\frac{x^2 - xy}{x^2 y} = 5$ तथा $\frac{xy + y^2}{xy^2} = 7$ हो तो y का मान

होगा।

(a) 1

(c) $\frac{1}{2}$

☒ (b) $\frac{1}{6}$

(d) $\frac{1}{3}$

(B)

19

If $5^2 \cdot 5^4 \cdot 5^6 \dots 5^{2x} = (0.04)^{-28}$ then value of x is.

यदि $5^2 \cdot 5^4 \cdot 5^6 \dots 5^{2x} = (0.04)^{-28}$ तो x का मान होगा।

(a) 5

(b) 10

(c) 8

(d) 7

$$5^{2+4+6+\dots+2x}$$

$$5^{2(1+2+\dots+x)}$$

$$5^{\frac{2x(x+1)}{2}} = 5^{26}$$

$$x=7$$

D

$$0.04 \rightarrow \frac{4}{100} = \frac{1}{25} = 5^{-2}$$

20

If $23x - 29y = 98$, and $29x - 23y = 110$

then the value of $\sqrt{x^2 + y^2}$ is.

$$6(x+y) = 12^2$$

$$52(x-y) = 208$$

$$x = 3$$
$$y = -1$$

यदि $23x - 29y = 98$, और $29x - 23y = 110$

तो $\sqrt{x^2 + y^2}$ का मान है।

☒ (a) $\sqrt{10}$

(c) 10

(b) $\sqrt{5}$

(d) 7

$\sqrt{10}$ (A)

(21)

If $x = \frac{y}{y+1}$ and $y = \frac{a-2}{2}$, then the value

of $x(y+2) + \frac{x}{y} + \frac{y}{x}$ is

यदि $x = \frac{y}{y+1}$ तथा $y = \frac{a-2}{2}$, तो $x(y+2) +$

$\frac{x}{y} + \frac{y}{x}$ का मान होगा।

(a) 1

(c) -1

(b) 0

(d) a

(D)

$$y=1$$

$$x=\frac{1}{2}$$

$$a=4$$

$$\frac{1}{2}(3) + \frac{1}{2} + 2$$

$$4$$

a ✓

(21)

$$xy + x = y$$

$$xy = y - x$$

$$\frac{y + x + x^2 + y^2}{y - x}$$

$$\frac{y^2 = x^2 + x^2 + y^2}{y - x}$$

$$\frac{2yx}{xy} = \frac{2y}{x}$$

If $x = \frac{y}{y+1}$ and $y = \frac{a-2}{2}$, then the value

of $x(y+2) + \frac{x}{y} + \frac{y}{x}$ is

Rearrangement

यदि $x = \frac{y}{y+1}$ तथा $y = \frac{a-2}{2}$, तो $x(y+2) +$

$\frac{x}{y} + \frac{y}{x}$ का मान होगा।

(a) 1

(b) 0

(c) -1

(d) a

$$= 2(y+1) = 2\left(\frac{a-2}{2} + 1\right) = a$$

(D)

22

If $2x^4 - 166x^2 + 2 = 0$ then value of $x^3 - x^{-3}$ is.

यदि $2x^4 - 166x^2 + 2 = 0$ तो $x^3 - x^{-3}$ का मान होगा।

(a) 758

(c) 739

☒ (b) 756

(d) 737

B

$$x^4 - 83x^2 + 1 = 0$$

$$x^2 + \frac{1}{x^2} = 83$$

$$x - \frac{1}{x} = 9$$

① CND (23)

Find the value of x if $\frac{\sqrt{a+x} + \sqrt{a-x}}{\sqrt{a+x} - \sqrt{a-x}} = b$.

$$\sqrt{\frac{a+x}{a-x}} = \frac{b+1}{b-1}$$

$$\frac{a+x}{a-x} = \frac{(b+1)^2}{(b-1)^2}$$

$$\frac{a}{x} = \frac{2(b^2+1)}{2-4b}$$

$$x = \frac{2ab}{b^2+1}$$

यदि $\frac{\sqrt{a+x} + \sqrt{a-x}}{\sqrt{a+x} - \sqrt{a-x}} = b$ तो x का मान है।

(a) $\frac{2ab}{b^2+1}$

$a=5$
 $x=4$

(b) $-\frac{2ab}{a+b}$

(c) $\frac{a+b}{2ab}$

(A)

(2) $\frac{4}{2} = \frac{b}{2}$ (d) $\frac{b^2+1}{2ab}$

24

If $ax^2 + bx + c = a(x-p)^2$, the relation among a , b , and c is.

यदि $ax^2 + bx + c = a(x-p)^2$, तो a , b , and c निम्न में कौन सा सही है।

~~$ax^2 + bx + c$~~

~~$= ax^2 + ap^2 - 2apx$~~ (a) $abc=1$

(b) $2b=a + c$

(c) $b^2 = ac$

~~(d) $b^2=4ac$~~

D

$b = -2ap$
 $c = ap^2$
 $\rightarrow b^2 = 4a^2p^2$

$= 4aap^2$
 $b^2 = 4ac$

25

$$\frac{-2p^3 - 2q^3 - 2r^3}{pqr}$$

$$pqr$$

$$\frac{-2(p^3 + q^3 + r^3)}{pqr}$$

$$pqr$$

$$\frac{-2 \times 3pqr}{pqr}$$

$$\cancel{pqr}$$

$$-6 \text{ (D)}$$

If $p + q + r = 0$ then the value of $\frac{2p^2(q+r) + 2q^2(p+r) + 2r^2(p+q)}{pqr}$.

यदि $p + q + r = 0$ तो

$\frac{2p^2(q+r) + 2q^2(p+r) + 2r^2(p+q)}{pqr}$ निम्न का मान

होगा।

(a) $3pqr$

(b) $\frac{1}{pqr}$

(c) 6

(d) -6

26

$$x = \frac{\sqrt{3}+1}{2}$$

$$2x-1 = \sqrt{3}$$

$$4x^2+1-4x=3$$

$$4x^2-4x=2$$

$$2x^2-2x=1$$

$$4x^3 = 4x^2 + 2x$$

If $x = \frac{1}{\sqrt{3}-1}$ then find the value of $4x^3 +$

$$2x^2 - 8x - 3.$$

यदि $x = \frac{1}{\sqrt{3}-1}$ तो $4x^3 + 2x^2 - 8x - 3$ का मान

बताओं।

(a) 0

(c) -2

$$4x^3 + 2x^2 - 8x - 3$$

(b) 2

(d) $\sqrt{2}$

$$6x^2 = 6x - 3$$

$$3-3=0 \text{ (A)}$$

(27) Find the value of x $\frac{1}{a+b+x} - \frac{1}{x} = \frac{1}{a} + \frac{1}{b}$.

Solve नहीं

करना

Option से

x का मान बताओं यदि $\frac{1}{a+b+x} - \frac{1}{x} = \frac{1}{a} + \frac{1}{b}$ है।

(a) ~~$-a, b$~~

(c) $a, -b$

~~(b) $-a, -b$~~

(d) a, b

(B)

28

$$\sqrt{x} = a$$

$$\sqrt{y} = b$$

$$a^3 + b^3 = 183$$

$$3 \times a^2 b + a b^2 = 182$$

$$(a+b)^3 = 729$$

$$a+b=9$$

$$\rightarrow ab(a+b) = 182$$

$$ab = \frac{182}{9}$$

x and y are positive real numbers such

that $x\sqrt{x} + y\sqrt{y} = 183$ and $x\sqrt{y} + y\sqrt{x} = 182$

then value of $\frac{18}{5} (x+y)$. $\frac{18}{5} (81 - \frac{364}{9})$

यदि **x** तथा **y** घनात्मक प्राकृतिक संख्याएँ हो तो

$x\sqrt{x} + y\sqrt{y} = 183$ तथा $x\sqrt{y} + y\sqrt{x} = 182$ तब $\frac{18}{5}$

(x + y) का मान होगा।

(a) 73

(c) 63

(B)

✓ (b) 146

(d) 126

$$\frac{18}{5} \times \frac{73}{9}$$

29

If $a^2 + 4b^2 + 16c^2 = 48$ and $ab + 4bc + 2ca = 24$. Then what is the value of $a^2 + b^2 + c^2$?

$$a^2 + 4b^2 + 16c^2 = 48$$

$$2 \times ab + 4bc + 2ca = 24$$

$$x^2 + y^2 + z^2 = 48$$

$$xy + yz + zx = 24$$

$$(x-y)^2 + (y-z)^2 + (z-x)^2 = 0$$

$$a=2b=4c$$

$$a=4 \\ b=2 \quad c=1$$

यदि $a^2 + 4b^2 + 16c^2 = 48$ तथा $ab + 4bc + 2ca = 24$ तब $a^2 + b^2 + c^2$ का मान होगा।

(a) 12

(b) 16

(d) 31

$$4^2 + 2^2 + 1^2$$

30

$$\sqrt[3]{x} \left(\frac{1}{9} + \frac{2}{9} + \frac{3}{18} \right) = 1$$

$$\sqrt[3]{x} = 2$$

$$x = 8$$

If $\sqrt[3]{\frac{x}{729}} + \sqrt[3]{\frac{8x}{729}} + \sqrt[3]{\frac{27x}{5832}} = 1$ then find the value of x .

$$729 \times 8$$

यदि $\sqrt[3]{\frac{x}{729}} + \sqrt[3]{\frac{8x}{729}} + \sqrt[3]{\frac{27x}{5832}} = 1$ तो x का मान बताओं

(a) 1

(c) 3

☒ (b) 8

(d) 4

B

(31)

$$\frac{1}{a} = \frac{p+q}{p-q}$$

$$\frac{1+q}{1-a} = \frac{p}{q}$$

$$\frac{p}{q} \times \frac{q}{r} \times \frac{r}{p}$$

1 (A)

If $a = \frac{p-q}{p+q}$, $b = \frac{q-r}{q+r}$, $c = \frac{r-p}{r+p}$ then the

value of $\frac{(1+a)(1+b)(1+c)}{(1-a)(1-b)(1-c)}$ is.

यदि $a = \frac{p-q}{p+q}$, $b = \frac{q-r}{q+r}$, $c = \frac{r-p}{r+p}$ तब

$\frac{(1+a)(1+b)(1+c)}{(1-a)(1-b)(1-c)}$ का मान बताओं

(a) 1

(c) 121

(b) 0

(d) 11

32

If $\sqrt{m} + \sqrt{n} - \sqrt{p} = 0$, then the value of $(m + n - p)^2$ is.

$$\sqrt{m} + \sqrt{n} = \sqrt{p}$$

यदि $\sqrt{m} + \sqrt{n} - \sqrt{p} = 0$, तो $(m + n - p)^2$ का मान बताओं।

$$m + n + 2\sqrt{mn} = p$$

$$m + n - p = -2\sqrt{mn}$$

$$(-2\sqrt{mn})^2 = 4mn$$

(a) mn

(c) $2mn$

(b) $-mn$

~~(d) $4mn$~~

Ⓓ

33

If $x = \frac{3 + \sqrt{5}}{2}$ and $y = x^3$, then y satisfies

the equation.

$$\frac{27 + 5\sqrt{5} + 27\sqrt{5} + 45}{8}$$

यदि $x = \frac{3 + \sqrt{5}}{2}$ तथा $y = x^3$, तो y निम्न समीकरण को

सन्तुष्ट करता है।

$$y \rightarrow 9 + 4\sqrt{5}$$

$$y^2 = 161 + 72\sqrt{5}$$

$$18y = 162 + 72\sqrt{5}$$

$$18y - y^2 = 1 \Rightarrow y^2 - 18y + 1 = 0$$

✓ (a) $y^2 - 18y + 1 = 0$ (b) $y^2 + 18y + 1 = 0$

(c) $y^2 - 18y - 1 = 0$ (d) $y^2 + 18y - 1 = 0$

(A)

34

If $a + b + c = 1$, $a^2 + b^2 + c^2 = 9$ and $a^3 + b^3 + c^3 = 1$, then find the value of

$$\frac{1}{a} + \frac{1}{b} + \frac{1}{c}$$

$\frac{ab+bc+ca}{abc}$

यदि $a + b + c = 1$, $a^2 + b^2 + c^2 = 9$ तथा $a^3 + b^3 + c^3 = 1$, तो निम्न $\frac{1}{a} + \frac{1}{b} + \frac{1}{c}$ का मान बताओं

(a) 4

☒ (b) 1

(c) $\frac{1}{2}$

$1 - \frac{1}{2} + \frac{1}{2}$

(d) $\frac{1}{4}$

☒ (b)

33

$$abcd = (abcd)^3$$

$$(abcd)^2 = 1$$

$$a = b = c = d = 1$$

$$\frac{4^4}{4^2} = 4^2 = 16 \text{ (A)}$$

If a, b, c, d are positive integers such that $a = bcd, b = cda, c = dab$ and $d = abc$

then the value of $\frac{(a + b + c + d)^4}{(ab + bc + cd + da)^2}$.

यदि a, b, c, d घनात्मक पूर्णांक है, तो $a = bcd, b = cda, c = dab, d = abc$ तो $\frac{(a + b + c + d)^4}{(ab + bc + cd + da)^2}$

का मान होगा।

(a) $\frac{16}{2}$

(b) $\frac{4}{1}$

—

36

If $a^x = (x + y + z)^y$, $a^y = (x + y + z)^z$, $a^z = (x + y + z)^x$, then

यदि $a^x = (x + y + z)^y$, $a^y = (x + y + z)^z$, $a^z = (x + y + z)^x$, तो

$$a^{x+y+z} = (x+y+z)^{x+y+z}$$

(a) $3(x + y + z) = a$

(b) $2a = x + y + z$

(c) $x + y + z = a$

(d) $x = y = z = \frac{a}{3}$



37

If a, b, c are such that $a + b + c = 2$, $a^2 + b^2 + c^2 = 6$, $a^3 + b^3 + c^3 = 8$, then $a^4 + b^4 + c^4$ is equal to.

$16+1+1$

$$(a+b+c)^2$$

यदि a, b, c इस प्रकार है $a + b + c = 2$, $a^2 + b^2 + c^2 = 6$, $a^3 + b^3 + c^3 = 8$, तब $a^4 + b^4 + c^4$ का

$$= a^4 + b^4 + c^4$$

$$+ 2abc(a+b+c)$$

(a) 10

(c) 18

(b) 12

(d) None of these

(c)

$$(a^2 + b^2 + c^2)^2 - 2(a^2b^2 + b^2c^2 + c^2a^2)$$

38

If $\frac{2x + 3y}{a - 2b} = \frac{4y + 7z}{3b - c} = \frac{6z + 5x}{2c - 3a}$, find the

$3 \times 2x + 3y = k(a - 2b)$ value of $11x + 17y + 20z$.

$2 \times 4y + 7z = k(3b - c)$ यदि $\frac{2x + 3y}{a - 2b} = \frac{4y + 7z}{3b - c} = \frac{6z + 5x}{2c - 3a}$ तो $11x + 17y + 20z$
 $6z + 5x = k(2c - 3a)$

$11x + 17y + 20z$
+ $20z$ का मान होगा।

$= k(\cancel{3a} - \cancel{6b} + \cancel{6b} - \cancel{2c} + \cancel{2c} - \cancel{3a})$
 $= 0$

(a) 0
(b) 1
(c) 2
(d) None of these

A

eqn Multiplication

39

$\left(\frac{a}{a+1}\right)^2 - 5\left(\frac{a}{a+1}\right) + 6 = 0$ then $\left(1 + \frac{1}{a}\right)$ equals $\frac{a+1}{a}$ to.

$$x^2 - 5x + 6 = 0$$
$$(x-3)(x-2) = 0$$

$$x = 3$$
$$x = 2$$

$$1\frac{1}{3}, \frac{1}{2}$$

(a) 2 or 3

(c) 1

~~(b)~~ $\frac{1}{2}$ or $\frac{1}{3}$

(d) $-\frac{1}{2}$ or $-\frac{1}{3}$

13

40

$z = 3 + \sqrt{10}$, then $z^3 \frac{-1}{z^3}$

(a) 334

(b) 216

☒ (c) 234

(d) 254

$$\frac{1}{z} = \sqrt{10} - 3$$

$$z - \frac{1}{z} = 6$$

(41)

$$2 \left(z + \frac{1}{z} \right) = \sqrt{8} z^{48} + z^{40} + \cancel{z^{32}} + \cancel{z^{20}} + 1 = ?$$

(a) 4

~~(c) 3~~

(b) 1

(d) 2

$$z + \frac{1}{z} = \sqrt{2}$$

$$z^2 + \frac{1}{z^2} = 0$$

$$z^4 + 1 = 0$$

$$z^4 = -1$$

(C)